

# Flow Control: TD4-2

## *Overview*

- General issues, passive vs active...
  - Control issues: optimality and learning vs robustness and rough model
  - Model-based control: linear model, nonlinear control
    - Linear model, identification
    - Sliding Mode Control
    - Delay effect
    - Time-delay systems
  - Introduction to delay systems
    - Examples
    - Much a do about delay? Some special features + a bit of maths
    - Time-varying delay
  - Model-based control: nonlinear model, nonlinear control
    - Overview of MF's PhD: Sliding Mode Control
    - Application to the airfoil
    - Application to the Ahmed body (MF and CC'PhDs)
- ...
- Machine Learning and model-free control: + 4h with [Thomas Gomez](#)

# Reducing Car Consumption by Means of a Closed-loop Drag Control

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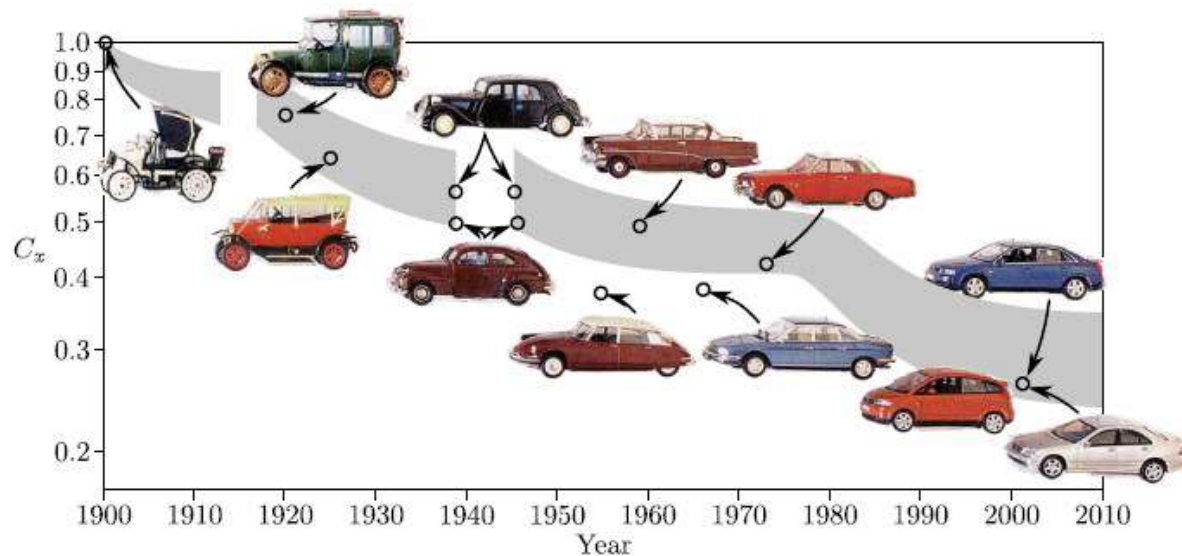
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Jean-Marc Foucaut <sup>5</sup>

<sup>1</sup> LAMIH, <sup>2</sup> CRIStAL, INRIA, <sup>3</sup> pPRIME, <sup>4</sup> IPSA, <sup>5</sup> LMFL.



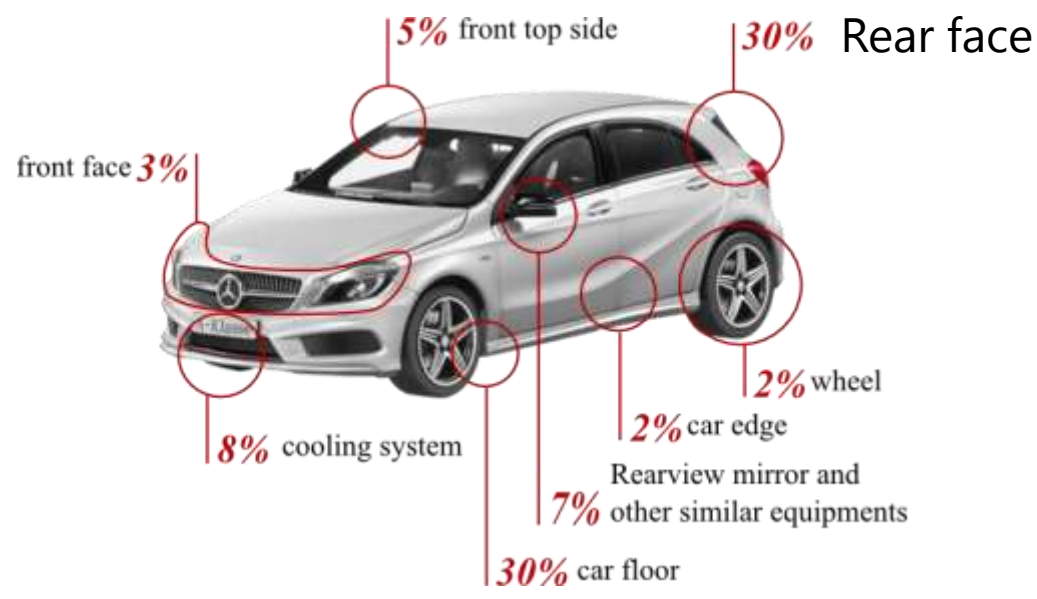
# Transportation industry



PROBLEM

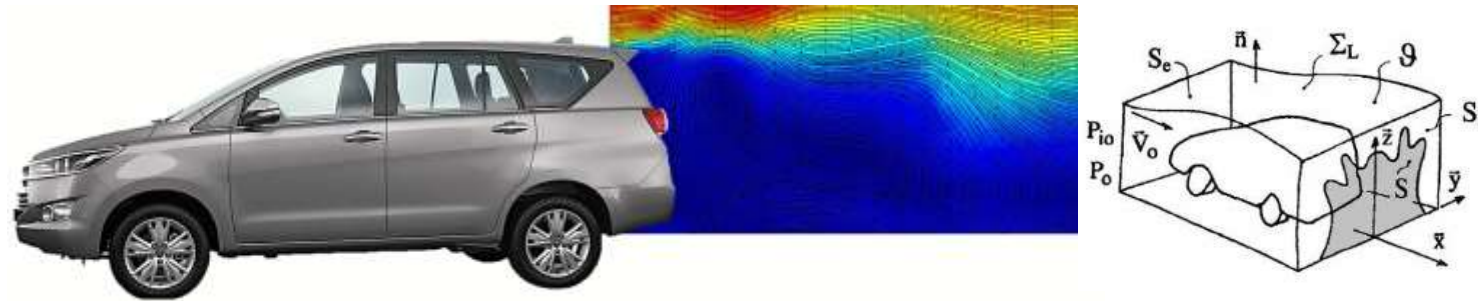


Reduce gas consumption



# Automotive problem

## Flow configuration



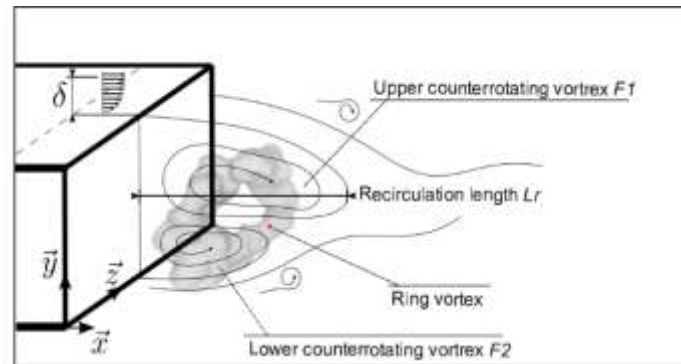
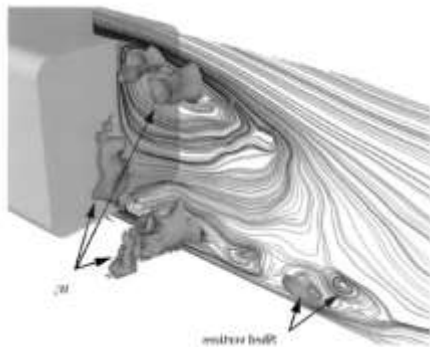
PROBLEM



Reduce gas consumption



Drag reduction



$$F_D = \iint_{S_w} (P_{t\infty} - P_{t_{S_w}}) d\sigma + \frac{1}{2} \rho V_\infty^2 \iint_{S_w} \left( \frac{V_z^2}{V_\infty^2} + \frac{V_z^2}{V_\infty^2} \right) d\sigma - \frac{1}{2} \rho V_\infty^2 \iint_{S_w} \left( 1 - \frac{V_x}{V_\infty} \right)^2 d\sigma$$

# Automotive problem



## Methods of flow control

### ✘ **Passive control**

(Small variation in the geometric configuration)  
Limitations of design requirements

✔ **Active control** (Injection of momentum)



C\_AIR LOUNGE

# Transportation industry

Physical system: Case II – Vehicle



Physical system: Case I – Ahmed body



**PROBLEM**

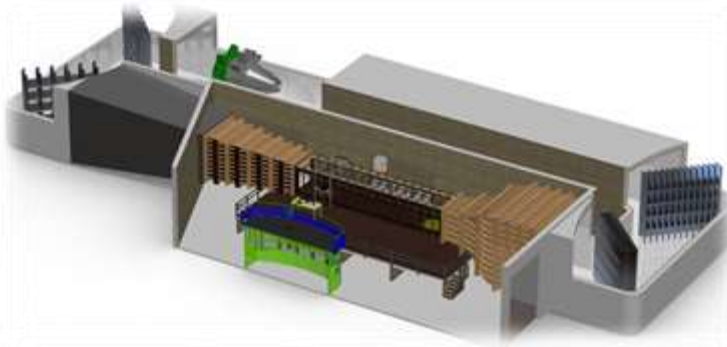


Reduce gas  
consumption



**Drag  
reduction**

# Wind tunnel



## Characteristics:

- ✓ Closed-loop wind tunnel
- ✓ Max. velocity 60m/s (200km/h)
- ✓ Optimal test section:  
2m x 2m, length 10m

