

# Networked Control Systems :

*to buff, or not to buff? \**

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GREYC, Caen 27 novembre 2013

\*  *Systèmes Contrôlés en Réseau : s'en tamponner, ou pas ?*



## NCS: to *buff*, or not to buff?

Networks such as Internet or Wireless 802.11 present great advantages for flexible and low-cost networking. However, they are not as reliable as CANs, and integrating them in control applications, while preserving some performance, constitutes an interesting challenge.

Using delay models allows for catching many of the effects introduced by the presence of unreliable networks in the control loops. Several theoretical techniques allow for analyzing the resulting systems. Some of them need the delay to be constant, which can be obtained by using waiting strategies involving buffers. Some other tolerate fast varying delays.

Without entering into many technical details, we'll try to draw a panel of some techniques, in particular the ones we developed at LAGIS.

*It will be some story about network effects, sampling and lost packets, **time /event -driven** solutions, remote observers and bilateral teleoperation...*



synchrone / asynchrone

## Verbe

**buff** /bʌf/

1. Polir, poncer, meuler, buffler.
2. (*Jeux vidéo*) Rendre un personnage plus fort.

## Antonymes

Temps	Forme
Infinitif	to buff /bʌf/
Présent simple, 3 <sup>e</sup> pers. sing.	buffs /bʌfs/

## Nom commun

**buff** /bʌf/

1. Cuir brut obtenu de la peau du buffle ou d'un animal similaire.

Singulier	Pluriel
<b>buff</b> /bʌf/	buffs /bʌfs/

## Nom commun

**buffer** /bʌ.fə(ɹ)/

1. (*Transport*) Tampon, pare-chocs.
2. (*Chemin de fer*) (*Royaume-Uni*) Heurtoir (*train buffer stop*).
3. (*Informatique*) Mémoire tampon, tampon (*data buffer*).
  - **Buffer overrun** is a common cause of bugs.
4. (*Informatique*) Tampon d'affichage (*display buffer*).
5. (*Chimie*) Solution stabilisant le pH d'un liquide.

Singulier	Pluriel
<b>buffer</b> /bʌ.fə(ɹ)/	buffers /bʌ.fə(ɹ) z/

...tion à la couleur de la  
du chamois)

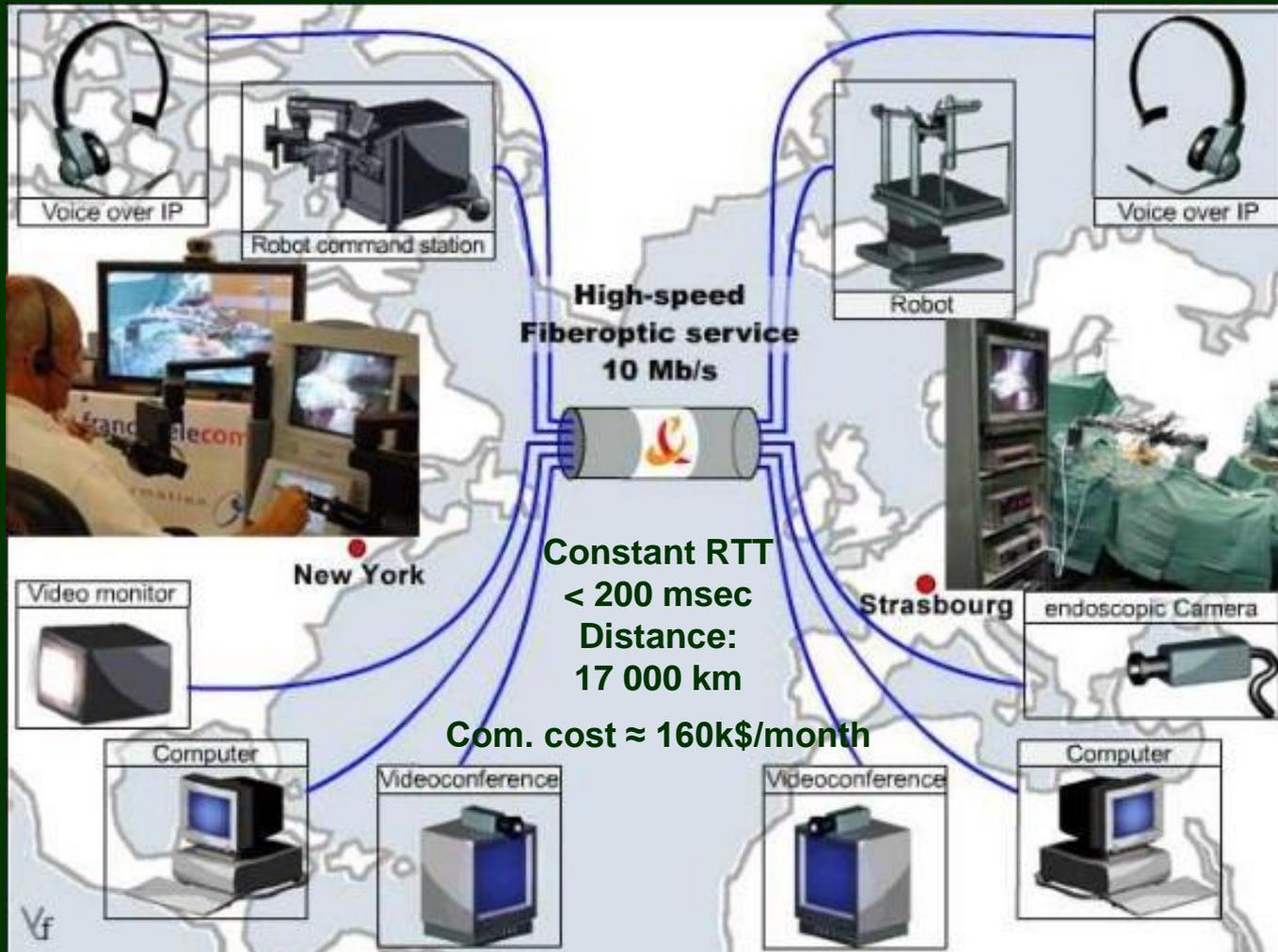
cuir, utilisé pour polir. Il est formé d'une sorte  
né (autrefois constituée par des disques de  
ne de laquelle on applique à chaud une colle

<http://fr.wiktionary.org/wiki/buff>

# Overview

- Motivation and examples
- Modelling
- Sampling and delay
- A crude example
- Control : *to buff, or not to buff?* A selection of results
- Conclusions

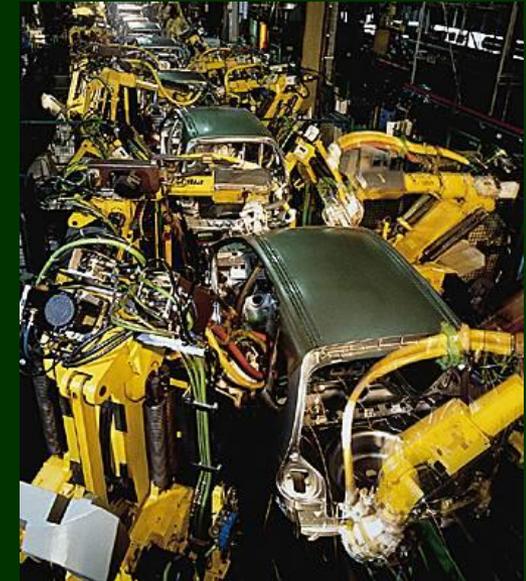
# Tele surgery: the Lindbergh operation, 07/09/2001



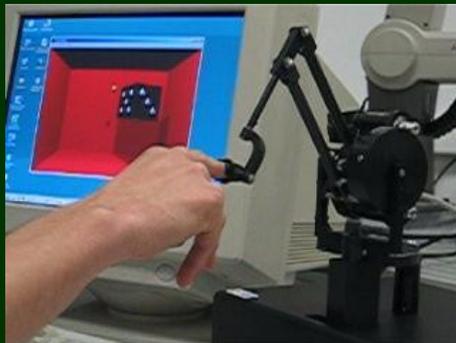
« The only restriction to the development of long-distance tele-surgery as to do, still today, with its cost. For tele-surgery, you must use a transcontinental ATM line, that you have to book during 6 months, at the price of about 1 million dollars. » [Prof. J. Marescaux, Le Monde, January 6, 2010](#)

# other examples...

Remote Monitoring



Avoiding electrical cabling



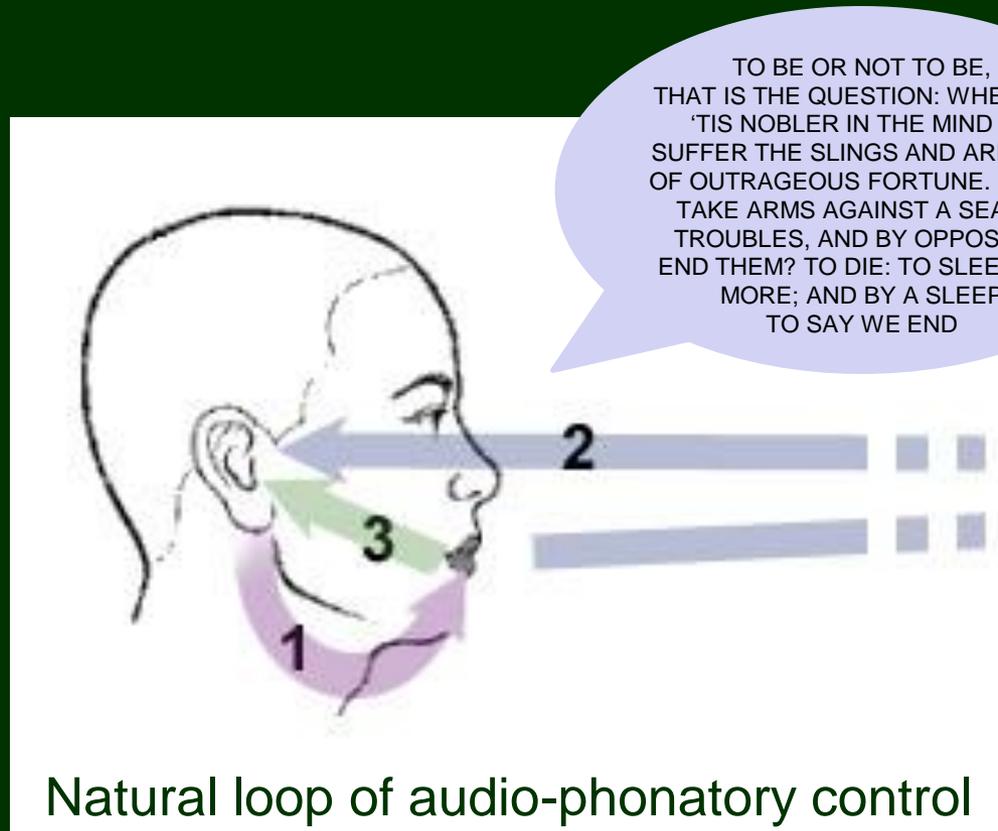
Bilateral Teleoperation

Robot collaboration



Movies: see <http://chercheurs.lille.inria.fr/~jrichard/manips.htm>

and an example from everyday life...



and an example from everyday life...



# Some surveys...

- Control methodologies in Networked Control Systems  
Y. Tipsuwan, M.Y. Chow, *Control Eng. Practice* 11, 1099-111, **2003**
- Networked Control System: a brief survey  
T.C. Yang, *IEE Proc. Control Theory Appl.*, 153 (4), **2006**
- Control over Wireless Networks  
K.H. Johansson, *25th Benelux Meeting on S&C, The Netherland*, **2006**
- A survey of recent results in Networked Control Systems  
J.P. Hespanha, P. Naghshtabrizi, Y. Xu, *Proc. of the IEEE*, 95 (1), **2007**
- Trends in Networked Control Systems  
S. Zampieri, *17th IFAC World Congress, Seoul*, **2008**
- A switched system approach to exponential stabilization through com. network  
A.Kruszewski, WJ.Jiang, E.Fridman, J.P.Richard, A.Toguyeni, *IEEE CST*, 20 (4) **2012**



nice (wrt 2007)



not that bad, too

SYSTEMES  
AUTOMATISÉS

Information - Commande - Communication

## Systemes commandés en réseau

*sous la direction de*  
Jean-Pierre Richard  
Thierry Divoux

2007

*hermes*

*Lavoisier*

C. Canudas de Wit, T. Divoux, P. Fraisse, D. Georges, J.P. Georges,  
G. Juanole, A. Lelevé, F. Lepage, F. Michaut, G. Mouney, W. Perruquetti,  
J.P. Richard, E. Rondeau, O. Sename, A. Seuret, E. Wittrant.

not forgetting...