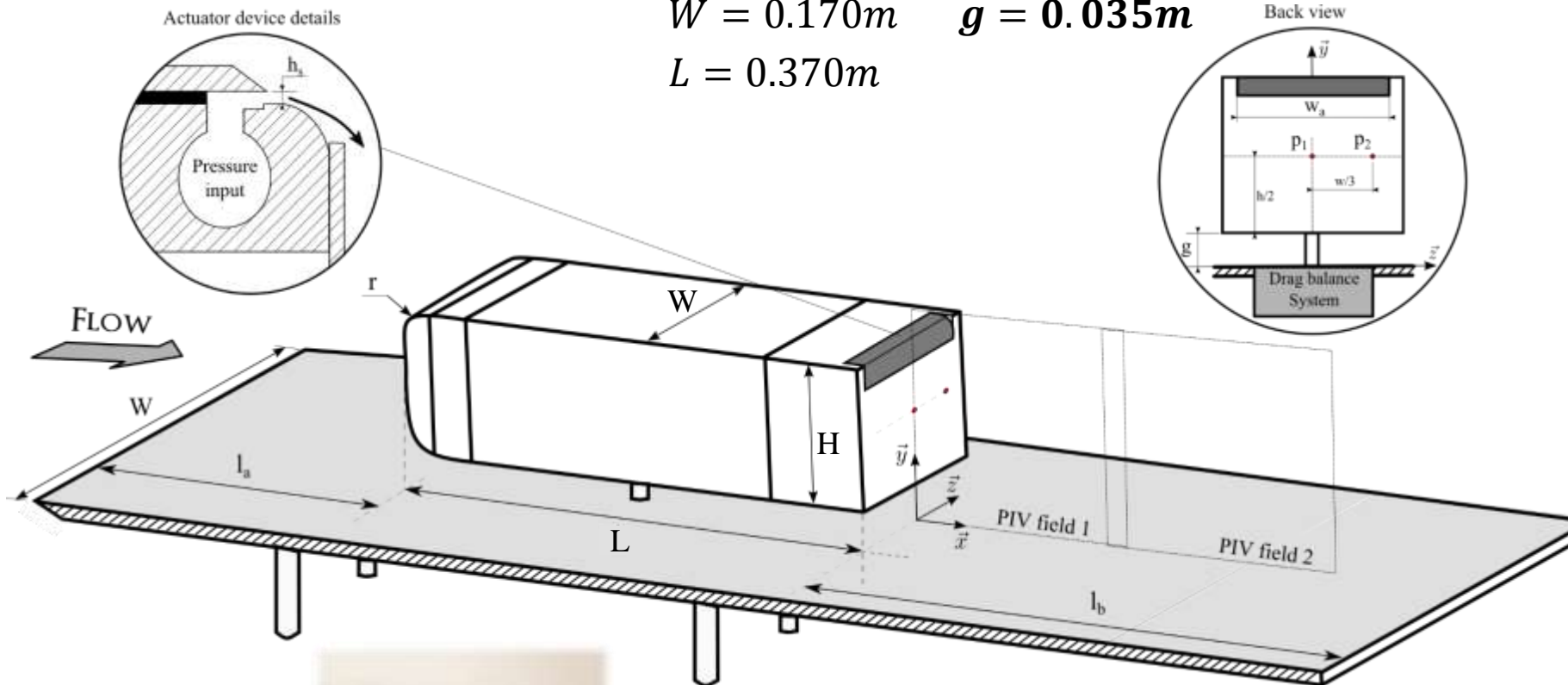


# Physical System I – Ahmed body

$$H = 0.135m \quad r = 0.05m$$

$$W = 0.170m \quad g = 0.035m$$

$$L = 0.370m$$



$$U_\infty = 10m/s$$

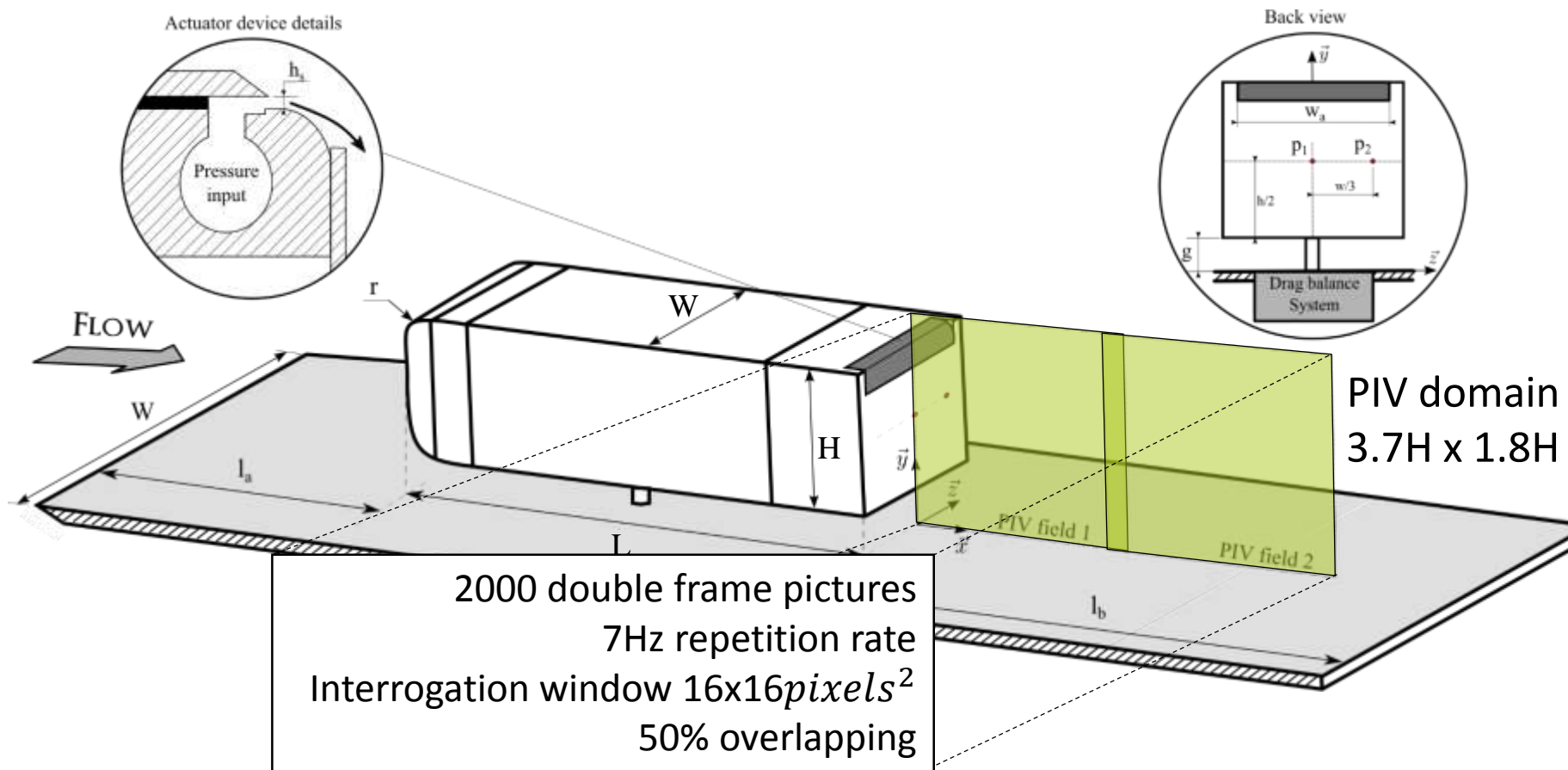
$$Re_{hH} = 9 \times 10^4$$



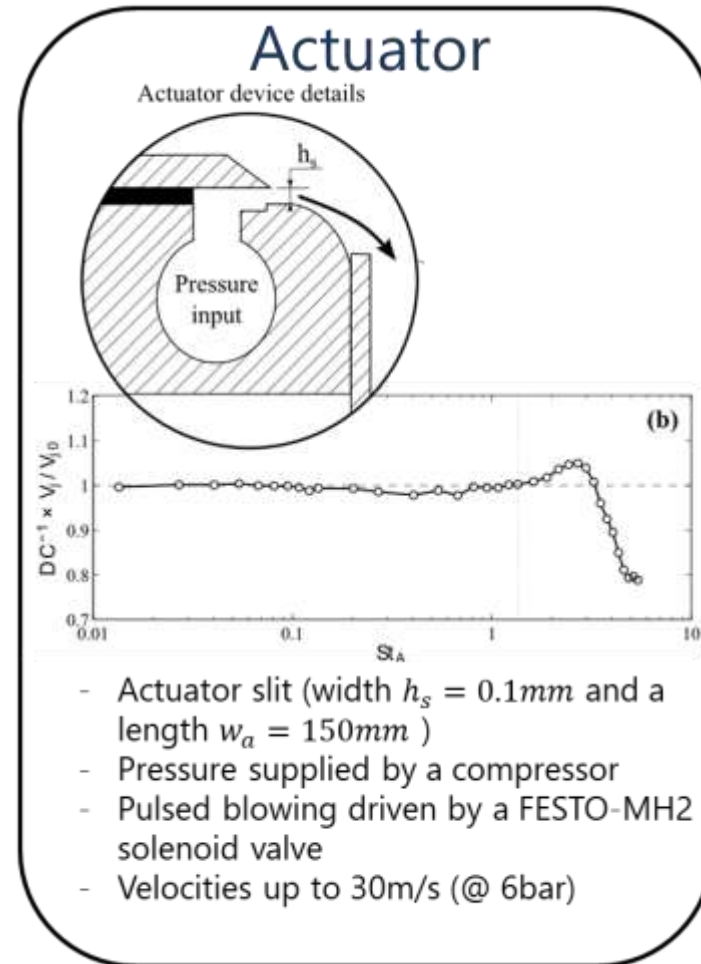
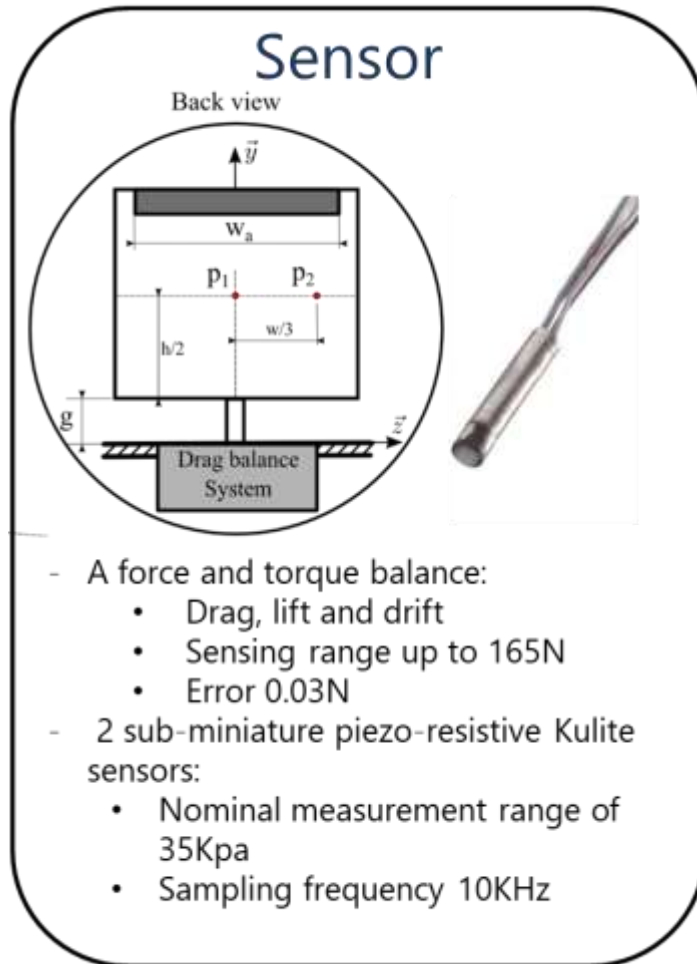


# Physical System

## PIV



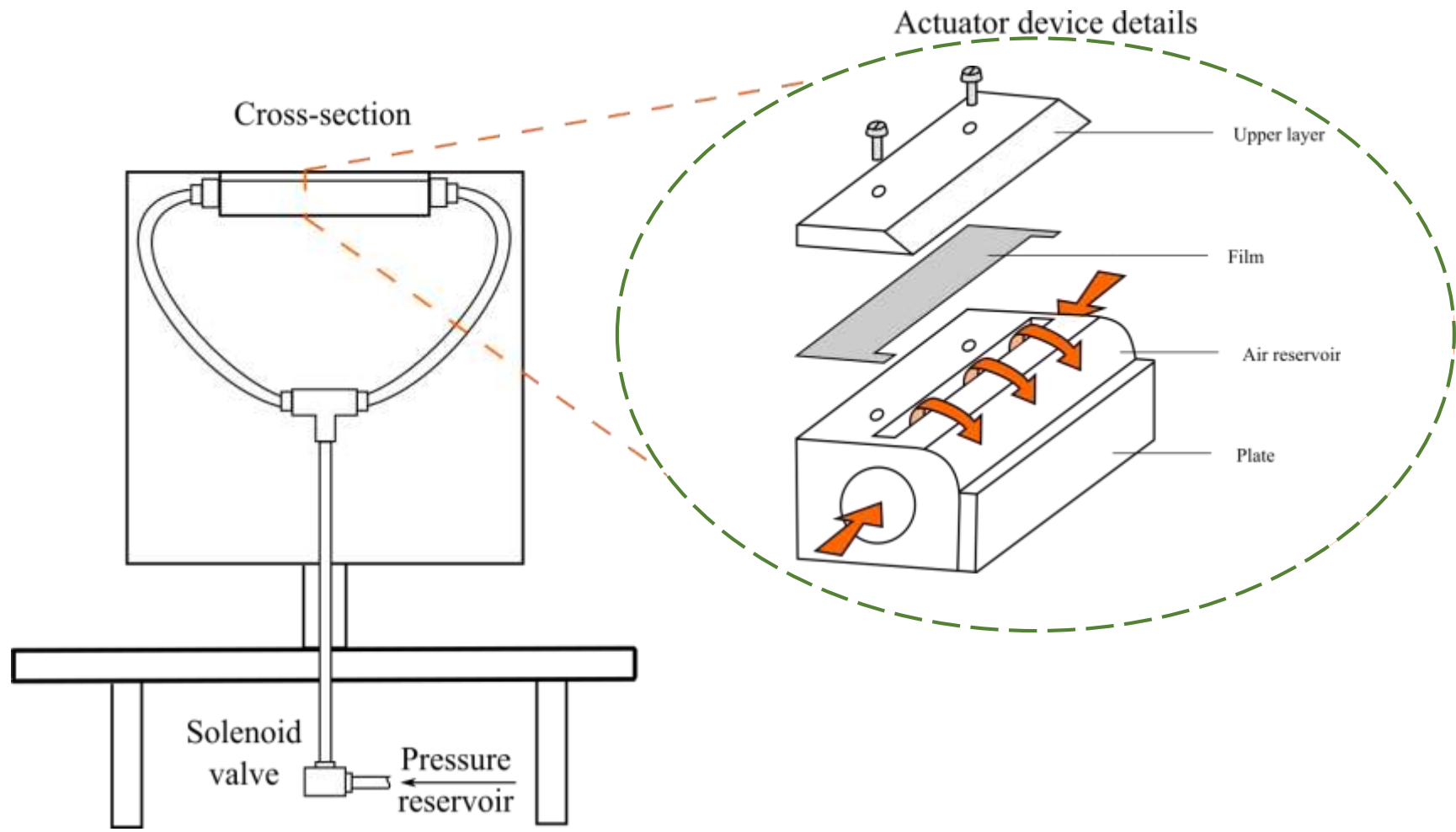
# Sensor and actuator characteristics



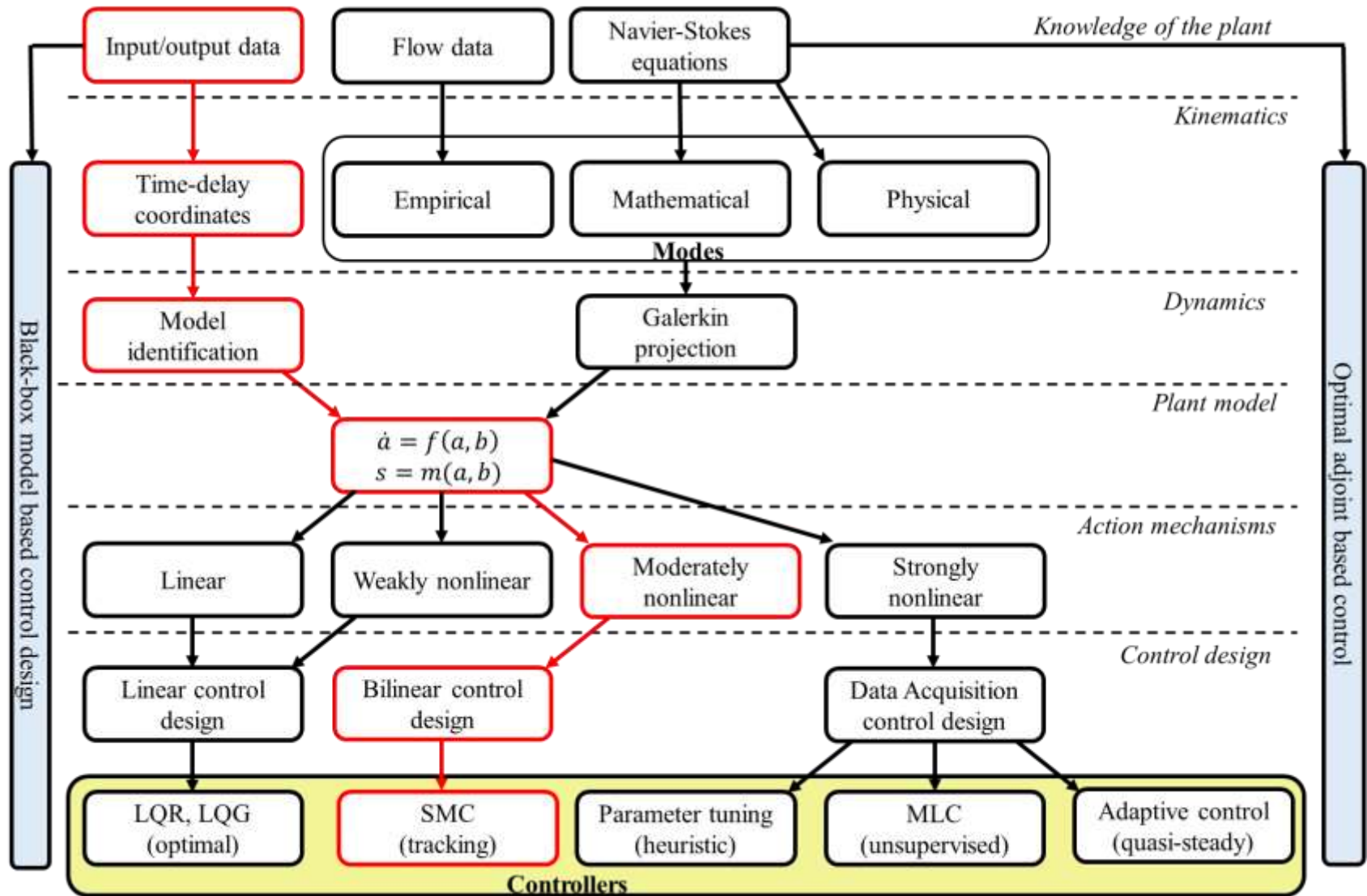
Jet velocity  
 $V_j$

Steady jet velocity  
 $V_{j0} = 16m/s$

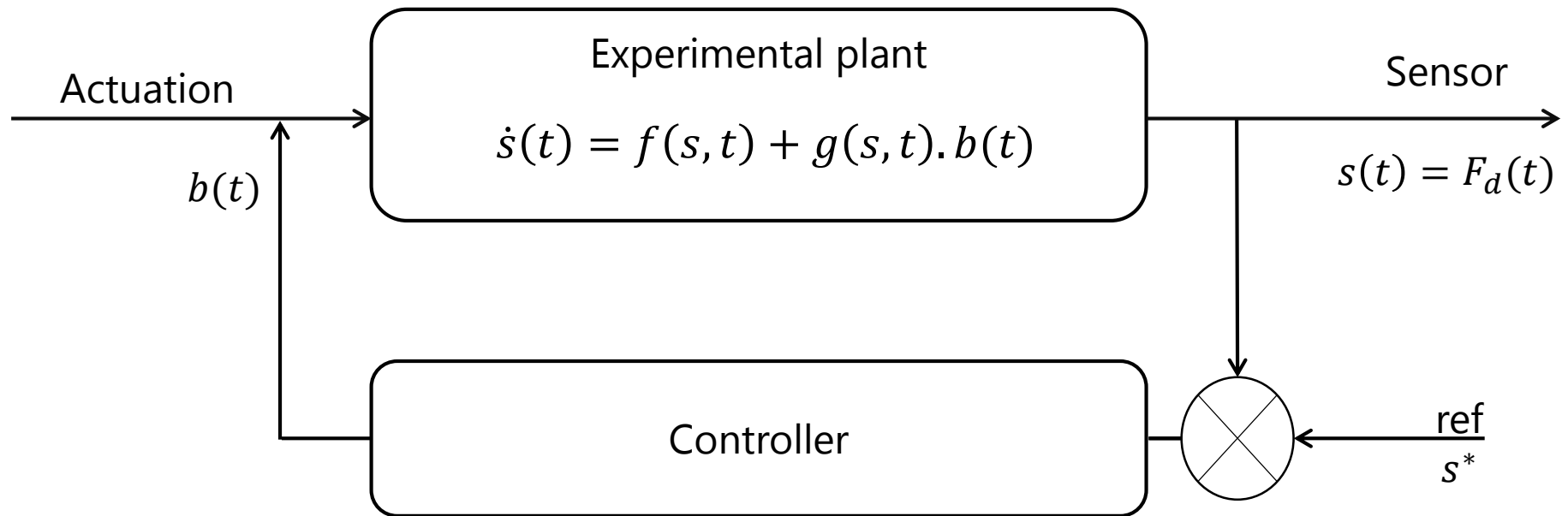