# Overview

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- **Modelling**
- Sampling and delay
- A very basic example
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- Conclusions

# Single-loop NCS

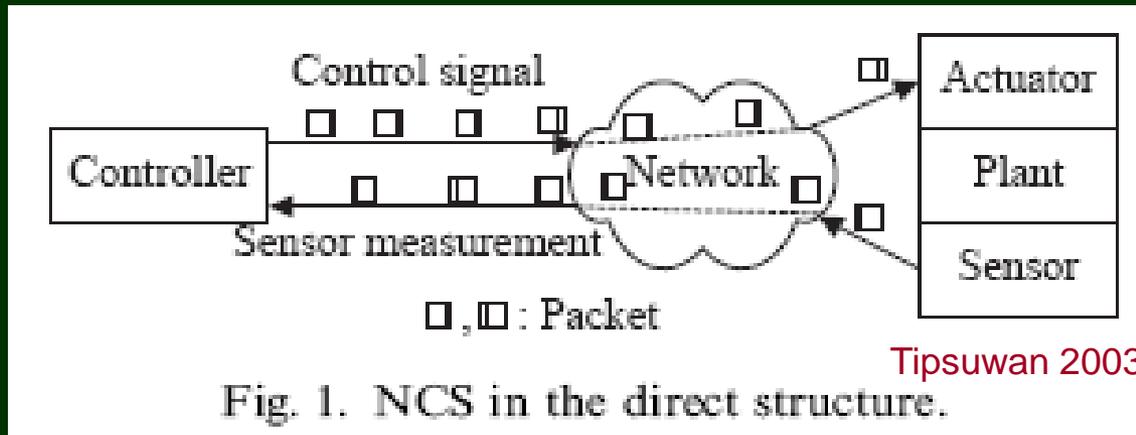


Fig. 1. NCS in the direct structure.

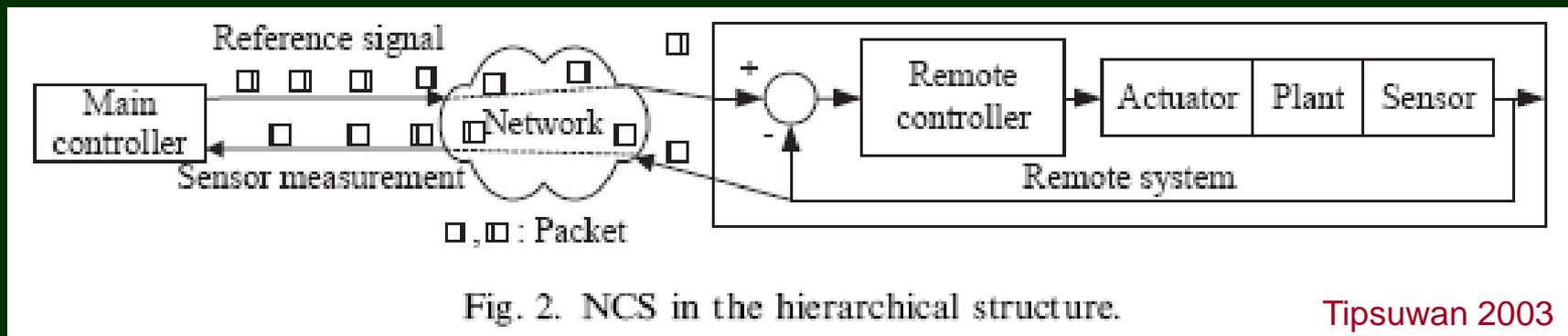


Fig. 2. NCS in the hierarchical structure.

Tipsuwan 2003

What about multi-loop?

# Multiple-loop NCS according to [Yang 2006]:

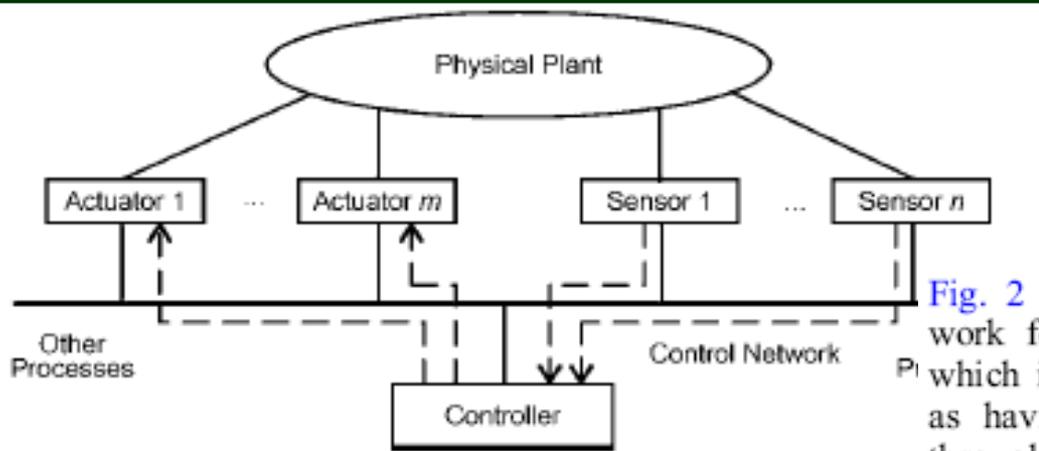
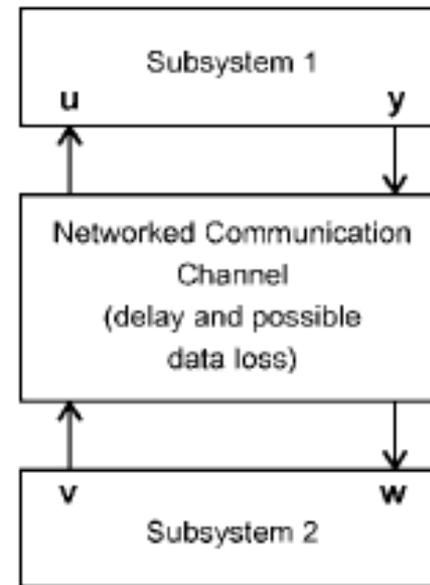
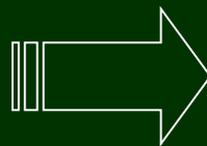


Fig. 1 Typical NCS setup and information flows

Yang 2006

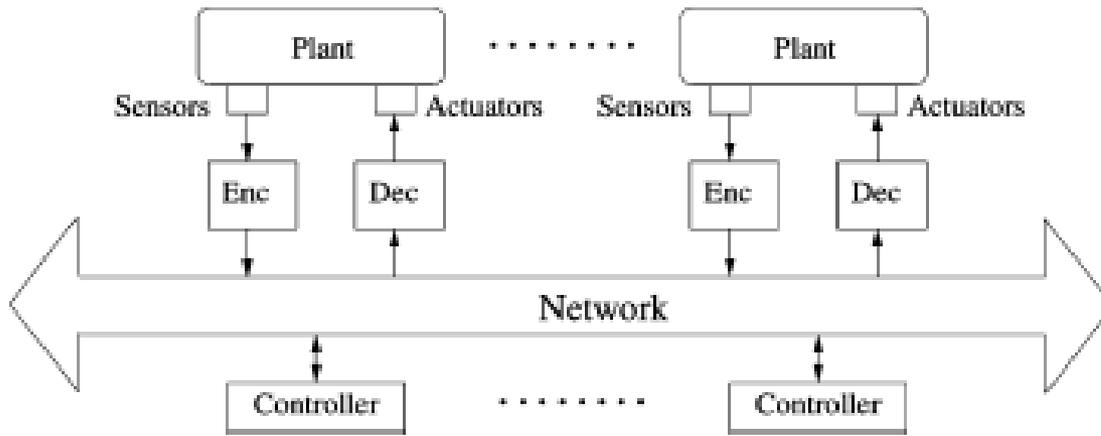
Fig. 2 is a block diagram, representing a general framework for the study of networks and control. An NCS, which is the main topic of this paper, can be considered as having **two subsystems** interacting with each other through networked communication channels. Here, it is



Yang 2006

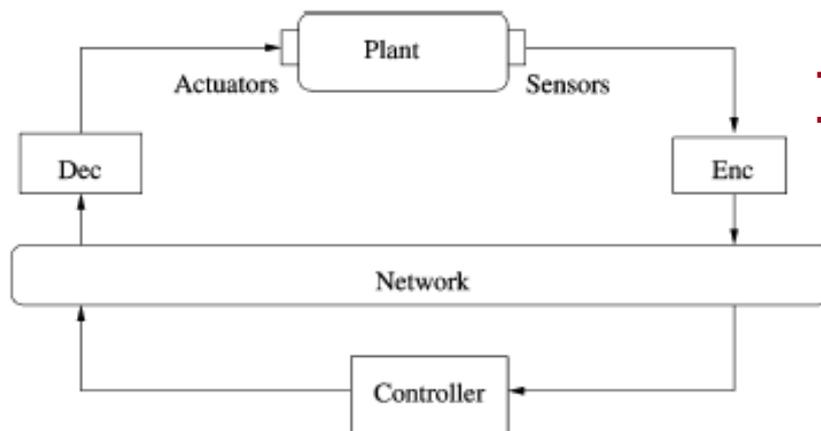
Fig. 2 General framework for networks and control

# Multiple-loop NCS according to [Hespanha 2007]:



**Fig. 1.** General NCS architecture.

Hespanha 2007



**Fig. 2.** Single-loop NCS.

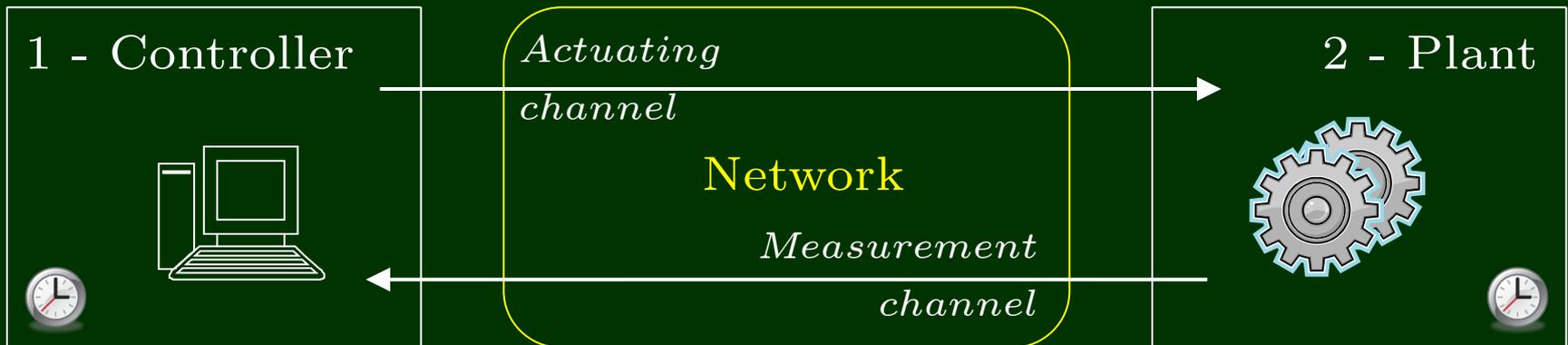
Hespanha 2007

It is also often common to consider a single feedback loop as in Fig. 2. Although considerably simpler than the system shown in Fig. 1, this architecture still captures many important characteristics of NCSs such as bandwidth limitations, variable communication delays, and packet dropouts.

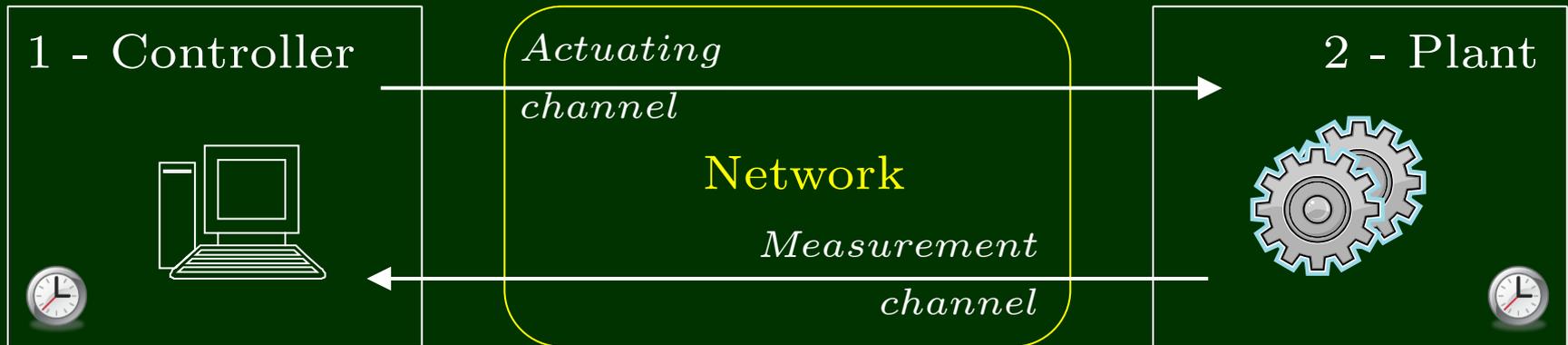
# Single-loop NCS.

... the talk will be limited to this case, too.