# Flow control

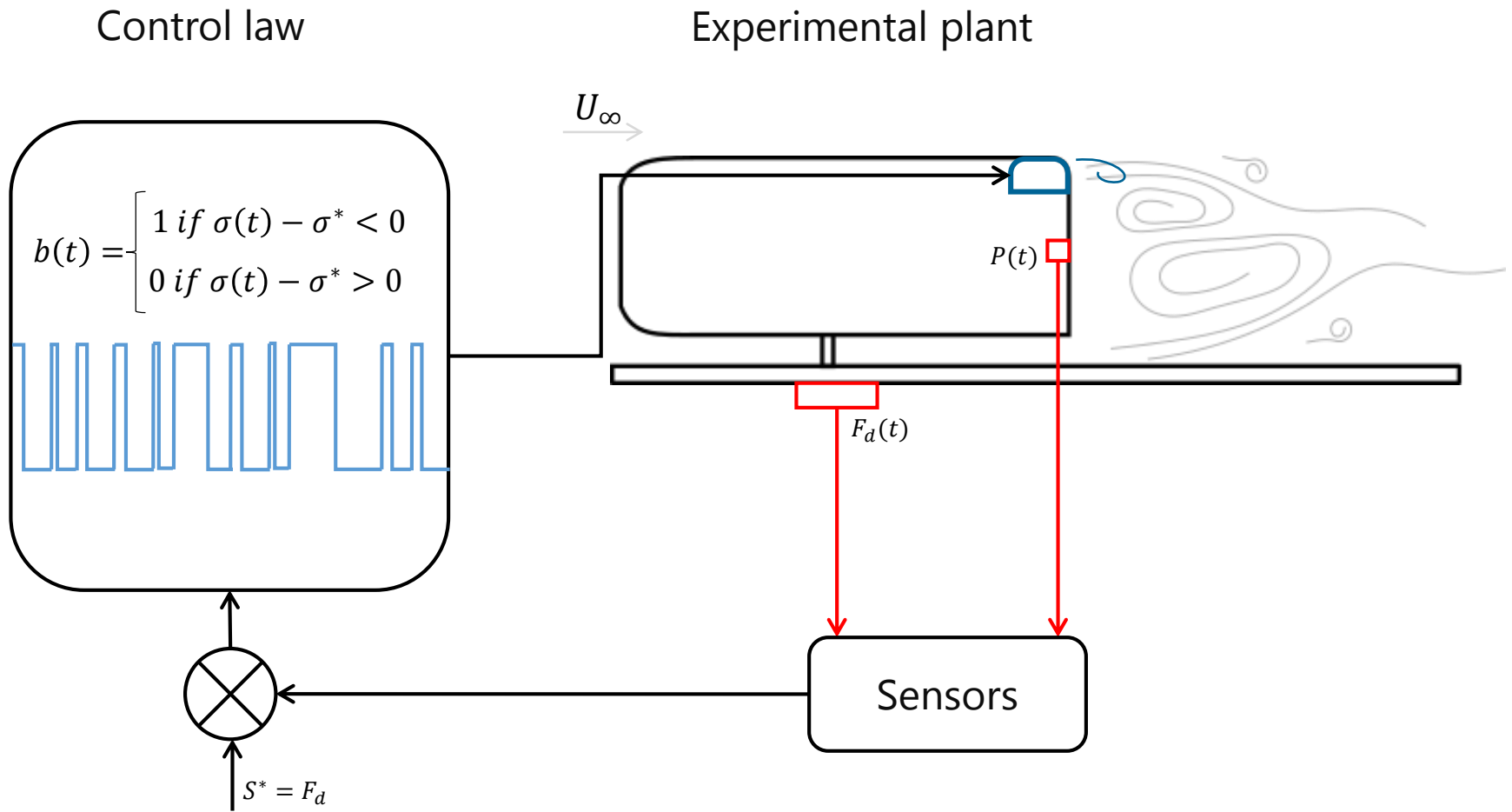


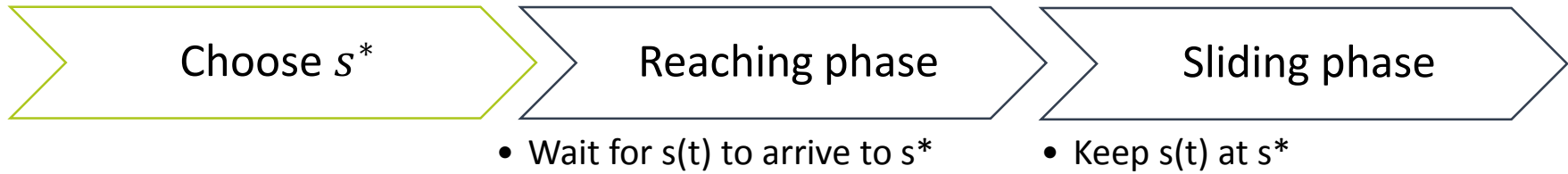
# Flow control

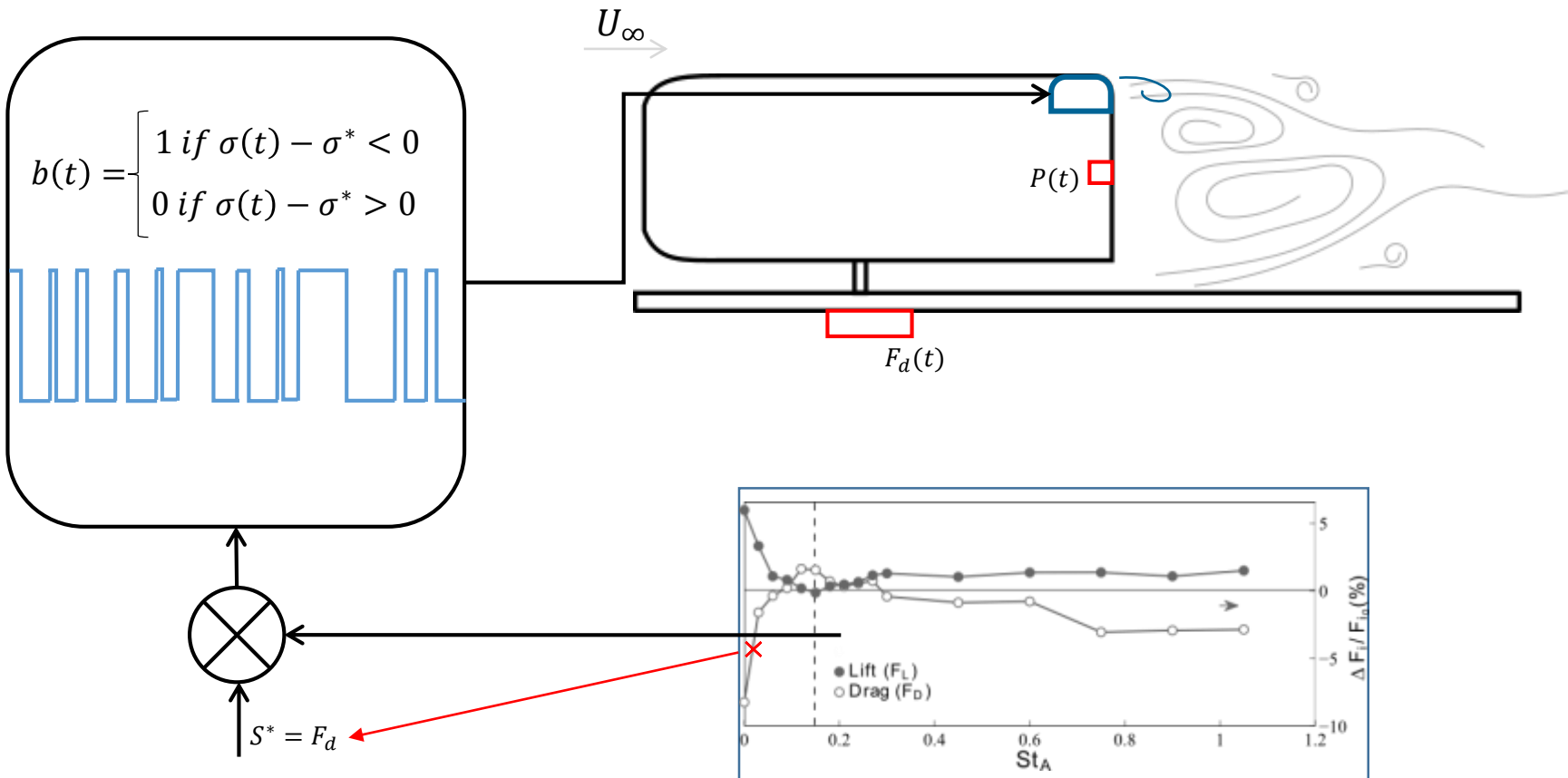


# Sliding Mode Control

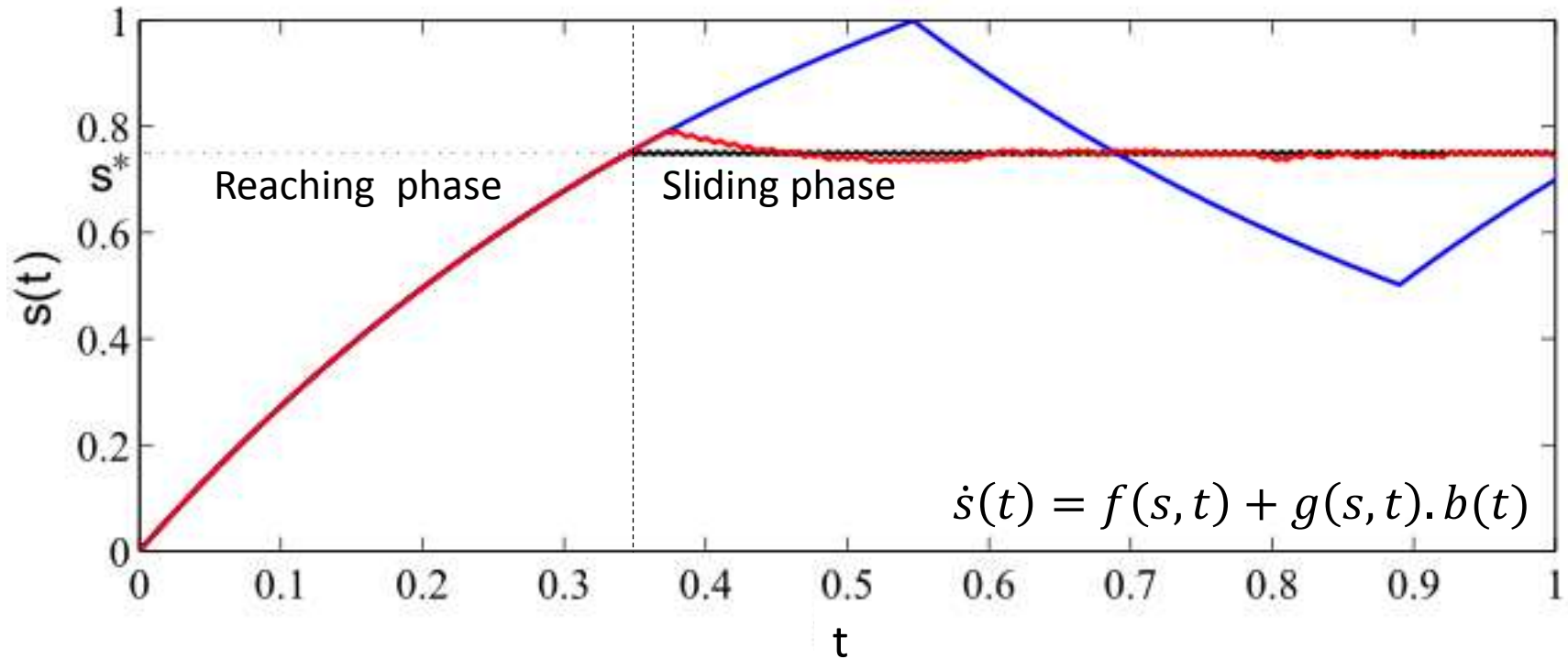
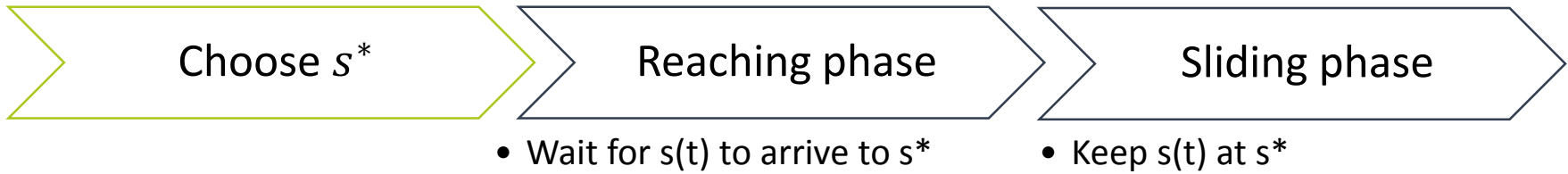