A good starting point for understanding  
the issues linked to the presence  
of networks in the loops



# Single-loop NCS



## Types of networks:

- ✓ dedicated (ControlNet, DeviceNet) : frequent transmission of small packets → guaranteed time but €
- ✓ Ethernet, wifi : rare transmission of bigger packets → no guarantee for delay but €

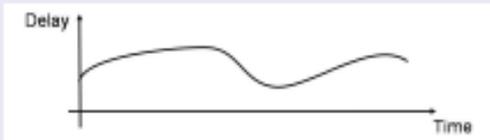
# Effects of the network on the closed-loop control

<i>Issue</i>	<i>Translation in control terms</i>	<i>Concerned</i>	<i>Not concerned</i>
<b>limited bandwidth</b>	quantification, limited quantity of info per second (Shannon, <i>maximum bit rate</i> )	limited energy resource systems (UAVs, WSN, $\mu$ -sensors or $\mu$ -actuators, aerosp...)	packet-transmiss. type Inter/Ethernet, Bluetooth... 1 bit or 300 $\rightarrow$ <i>idem</i> ATM=384, Ethernet>368, Bluetooth>499
<b>sampling, coding, scheduling, transmission, asynchronism</b>	variable delays, estimated if there is a model, or time-stamps	packet transmission systems	dedicated and unshared netw. (ControlNet, DeviceNet)
<b>packet losses</b>	asynchronous sampling, variable delay	wireless, UDP-like protocols	TCP-like protocols (but generally useless: time wasting for outdated info)
<b>out-of-sync clocks</b>	delays (at least)	internet	control-dedicated netw. (CAN bus...)

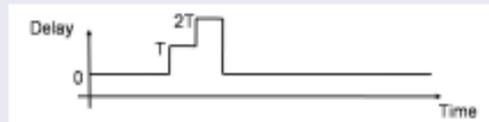
today

In such a framework, we have the equation:

*communication + packet loss + sampling = 1 delay*



Communication delay :  $\tau_i^c(t)$

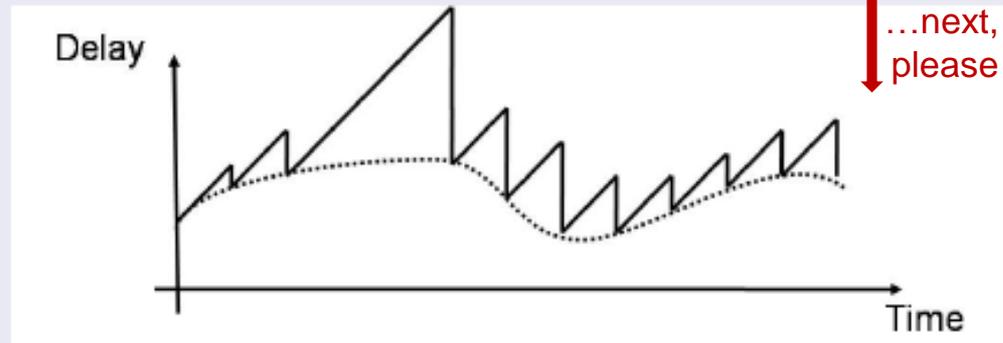


Delay from packet loss :  $nT$



Sampling delay :  $\tau_i^s(t)$

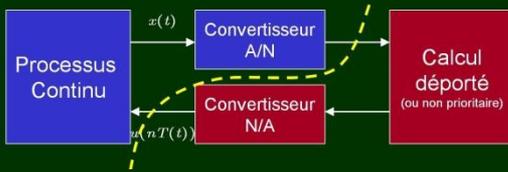
Total time-delay of NCS :  
 $\delta_{con}(t)$  and  $\delta_{obs}(t)$



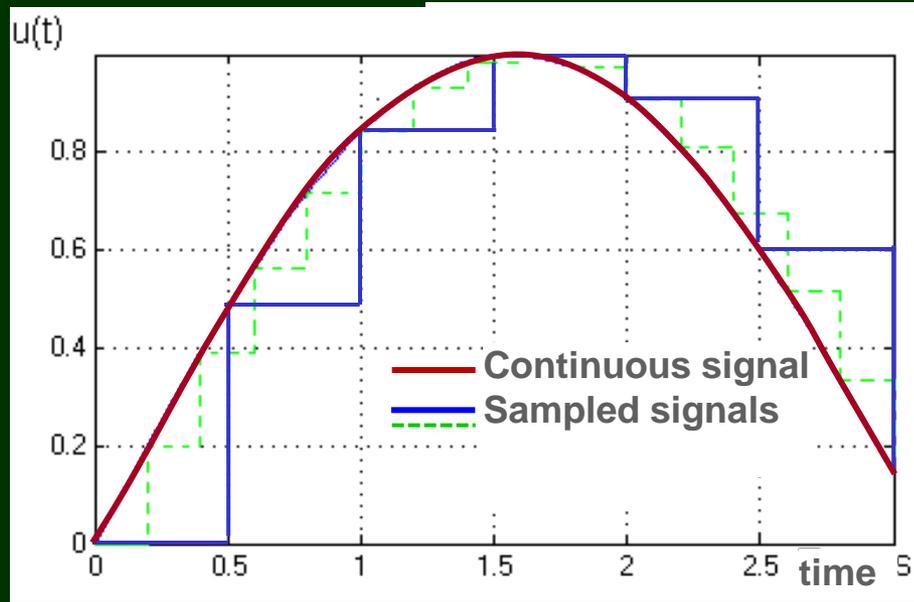
...next,  
please

# Overview

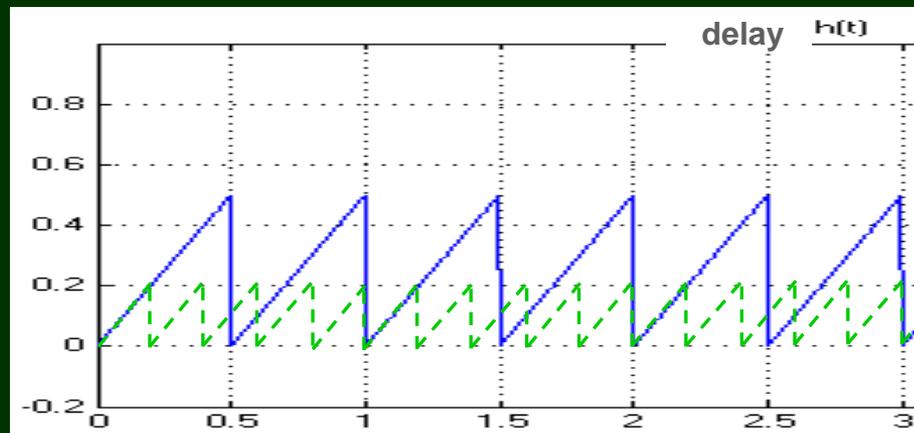
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- Modelling
- **Sampling and delay**
- A very basic example
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Fridman, Seuret, Richard - *Automatica* 2004

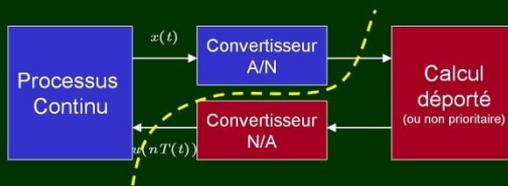


Sampled and hold signal  
(depicted for a constant period)

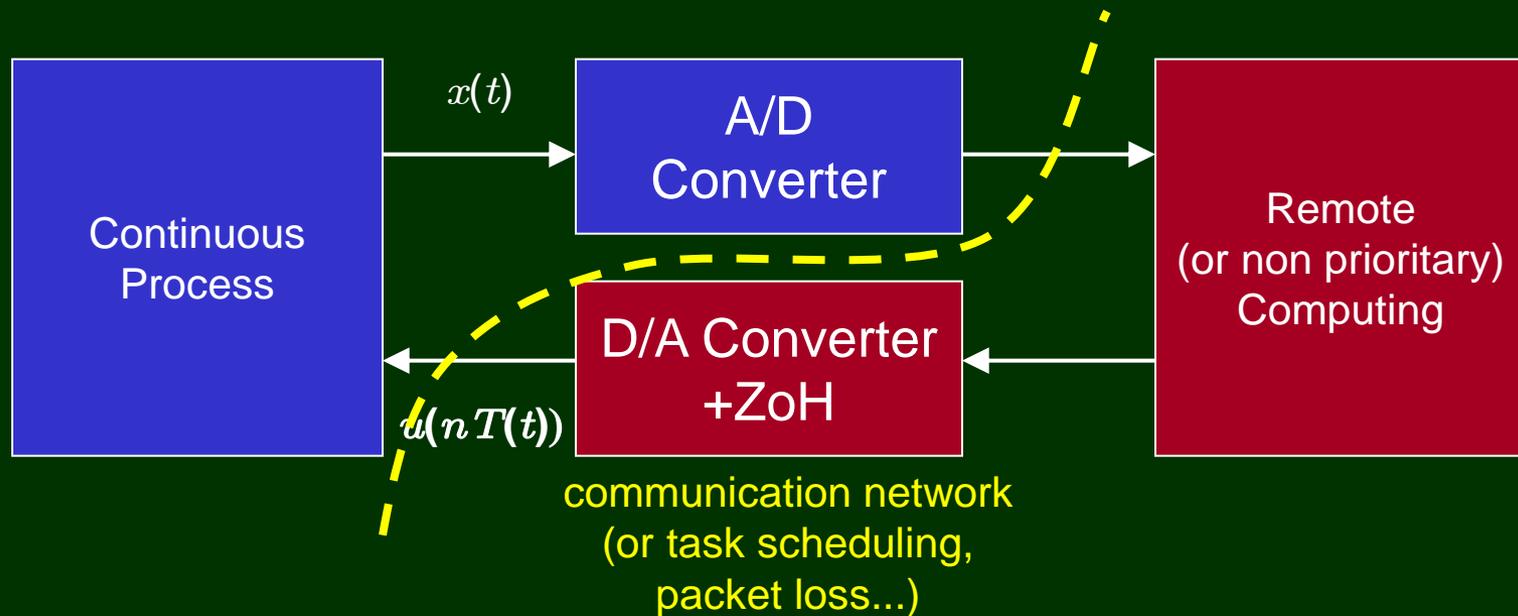


Delayed signal  
with variable  $h(t)$

$$u(t) = u_d(t_k) = u_d(t - [t - t_k]) = u(t - h(t))$$

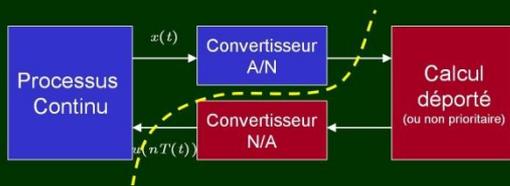


## A periodic sampling

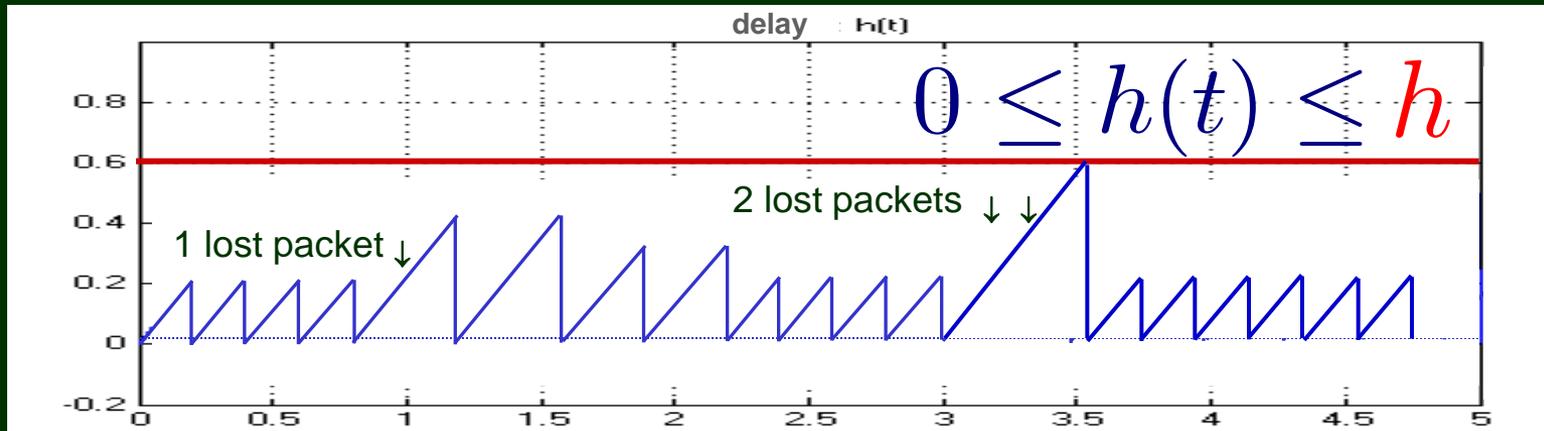


Integration,  $z$ -transform, everything's ok, etc.

$$u(t) = u_d(t_k) = g(x(t_k)), \quad t_k \neq kT$$



Another statement of the same problem...



- influence of the *maximum* sampling period  $h$

- application of Fridman's criterion

$$\dot{h}(t) \leq 1$$

See also refined results in:

“A refined input delay approach to sampled-data control”. E. FRIDMAN, Automatica 2010

“A novel stability analysis of linear systems under asynchronous sampl”. A. SEURET, Automatica 2011

“SOS for sampled-data systems” A. SEURET, M. PEETS, IFAC'11, Milano, Italy, 2011

## Note : approaching aperiodic sampling via *switched systems*

PhD L. Hetel 2007 + IEEE TAC 2006 (Daafouz, lung)

intra-sampling: Taylor trunc. of the exponential terms (cont. delay)  $\rightarrow$  *polytopes, LMI*

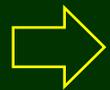
nb of packet losses  $\rightarrow$  discrete delay

augmented model  $\rightarrow$  *switched system* (event-based model)

$$\begin{aligned}
 x(k+1) &= A(k)x(k) + B(k)u(k) \\
 A(k) &= e^{M(t_{k+1}-t_k)}, \quad B(k) = \int_0^{t_{k+1}-t_k} e^{M(t_{k+1}-t_k-s)} ds N.
 \end{aligned}
 \left| \begin{aligned}
 \eta_{i+1} &= A(\rho_i)\eta_i + B(\rho_i)u_i. \\
 A(\rho_i) &= e^{M\rho_i}, \quad B(\rho_i) = \int_0^{\rho_i} e^{Ms} ds N. \\
 u_c(t_i) &= Kx_c(t_j) = Kx_c(t_i - \theta_i), \\
 \theta_i &\in \mathcal{T} = \{\theta \in \mathbb{Z}^+ : \underline{\theta} \leq \theta \leq \bar{\theta}\}
 \end{aligned}
 \right.$$

$$\begin{aligned}
 z_i = \begin{bmatrix} \eta_i^T & \eta_{i-1}^T & \cdots & \eta_{i-\bar{\theta}}^T \end{bmatrix}^T & \xrightarrow{\quad} \bar{A}(\rho_i) = \begin{bmatrix} A(\rho_i) & \mathbf{0} & \cdots & \cdots & \mathbf{0} \\ \mathbf{I} & \mathbf{0} & \cdots & \cdots & \mathbf{0} \\ \mathbf{0} & \mathbf{I} & \mathbf{0} & \cdots & \mathbf{0} \\ \vdots & & & & \vdots \\ \mathbf{0} & \cdots & \mathbf{0} & \mathbf{I} & \mathbf{0} \end{bmatrix}, \quad \bar{B}(\rho_i) = \begin{bmatrix} B(\rho_i) \\ \mathbf{0} \\ \mathbf{0} \\ \vdots \\ \mathbf{0} \end{bmatrix}
 \end{aligned}
 \left| \begin{aligned}
 u_i &= \bar{K}_{(\theta_i)} z_i, \\
 \bar{K}_{(\theta_i)} &= [\mathbf{0} \quad \cdots \quad \mathbf{0} \quad K \quad \mathbf{0} \quad \cdots \quad \mathbf{0}] \\
 \boxed{z_{i+1} &= (\bar{A}(\rho_i) + \bar{B}(\rho_i)\bar{K}_{(\theta_i)}) z_i}
 \end{aligned}
 \right.$$

## Note : approaching aperiodic sampling via *switched systems*



**Unification of both approaches input delay / switched :**

"Discrete and intersample analysis of systems with aperiodic sampling"

L. HETEL, A. KRUSZEWSKI, W. PERRUQUETTI, J.P. RICHARD

IEEE TAC 56 (7), p.1696 - 1701, 2011

$$\dot{x}(t) = A_c x(t) + B_c K x(t_k), \quad \forall t \in [t_k, t_{k+1}]$$

$$x(t) = \Lambda(t - t_k) x(t_k)$$

$$\Lambda(\theta) := I + \int_0^\theta e^{sA_c} ds (A_c + B_c K)$$

$$\mathcal{H}(x) = \{y : y = \Lambda(\theta)x, \theta \in \mathcal{T}\}$$



$$x(t_{k+1}) \in \mathcal{H}(x(t_k))$$

*difference inclusion*

$x = 0$  *asympt. stable*



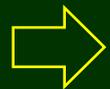
**constructive**

$\exists$  *quasi-quadratic Lyapunov function*

$$V(x) = x^T \mathcal{L}_{[x]} x, \quad \mathcal{L}_{[\cdot]} : \mathbb{R}^n \rightarrow \mathbb{R}^{n \times n},$$

$$\mathcal{L}_{[x]} = \mathcal{L}_{[ax]}^T = \mathcal{L}_{[ax]}, \quad \forall x \neq 0, a \neq 0$$

# Note : State-Dependent Sampling



**Next sampling instant depends on state  $x_k$**

"A state-dependent sampling for linear state feedback"

C. FITER, L. HETEL, W. PERRUQUETTI, J.P. RICHARD

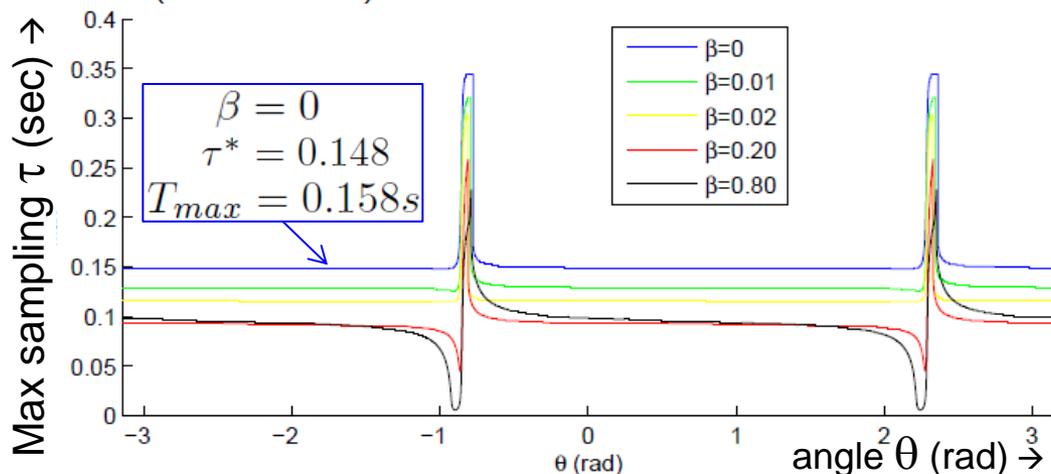
Automatica 48 (8), p.1860-1867, 2012

- Self-triggering
- Complexity is off-line
- LRF technique

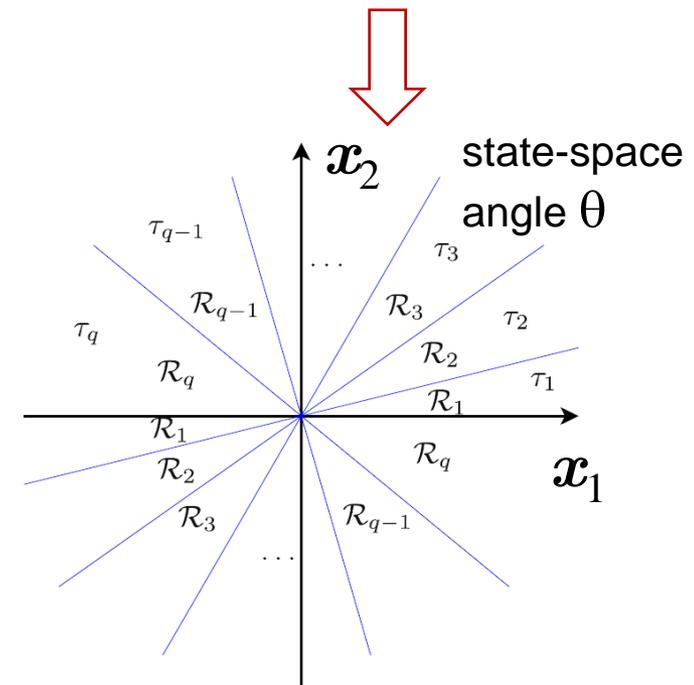
$$\dot{x}(t) = A_c x(t) + B_c K x(t_k), \quad \forall t \in [t_k, t_{k+1}]$$

$$\dot{x}(t) = \begin{pmatrix} 1 & 15 \\ -15 & 1 \end{pmatrix} x(t) - \begin{pmatrix} 1 \\ 1 \end{pmatrix} K x(t_k),$$

$$K = \begin{pmatrix} -5.33 & 9.33 \end{pmatrix}.$$



$$t_{k+1} = t_k + \tau(x(t_k))$$



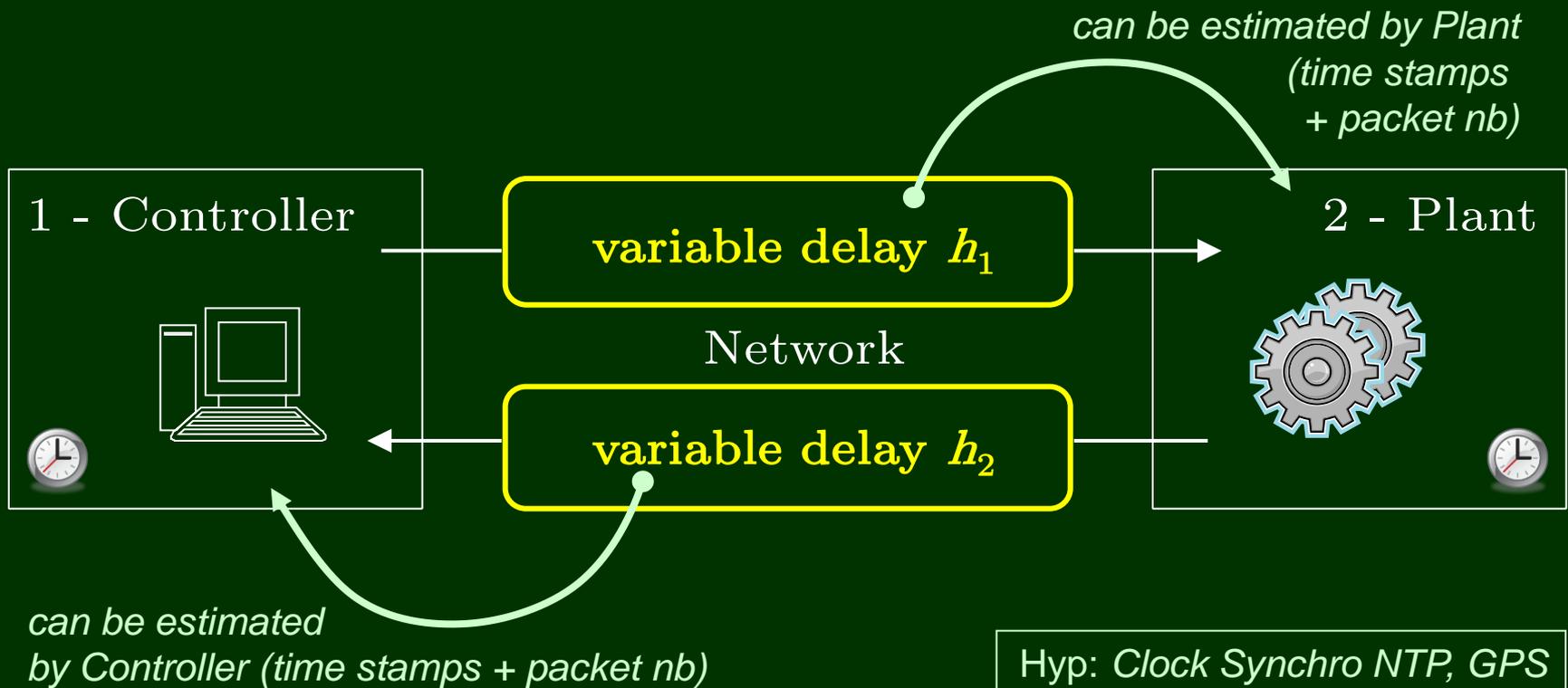
Max next sampling computed off-line ( $\beta$ -stab.)  $\rightarrow$  less often than with periodic sampling

*... let's sum up until now:*

transmission time + access time + packet loss + sampling...

**= 2 variable delays**

known / unknown ?