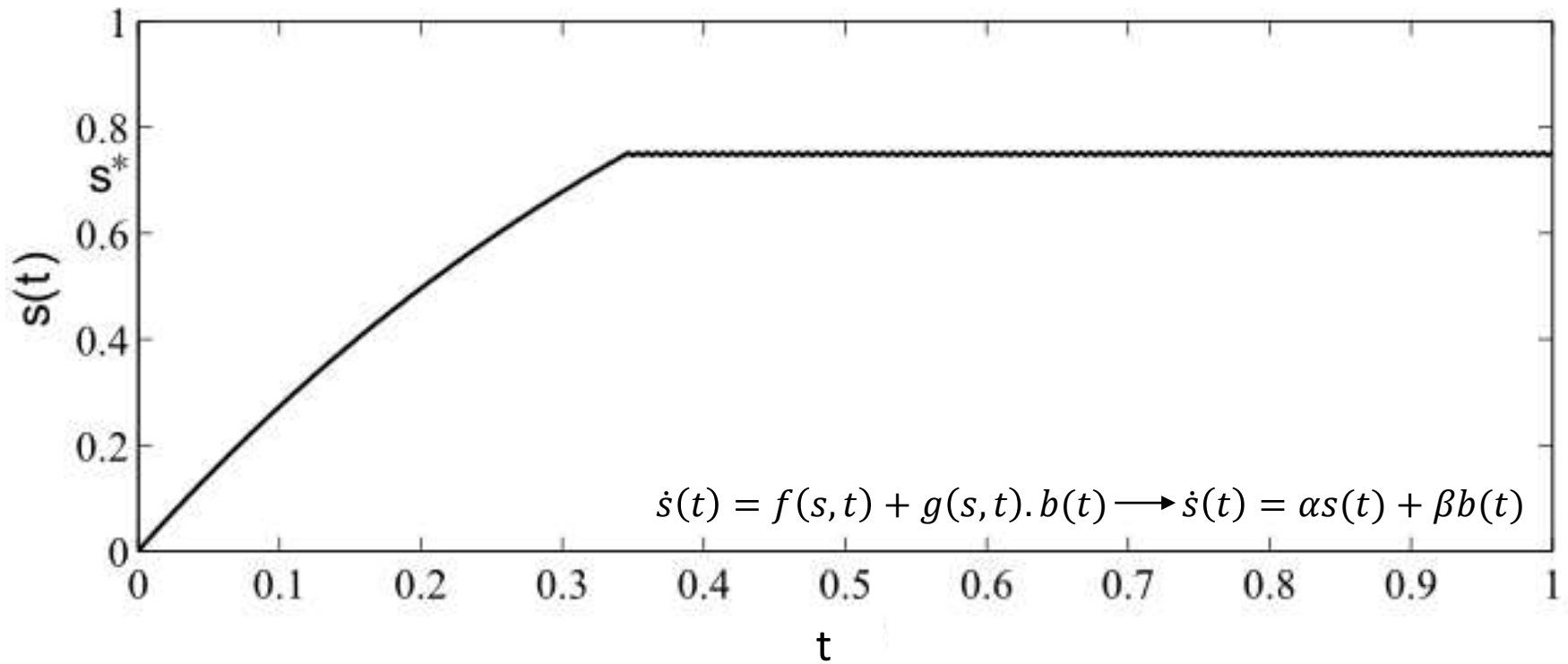




$$\dot{s}(t) = \alpha s(t) + \beta b(t)$$

$$\sigma^* = s(t)$$

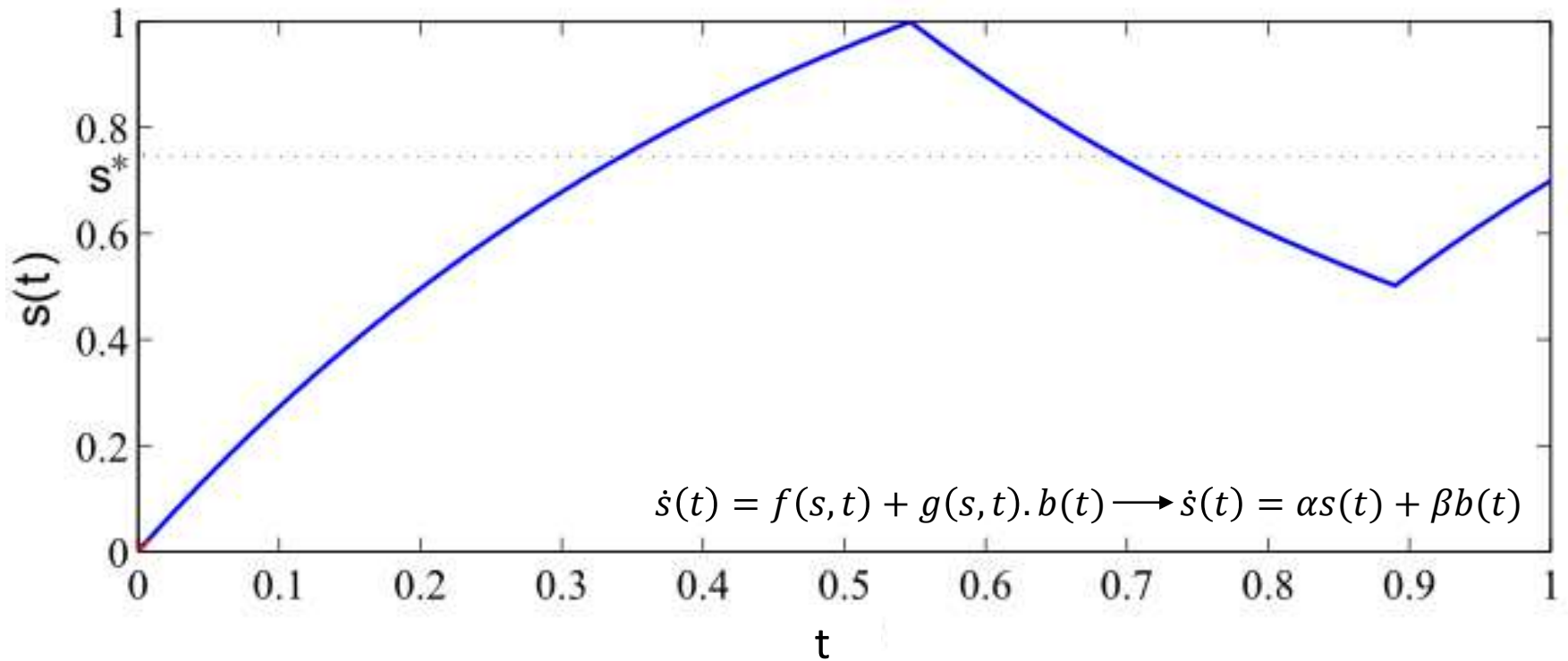
$$b(t) = \begin{cases} 1 & \text{if } \sigma(t) - \sigma^* < 0 \\ 0 & \text{if } \sigma(t) - \sigma^* > 0 \end{cases}$$