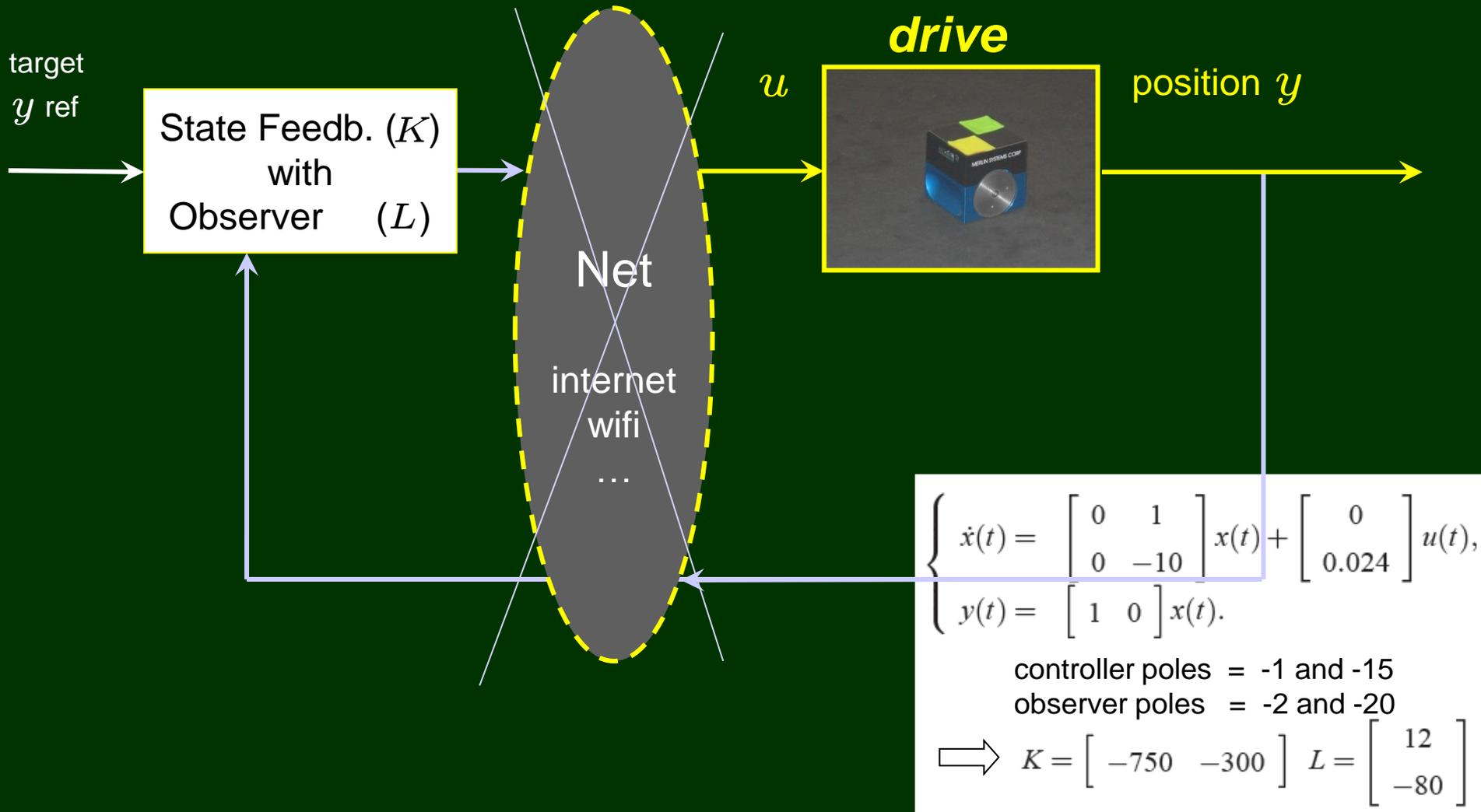


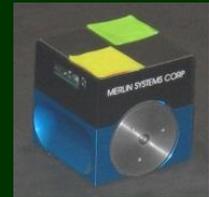
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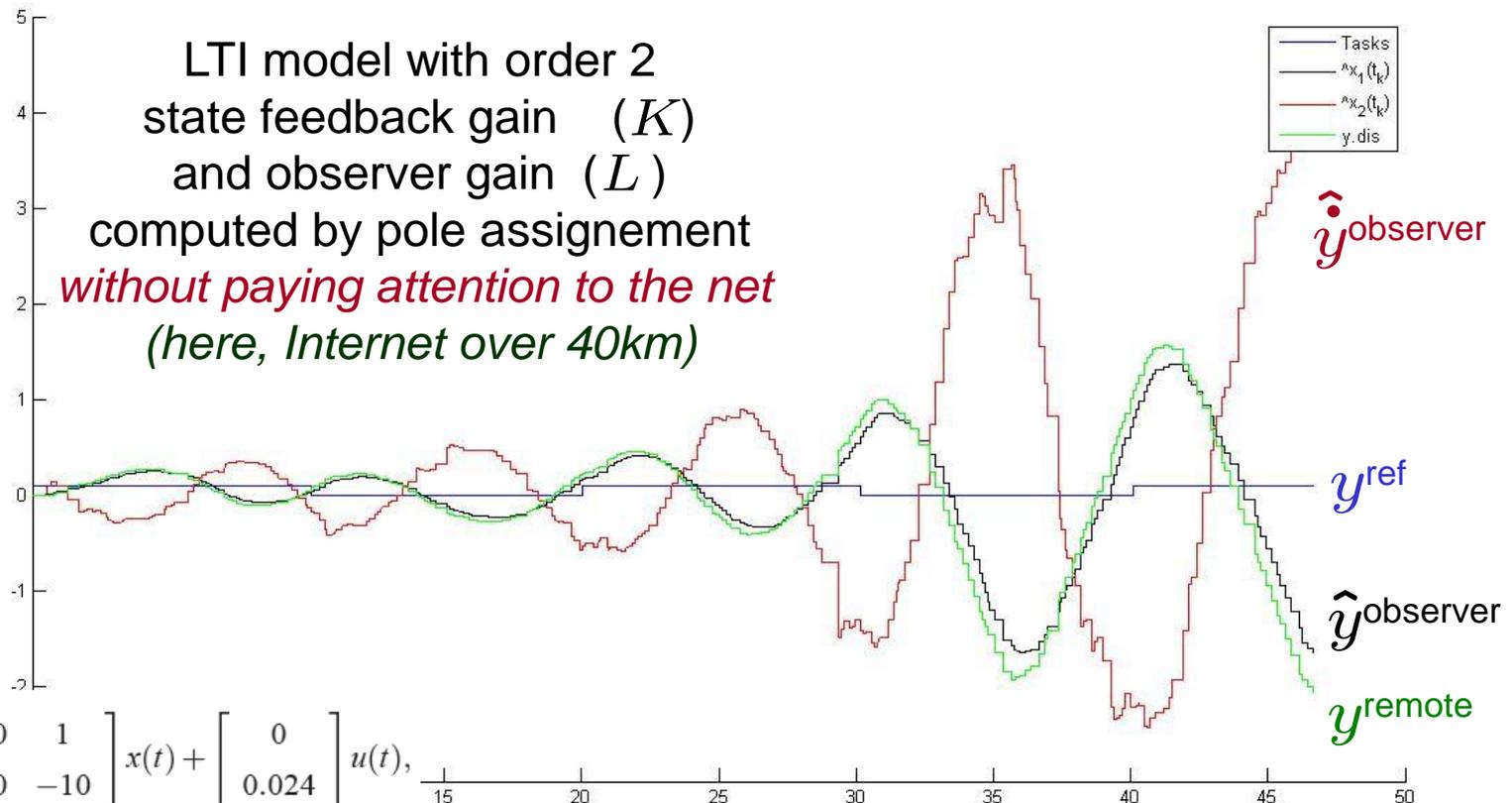
## A crude example

### Theory (when neglecting the network effect)





# Experimental results (with network)



$$\begin{cases} \dot{x}(t) = \begin{bmatrix} 0 & 1 \\ 0 & -10 \end{bmatrix} x(t) + \begin{bmatrix} 0 \\ 0.024 \end{bmatrix} u(t), \\ y(t) = \begin{bmatrix} 1 & 0 \end{bmatrix} x(t). \end{cases}$$

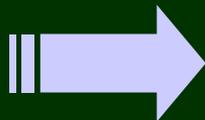
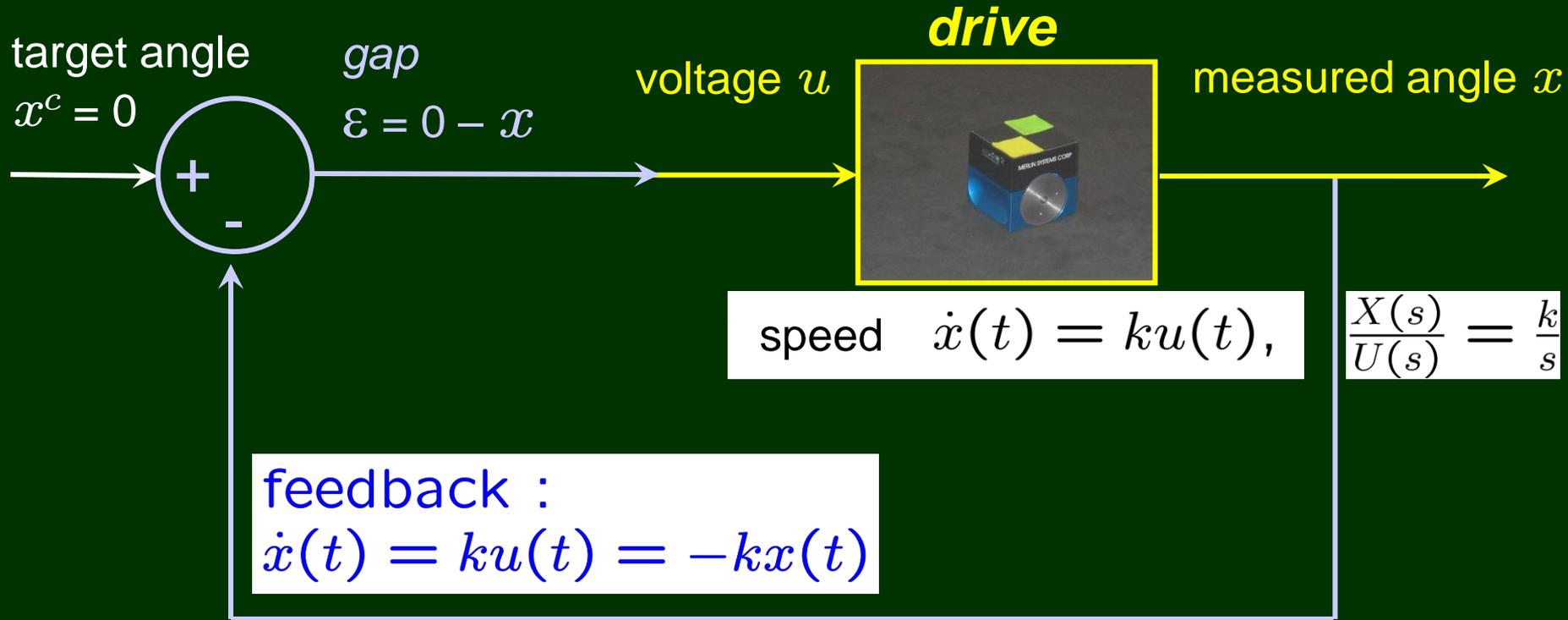
Controller poles = -1 and -15

Observer poles = -2 and -20

$$\Rightarrow K = \begin{bmatrix} -750 & -300 \end{bmatrix} \quad L = \begin{bmatrix} 12 \\ -80 \end{bmatrix}$$

# A crude example

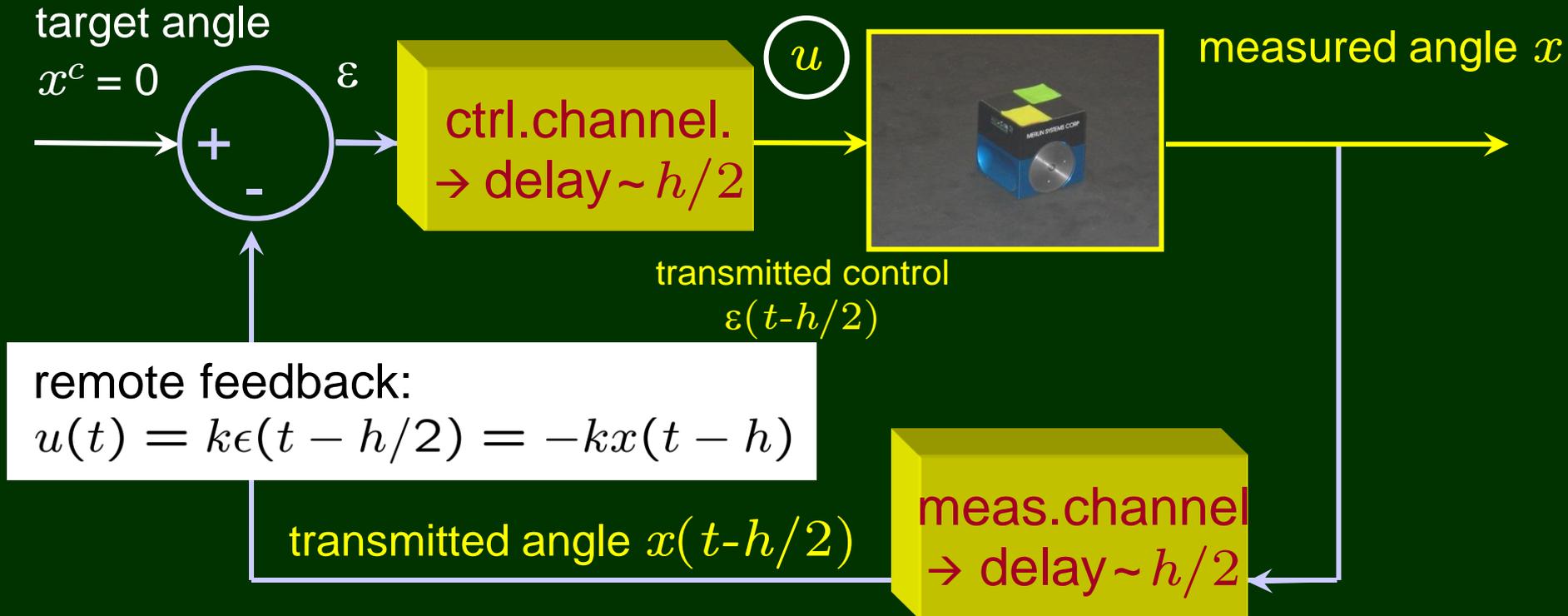
## Interpretation on a simplified model



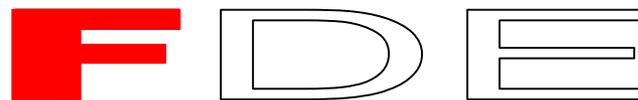
$$\dot{x}(t) + kx(t) = 0$$



# A crude example



$\dot{x}(t) + kx(t - h) = 0$



## A crude example

*Exercise ... for my students, don't worry ;-)*

$$\dot{x}(t) + x(t - h) = 0$$

$$(\text{cas } h = 1, k = 1)$$

$$\dot{x}(t) = -x(t - 1)$$

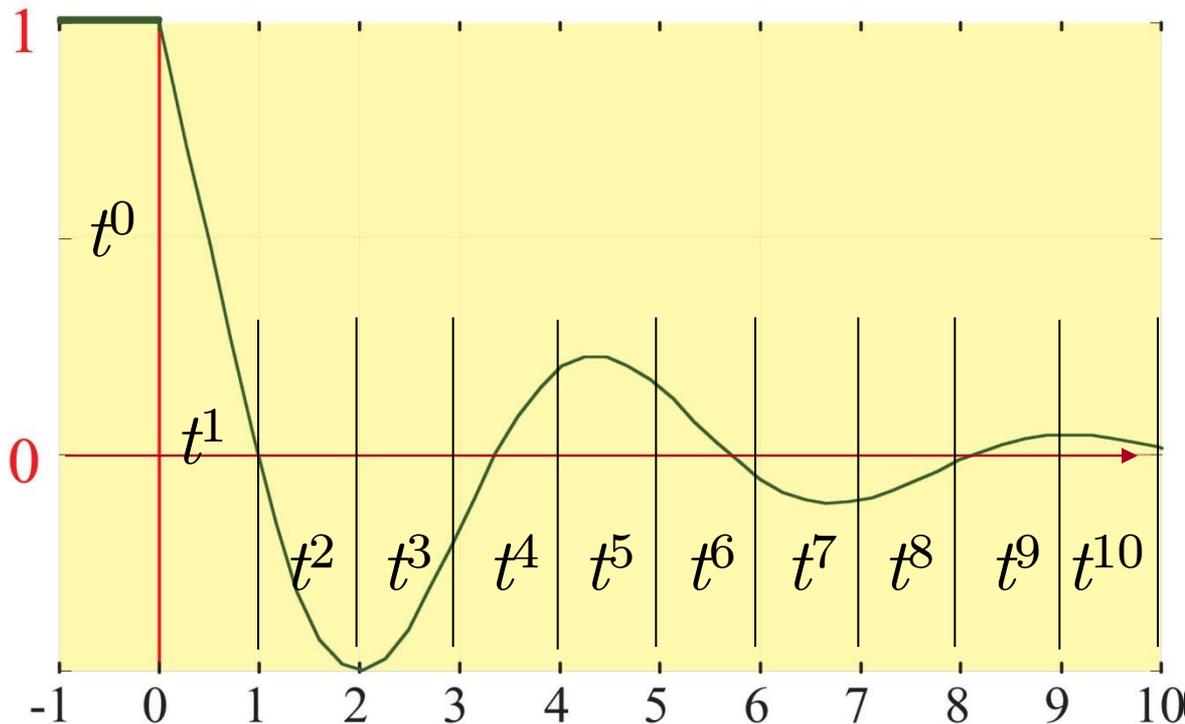
C.I.  $t = 0 : x(t = 0) = 1$  ??

$t \in [-1, 0] : x(t) = 1$  (C.I.)

$t \in [0, 1] : x(t) = 1 - t,$

$t \in [1, 2] : x(t) = \frac{1}{2} - t + \frac{t^2}{2},$

*etc.*



# A crude example

$$\dot{x}(t) + x(t - h) = 0$$

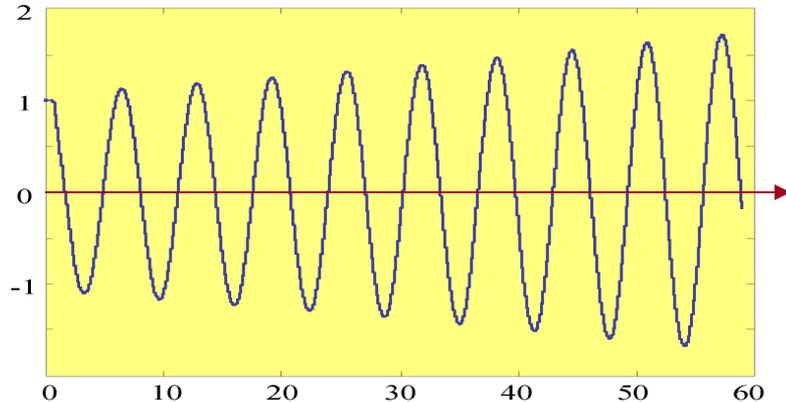
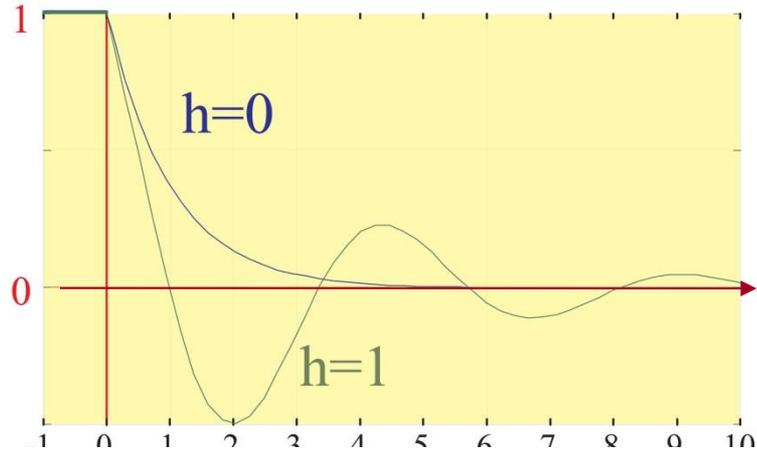
w.r.t.  $h$  ?

$$\dot{x}(t) + x(t) = 0$$

$$\dot{x}(t) + x(t - 1) = 0$$

$$\dot{x}(t) + x(t - \frac{\pi}{2}) = 0 ?$$

$$\dot{x}(t) + x(t - 1.6) = 0$$

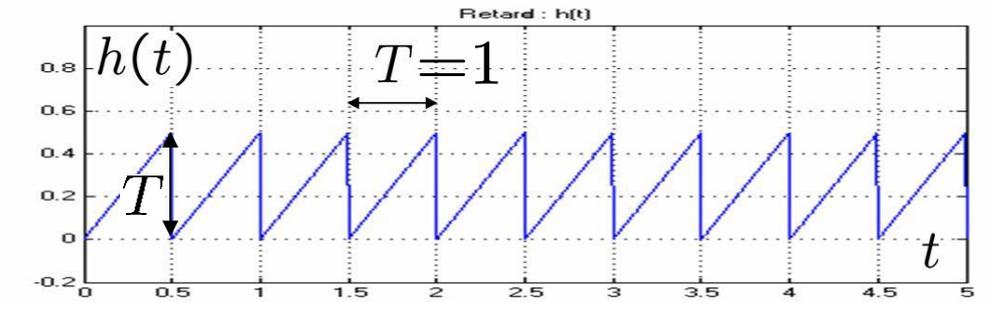


## A crude example

... and mind the variable delays!

$$\dot{x}(t) = -ax(t) - bx(t - h(t)) \quad (1)$$

$$h(t) = t - kT \quad \text{for } kT < t \leq (k+1)T$$

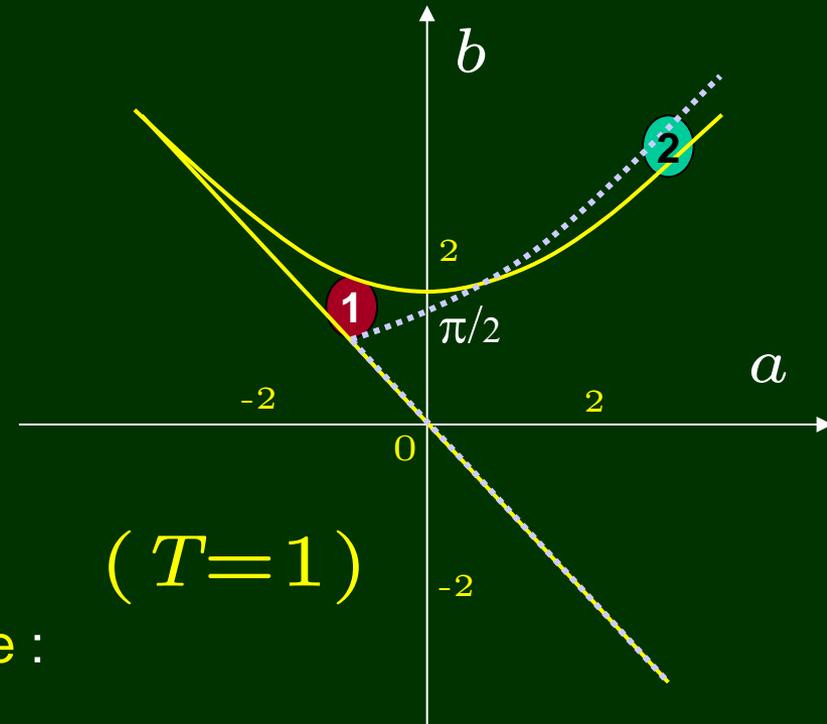


**variable** : asymptot. stable iff  $\in$  **yellow zone** :

$$\left| \left(1 + \frac{b}{a}\right)e^{-aT} - \frac{b}{a} \right| < 1 \quad \text{if } a \neq 0$$

$$|1 - bT| < 1 \quad \text{if } a = 0$$

constant :  $\forall h \in [0,1]$  iff  $\in$  **grey zone**



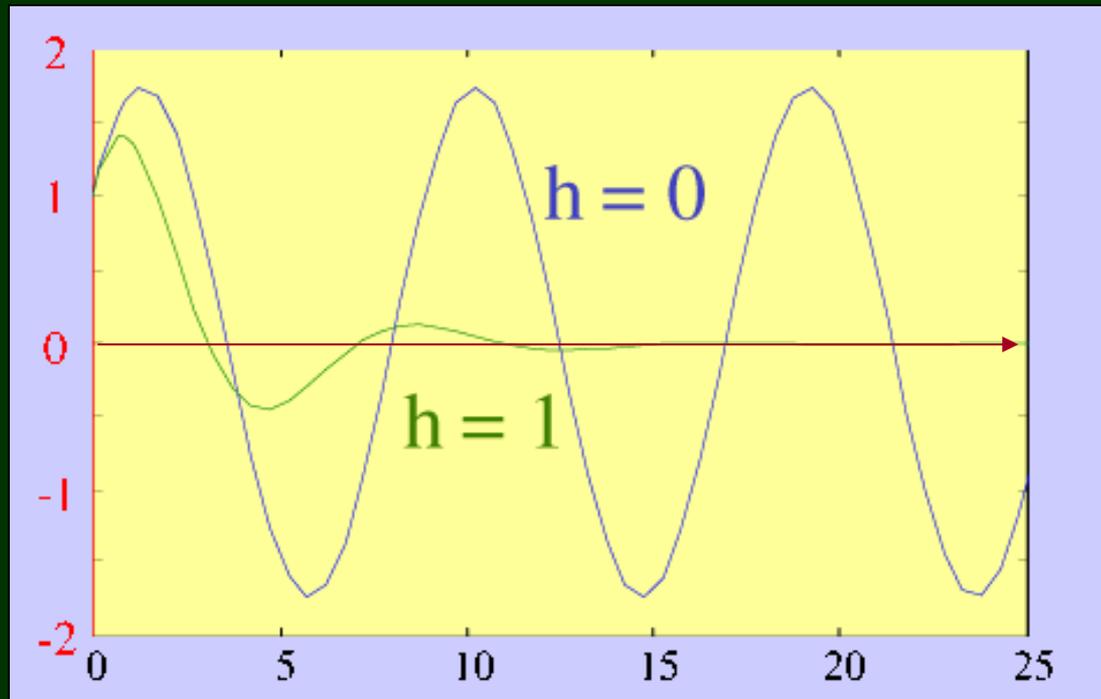
( T=1 )

- 1 stable  $h(t) < 1$  - unstable  $h = \text{cte} < 1$
- 2 unstable  $h(t) < 1$  - stable  $h = \text{cte} < 1$

*A crude example*

(digression...)

$$\ddot{y}(t) + y(t) - \frac{1}{2}y(t - h) = 0$$



*A known delay may also have a stabilizing effect*

Here, derivative effect:  $y(t - h) \approx y(t) - h\dot{y}(t)$

# Few words about Lyapunov method for TDS

**ODE :**

$$\dot{x}(t) = -ax(t)$$



$$V(x(t)) = x^2(t) > 0$$

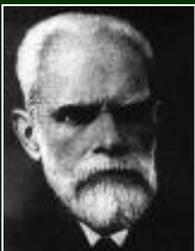
$$\dot{V}(x(t)) = -2 ax^2(t) < 0 \dots \text{etc.}$$

**FDE :**

$$\dot{x}(t) = -ax(t) - bx(t-h)$$

$$V(x(t)) = x^2(t) \quad (\text{« usual » quadratic})$$

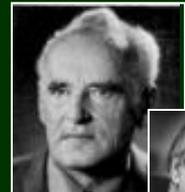
$$\dot{V}(x(t)) = -2 [ax^2(t) + \overset{\text{cross terms}}{bx(t)x(t-h)}] \leq \dots ?$$



→ need of specific adaptations:

1) *functions* of Lyapunov-Razumikhin (not here)

2) *functionals* of Lyapunov-Krasovskii



# Illustration of the LKF approach

(Lyapunov-Krasovskii functionals)

$$\dot{x}(t) = -ax(t) - bx(t-h)$$

$$V(x_t) = x^2(t) + |b| \int_{-h}^0 x^2(t+s) ds \quad (\text{quad} + \text{integral})$$

$$\begin{aligned} \dot{V}(x_t) &= -2x(t)[ax(t) + bx(t-h)] \\ &\quad + |b| \underline{[x^2(t) - x^2(t-h)]} \\ &\leq -2(a - |b|)x^2(t) \quad \dots \quad \dot{V}(x_t) < 0 \text{ if } |b| < a \end{aligned}$$

Remarks on the conservatism:

1) here, a « pessimistic » condition since it is i.o.d. - independent of the delay  $h$  ...