$$\dot{s}(t) = \alpha s(t) + \beta b(t - h)$$

$$\sigma^* = s(t)$$

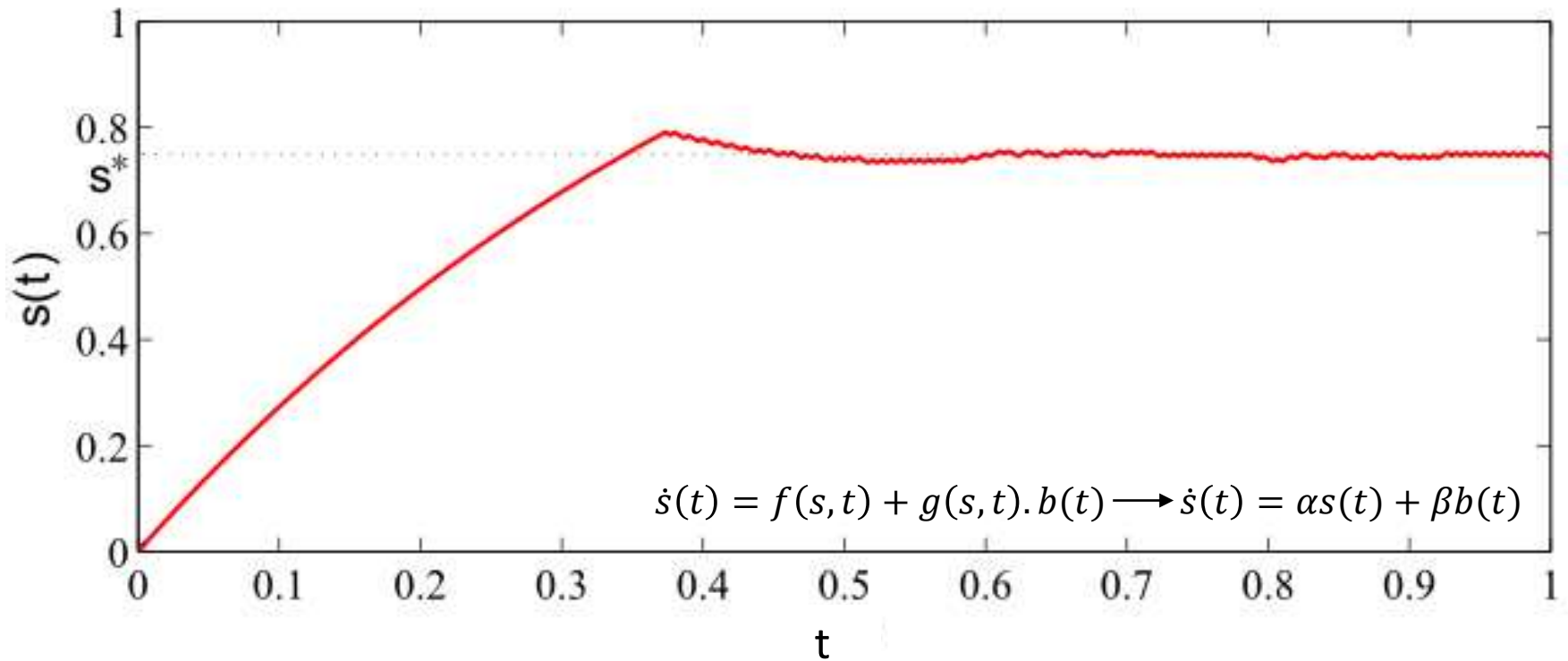
$$b(t) = \begin{cases} 1 & \text{if } \sigma(t) - \sigma^* < 0 \\ 0 & \text{if } \sigma(t) - \sigma^* > 0 \end{cases}$$



$$\dot{s}(t) = \alpha s(t) + \beta b(t - h)$$

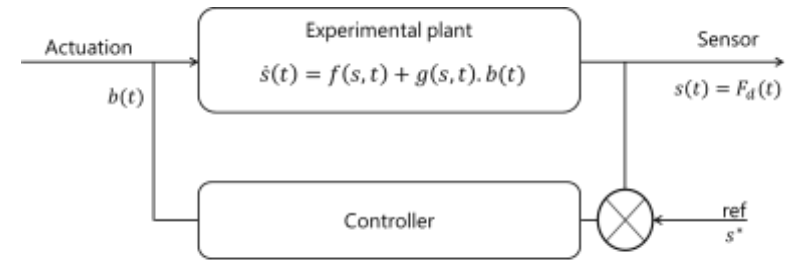
$$\sigma^* = s(t) + \beta \int_{t-h}^t b(p) dp$$

$$b(t) = \begin{cases} 1 & \text{if } \sigma(t) - \sigma^* < 0 \\ 0 & \text{if } \sigma(t) - \sigma^* > 0 \end{cases}$$



# SMC

## Identification



Sensor without delay

$$\dot{s}(t) = \alpha_1 \underbrace{s(t-h)}_{\text{Sensor with delay}} - \alpha_2 \overbrace{s(t)}^{\text{Sensor without delay}} + (\beta - \gamma s(t-h) + \gamma(t-\tau))b(t-h)$$

Sensor with delay

$$FIT(\%) = \left\{ 1 - \frac{\|S_{exp} - S_{sim}\|_{L_2}}{\|S_{exp} - \bar{S}_{exp}\|_{L_2}} \right\} \times 100\% = 53\%$$

$$\alpha_1 = 27.37 \quad \alpha_2 = 32.70 \quad \beta = 1.97 \quad \gamma = 1.92 \quad \tau = 0.18 \quad h = 0.01$$

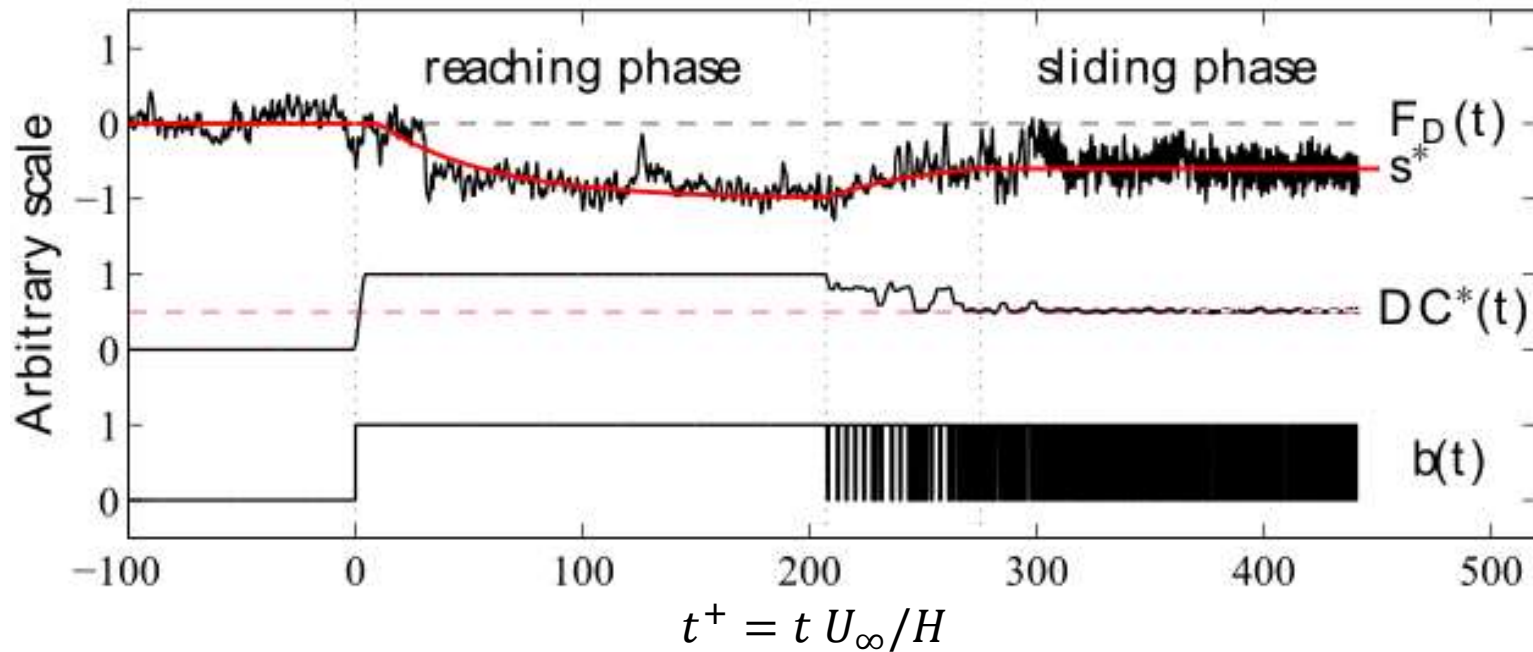
# SMC

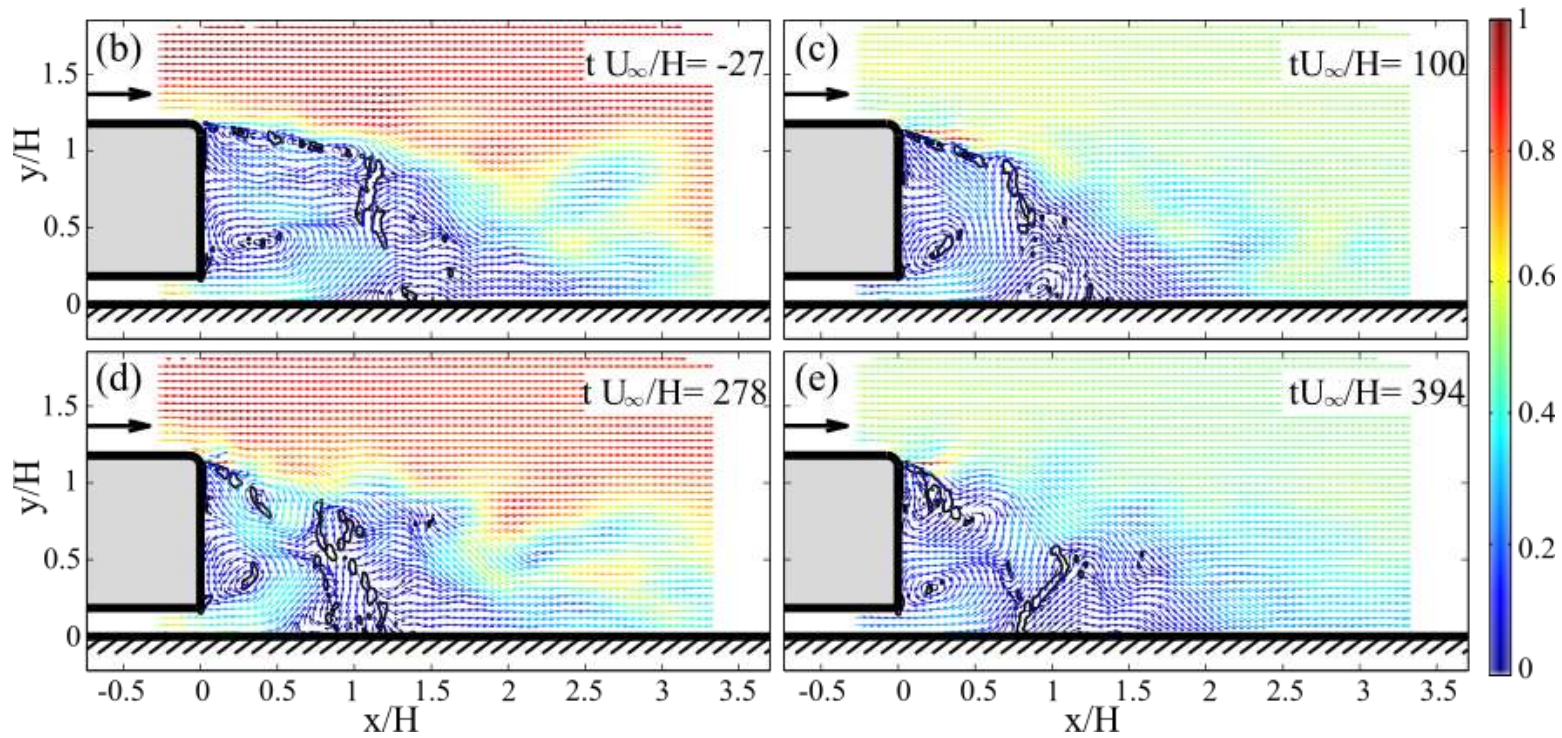
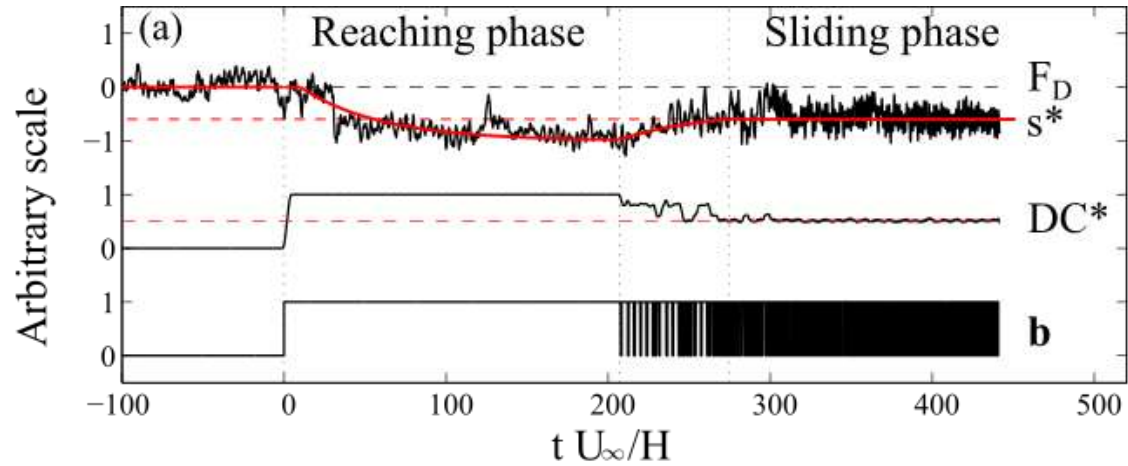
## Sliding mode control