2) linked with the majoration of the crossed terms, here :  $-[x(t) + x(t-h)]^2 \leq 0$   
 $\Rightarrow -2bx(t)x(t-h) \leq bx^2(t) + bx^2(t-h)$

## More general...

## The system model

$$\dot{x}(t) = Ax(t) + A_1x(t - \tau(t)), \quad (2)$$

with the initial condition :

$x$  vector + variable delay

$$x(t_0 + \theta) = \phi(\theta), \quad \dot{x}(t_0 + \theta) = \dot{\phi}(\theta), \quad \theta \in [-h_2, 0], \quad (3)$$

where  $\tau(t) \in [h_1, h_2]$ ,  $h_1 \geq 0$ .

## Lyapunov functionals

$$\begin{aligned} V(t, x_t, \dot{x}_t) = & x^T(t)Px(t) + \int_{t-h_1}^t x^T(s)Sx(s)ds \\ & + h_1 \int_{-h_1}^0 \int_{t+\theta}^t \dot{x}^T(s)R\dot{x}(s)dsd\theta \\ & + \int_{t-h_2}^t x^T(s)S_a x(s)ds + (h_2 - h_1) \int_{-h_2}^{-h_1} \int_{t+\theta}^t \dot{x}^T(s)R_a \dot{x}(s)dsd\theta \end{aligned} \quad (4)$$

where  $P > 0$  and  $R, R_a, S, S_a \geq 0$ .

# Overview

- Motivations and examples
- Modelling
- Sampling and delay
- A very basic example
- **Control : *to buff, or not to buff?* A selection of results**
- Conclusions

# to buff, or not buff?

## 1<sup>st</sup> solution = act « as if » constant

- ✓ [Niemeyer & Slotine 98][Huang & Lewis 03][Azorin et al. 03][Fattouh & Sename 03] etc.

## 2<sup>nd</sup> solution = force the delay to constant

- therefore, maximize it :  $0 \leq h_i(t) \leq h_{max} \Leftrightarrow h_i(t) = h_{max}$
- thanks to a *buffer* → *time-driven*
- then, apply classical techniques:
  - ✓ prediction (Smith) [Lelevé & Fraise 01]
  - ✓ error eqn. obeying a retarded model [Estrada, Marquez, Moog 07]
  - ✓ etc.

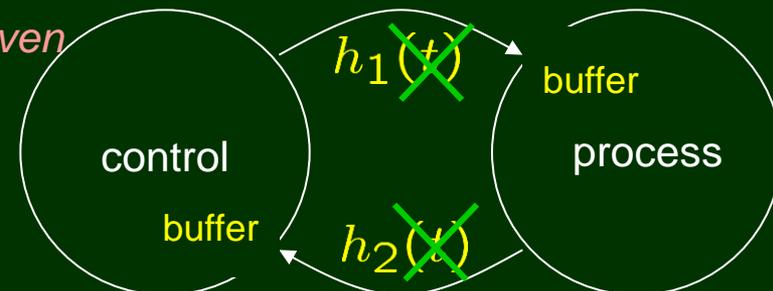
## 3<sup>rd</sup> solution (intermed.) only one buffer

[Seuret 06]  
[Jiang et.al 08]

## 4<sup>th</sup> solution = keep the variable delay...

- ✓ [Witrant et al. 07] [Seuret&Richard 08] → *event-driven*  
[Jiang et al. 09] [Kruszewski et al. 11, 12]

*Network delay: variable, asymmetric* →



# 4.1. Control with predictive model of the network

PhD E. Witrant 2005 + IEEE TAC 2007 (Witrant, Canudas, Georges, Almir)

with a model of the network and without packet loss (predictable delay)

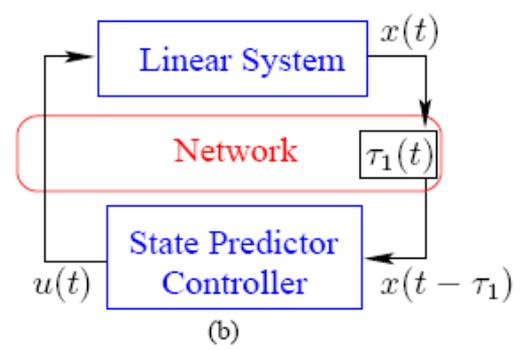
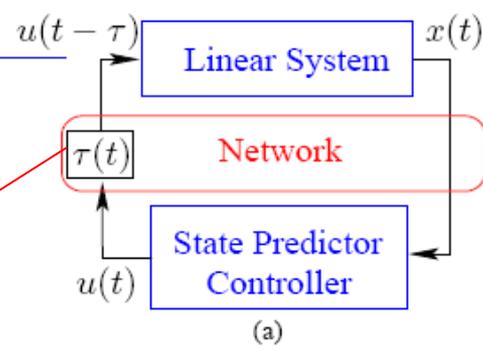
- state predictor with *variable* delays (implicit equation)
- controller of FSA type
- variable prediction horizon
- proven robustness (via *small gain*)
- Application to the T inverted pendulum

$$\begin{aligned} \dot{x}(t) &= Ax(t) + Bu(t - \tau(t)) \\ u(t) &= -Ke^{A\hat{\delta}(t)} \left[ x(t) + e^{At} \int_t^{t+\hat{\delta}(t)} e^{-A\theta} Bu(\theta - \hat{\tau}(\theta)) d\theta \right] \end{aligned}$$

where  $\hat{\delta}(t) = \hat{\tau}(t + \hat{\delta}(t))$  is the prediction horizon

$$\begin{aligned} \dot{x}(t) &= Ax(t) + Bu(t - \tau(t)), \\ y(t) &= Cx(t) \end{aligned}$$

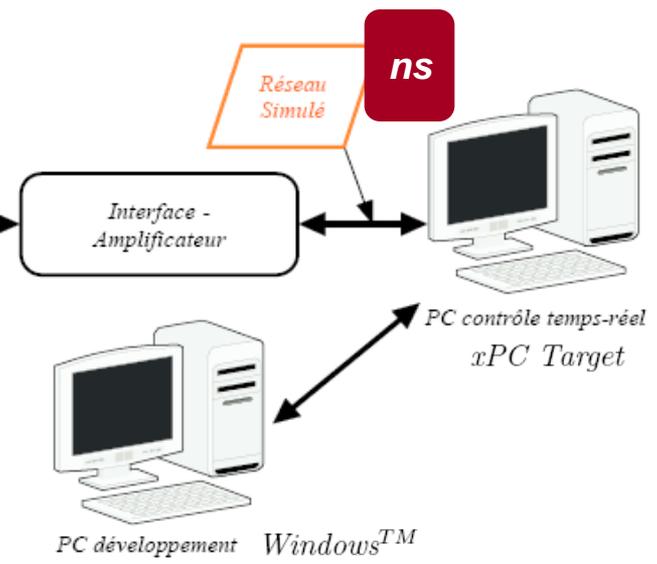
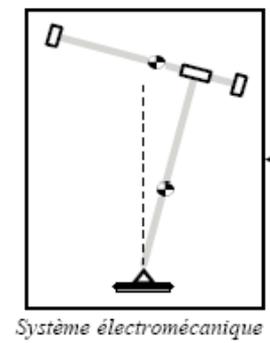
$$\begin{aligned} \dot{z}(t) &= f(z(t), u_d(t)), \quad z(0) = z_0 \\ \tau(t) &= h(z(t), u_d(t)) \end{aligned}$$



Time-delay on the actuator (a) and measurement (b) signals.



$$\dot{x}(t) = \begin{bmatrix} 0 & 1 & 0 & 0 \\ -18.785 & 0 & 14.820 & 0 \\ 0 & 0 & 0 & 1 \\ 56.924 & 0 & -15.181 & 0 \end{bmatrix} x + \begin{bmatrix} 0 \\ 7.520 \\ 0 \\ -8.824 \end{bmatrix} u$$



Retard induit par le réseau

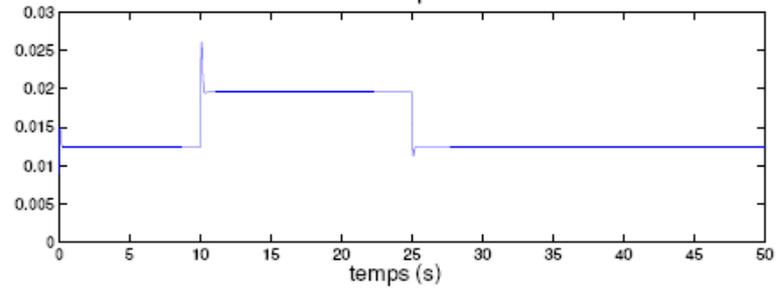
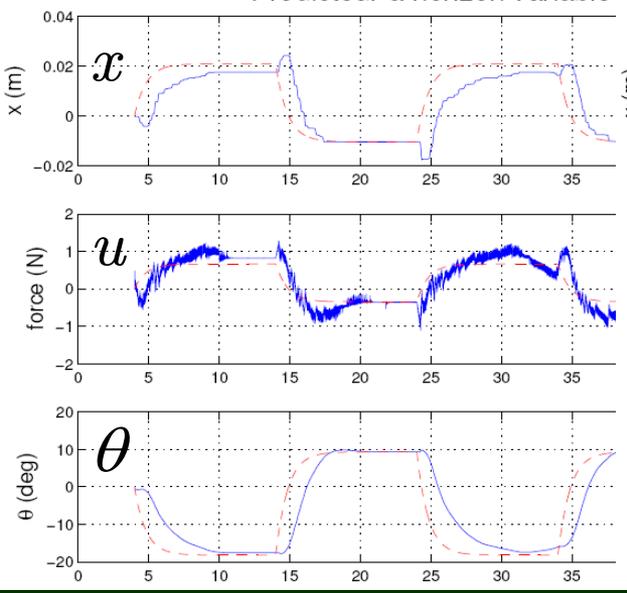
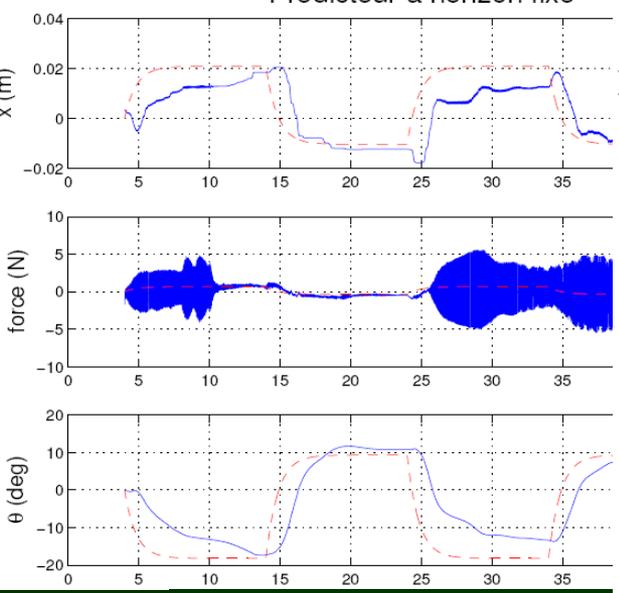


FIG. 5.6 – Banc d'essai expérimental.