$$\dot{s}(t) = \alpha s(t) + \beta b(t - h)$$

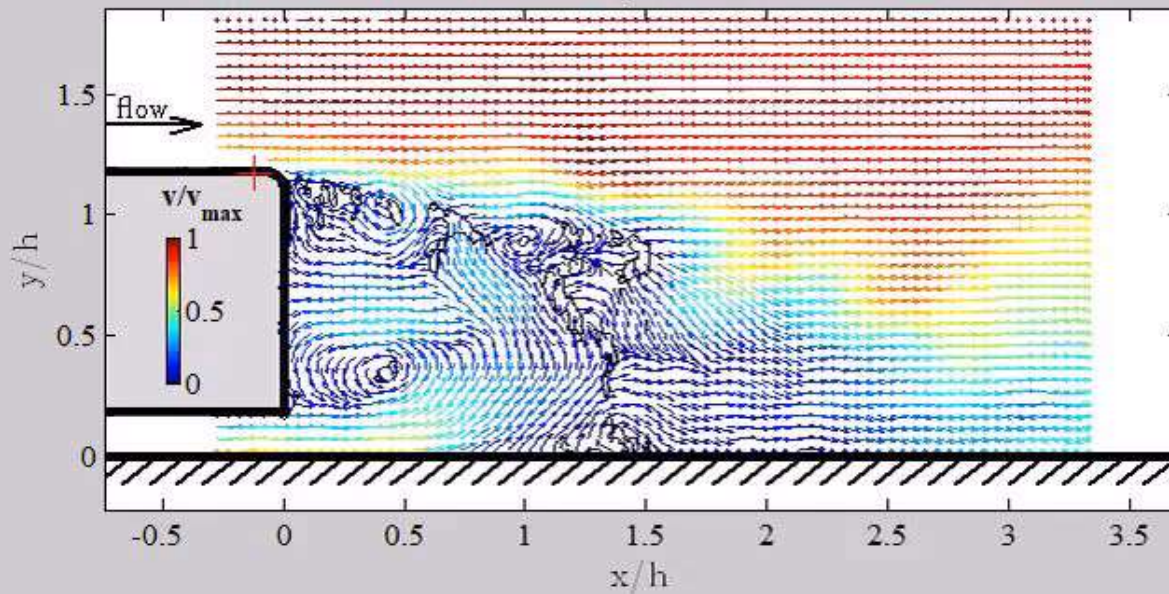
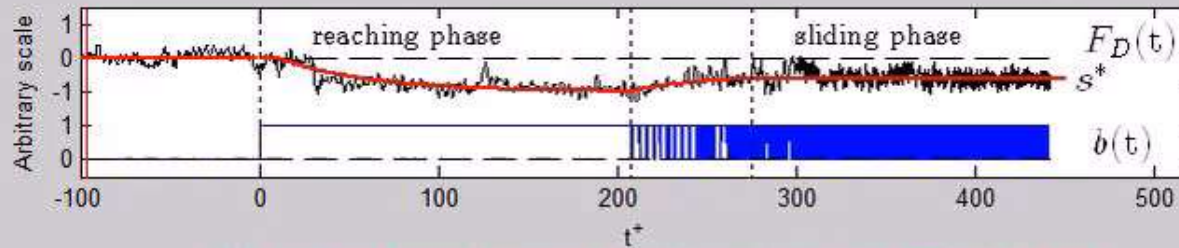
$$b(t) = \begin{cases} 1 & \text{if } \sigma(t) - \sigma^* < 0 \\ 0 & \text{if } \sigma(t) - \sigma^* > 0 \end{cases}$$

$$\sigma^* = s(t) + \gamma \int_{t-\tau+h}^t s(p) dp + \int_{t-h}^t (\alpha_1 s(p) + (\beta - \gamma s(p) + \gamma s(p - \tau + h)) b(p)) dp$$





## Closed-loop control on square back Ahmed body



b: Control

 $F_D$ : Drag $s^*$ : Setpoint

+: Control location

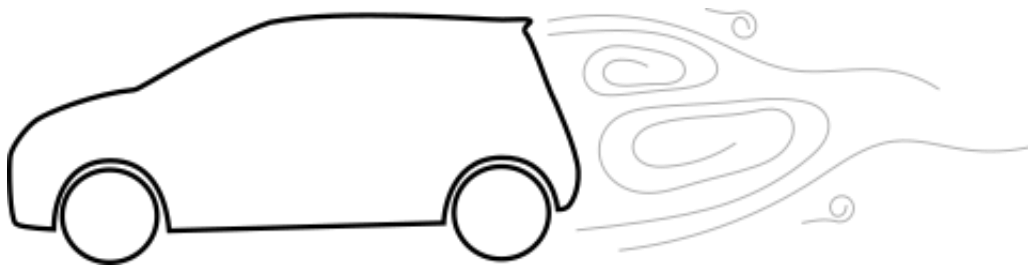


<https://www.youtube.com/watch?v=ZZ0qxbEBm8s>



# Transportation industry

Physical system: Case II – Vehicle



Physical system: Case I – Ahmed body



**PROBLEM**



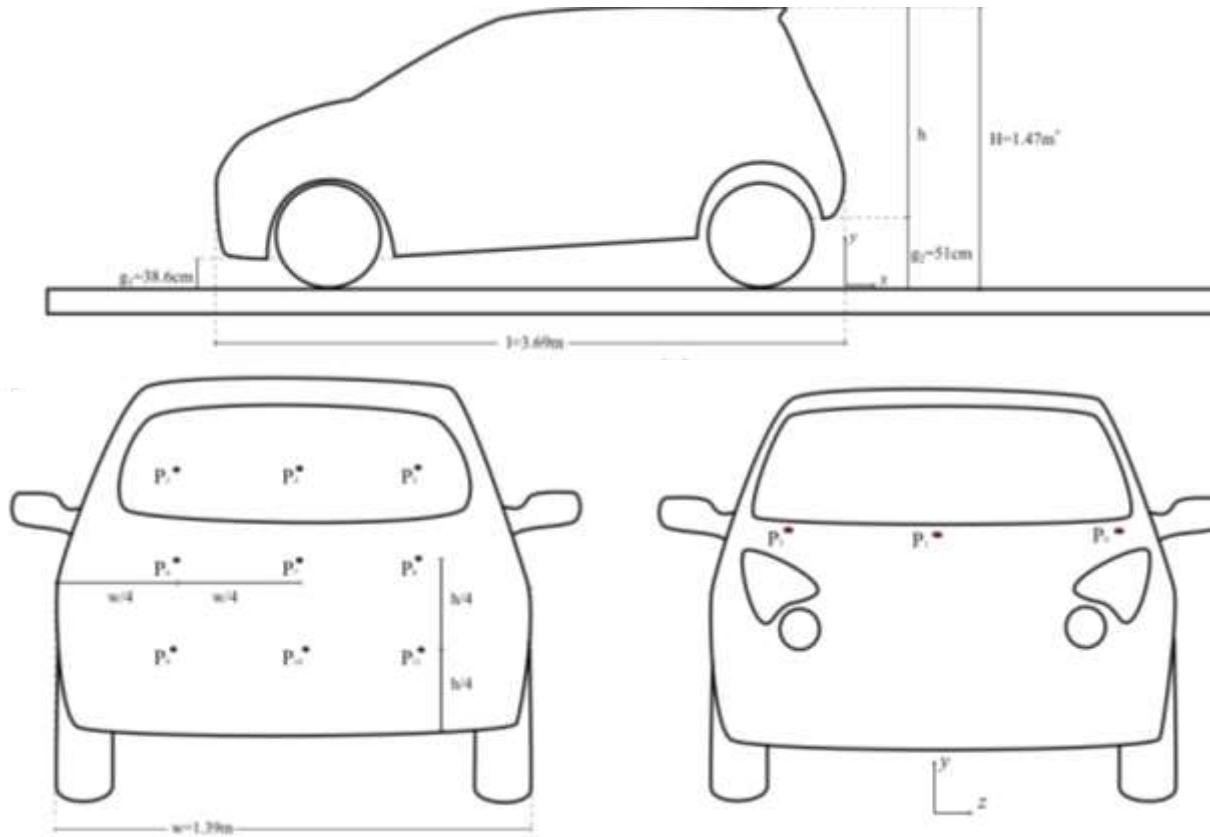
Reduce gas  
consumption



**Drag  
reduction**

# Physical System II – Real car

## Measurement mechanisms



Race track located at Clastres (North of France)

# Physical System II – Real car

## Measurement mechanisms

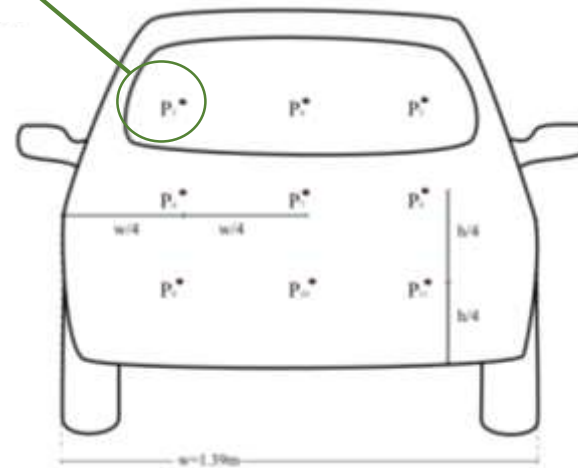
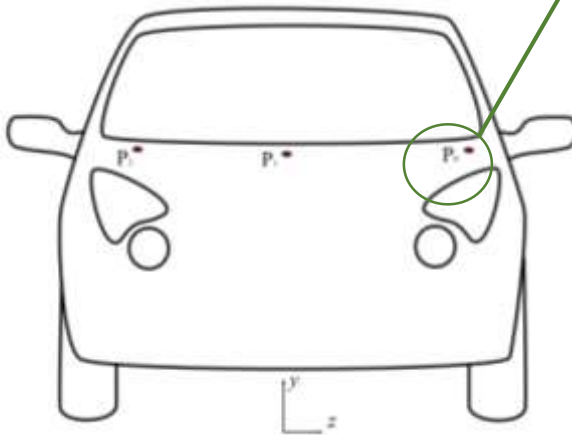
Onorato's relation

$$F_D = \iint_{S_w} (P_t^\infty - P_t^{S_w}) d\sigma - \frac{\rho U_\infty^2}{2} \iint_{S_w} \left( \frac{U_y^2}{U_\infty} + \frac{U_z^2}{U_\infty} \right) d\sigma + \frac{\rho U_\infty^2}{2} \iint_{S_w} \left( 1 - \frac{U_x^2}{U_\infty} \right) d\sigma$$

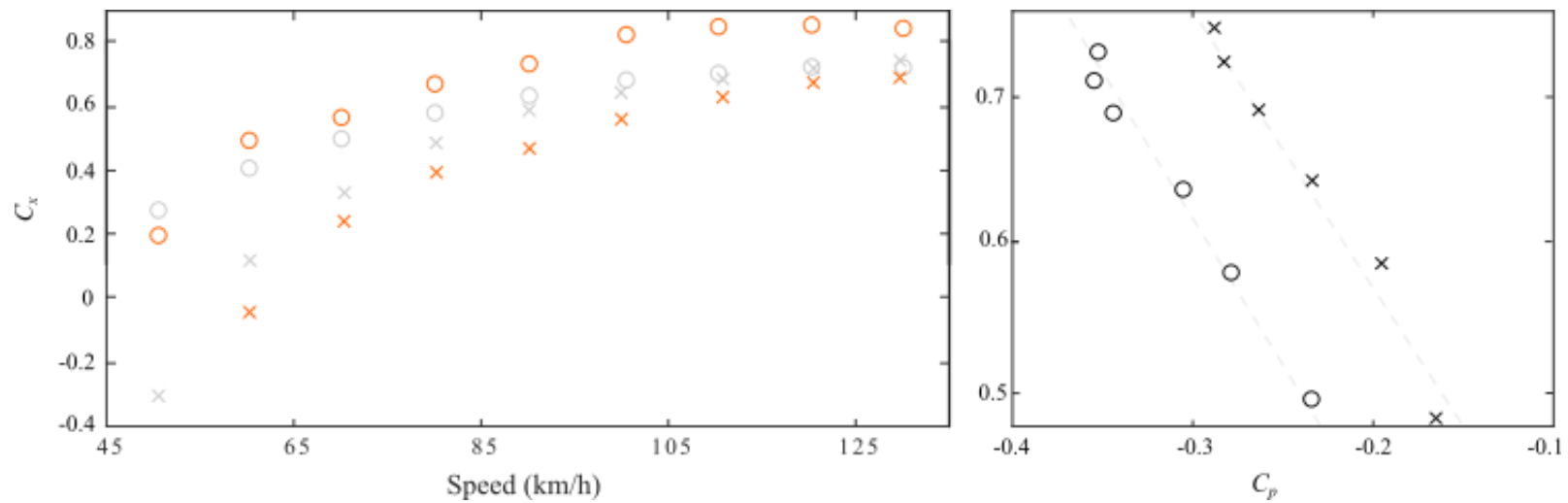
# Measurement mechanisms

Onorato's relation

$$F_D = \iint_{S_w} (P_t^{\infty} - P_t^{S_w}) d\sigma$$



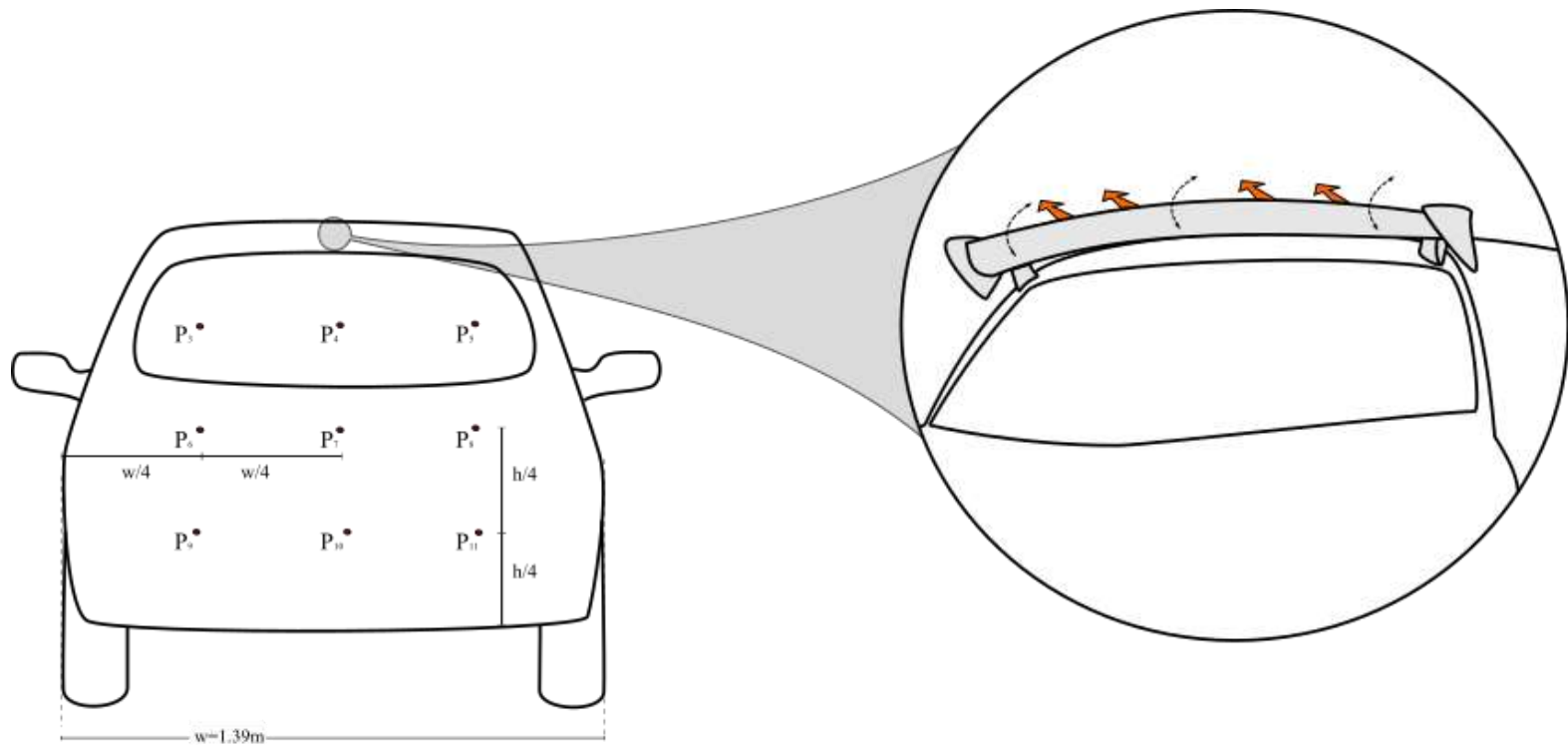
# Results



○ Direction I: departure to arrival

× Direction II: arrival to departure

# Future project – Flow control



# Flow Control

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  - Application to the airfoil
  - Application to the Ahmed body (MF and CC'PhDs)



- Machine Learning and model-free control: + 4h with [Thomas Gomez](#)



# References

## Journal:

**SISO model-based control of separated flows**, *Internat. Journal of Robust & Nonlinear Control*, 2017  
M. Feingésicht, A. Polyakov, F. Kerherve and J. P. Richard,

## Conferences:

**Nonlinear Control for Turbulent Flows**, *IFAC 2017 World Congress*, Toulouse, July 2017  
M. Feingésicht, A. Polyakov, F. Kerherve and J. P. Richard

**Model-Based Feedforward Optimal Control Applied to a Turbulent Separated Flow**, *IFAC 2017*  
M. Feingésicht, A. Polyakov, F. Kerherve and J. P. Richard

**A bilinear input-output model with state-dependent delay for separated flow ctrl**, *ECC 2016 Aalborg*  
M. Feingésicht, C. Raibaud, A. Polyakov, F. Kerherve and J. P. Richard

**Reducing Car Consumption by Means of a Closed-loop Drag Control**  
C. Chovet, M. Feingésicht et al., *VEHICULAR 2018, Venice*

## Patent:

**Dispositif de contrôle actif du recollement d'un écoulement sur un profil.**  
M. Feingésicht, A. Polyakov, F. Kerherve and J. P. Richard

## Book:

**Mathématiques pour l'ingénieur (chap.6: Systèmes à retard)** <https://hal.archives-ouvertes.fr/hal-00519555>  
J. P. Richard et al., 2009 (available online)

# What's next?



<https://youtu.be/V1BQaCjO7to>

Spotter



Twingo GT

*Dreams...*