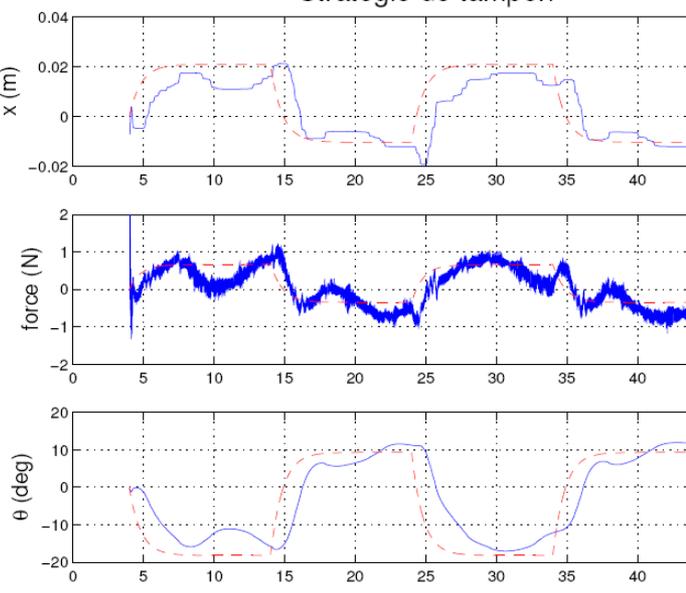
Prédicteur à horizon variable



Prédicteur à horizon fixe



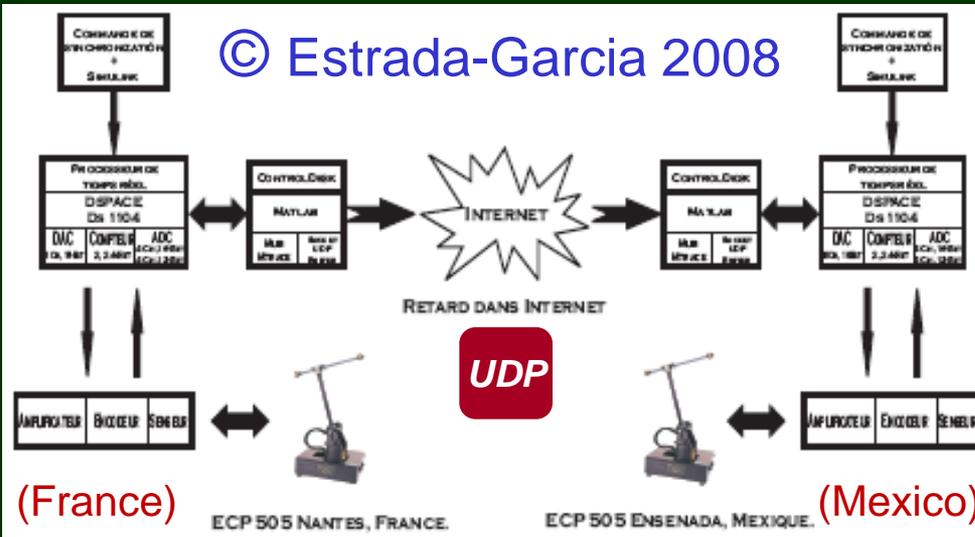
Stratégie de tampon



## 4.2. Control with buffers (two-way)

PhD H.J. Estrada-Garcia 2008 (+Moog, Marquez-Martinez)

© Estrada-Garcia 2008



**Aim:** synchronization of a Slave pendulum (Nantes) on a Master one (Ensenada).

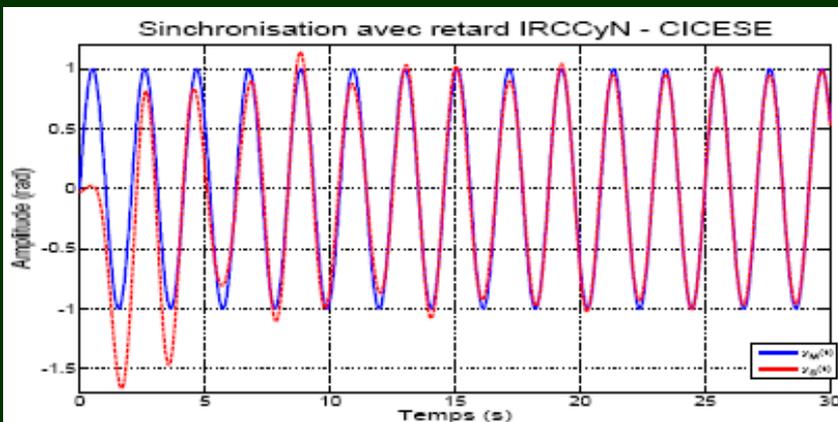
$y^{\text{ref}}$  supposed t.b. known from both sides.

**Strategy:**

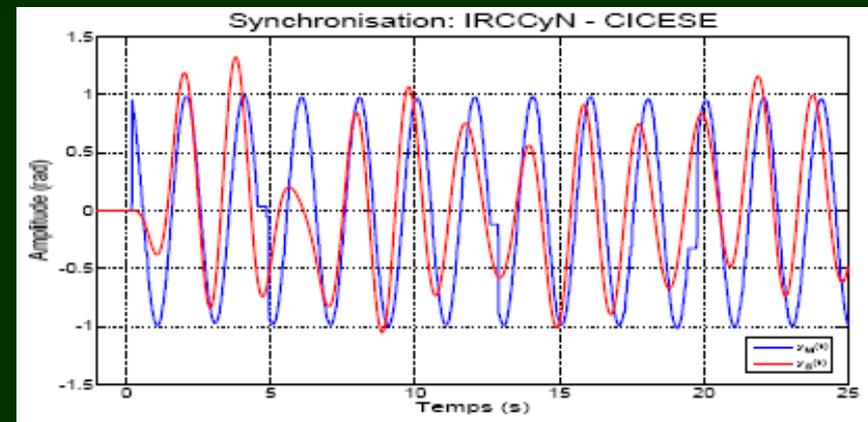
- 1) buffers at  $300\text{ms} = \tau$
- 2) control s.t. M/S error obeys:

$$e^{(3)}(t) + a_2 \ddot{e}(t - \tau) + b_2 \dot{e}(t - \tau) + c_2 e(t - \tau) = 0.$$

→ causal control



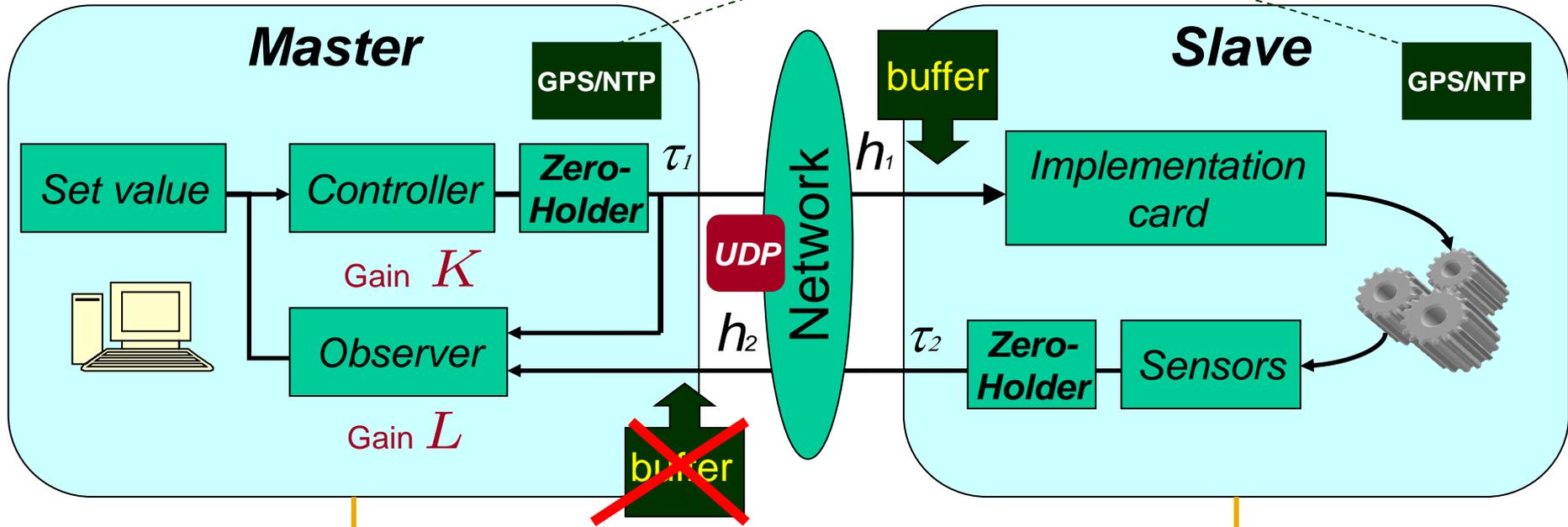
simulated pendulum, real network



real pendulum, real network

# 4.3. Commande avec tampon aller seul

PhD A. Seuret 2006 (+Dambrine, Richard)



$$\begin{cases} \dot{\hat{x}}(t) = A\hat{x}(t) + Bu(t - \delta_1(t)) \\ \quad -L(y(t - \delta_2(t)) - \hat{y}(t - \delta_2(t))), \\ \hat{y}(t) = C\hat{x}(t), \end{cases}$$

known thx to buffer

known thx to time-stamps

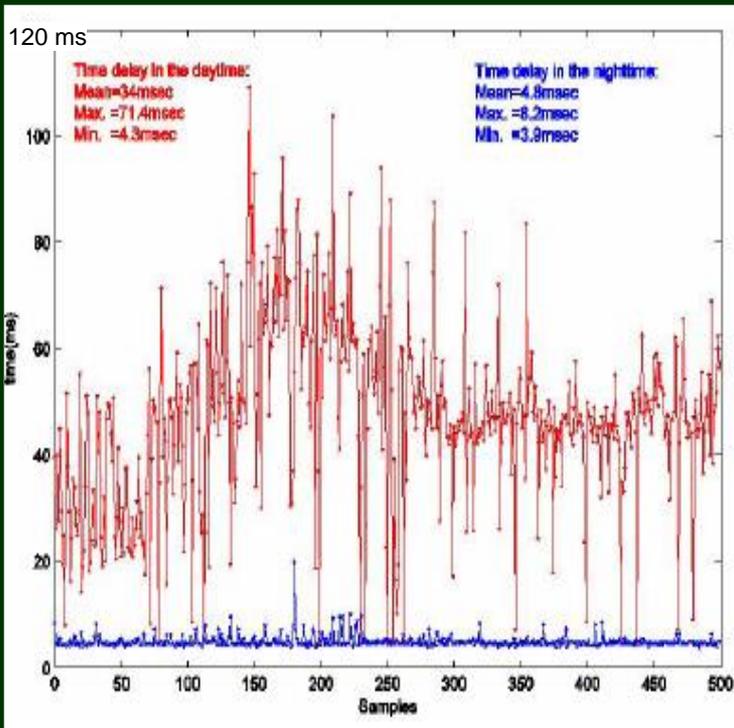
- defines the target
- receives Slave's output
- observes Slave's state
- computes & sends control

• Limited computation power

$$\begin{cases} \dot{x}(t) = Ax(t) + Bu(t - \delta_1(t)), \\ y(t) = Cx(t). \end{cases}$$

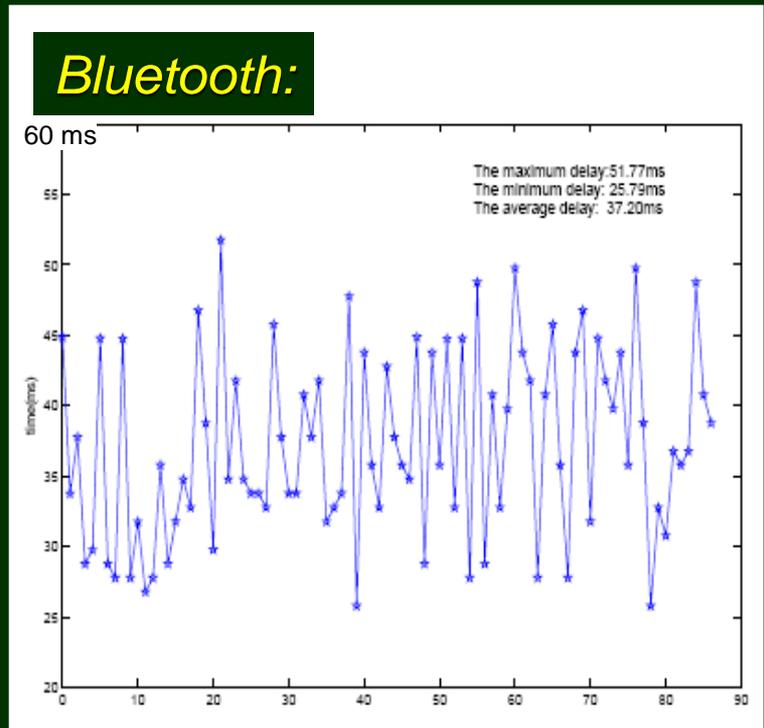
- receives & applies control
- sends measured output

Passage à l'expérimental + adaptation à la QoS disponible

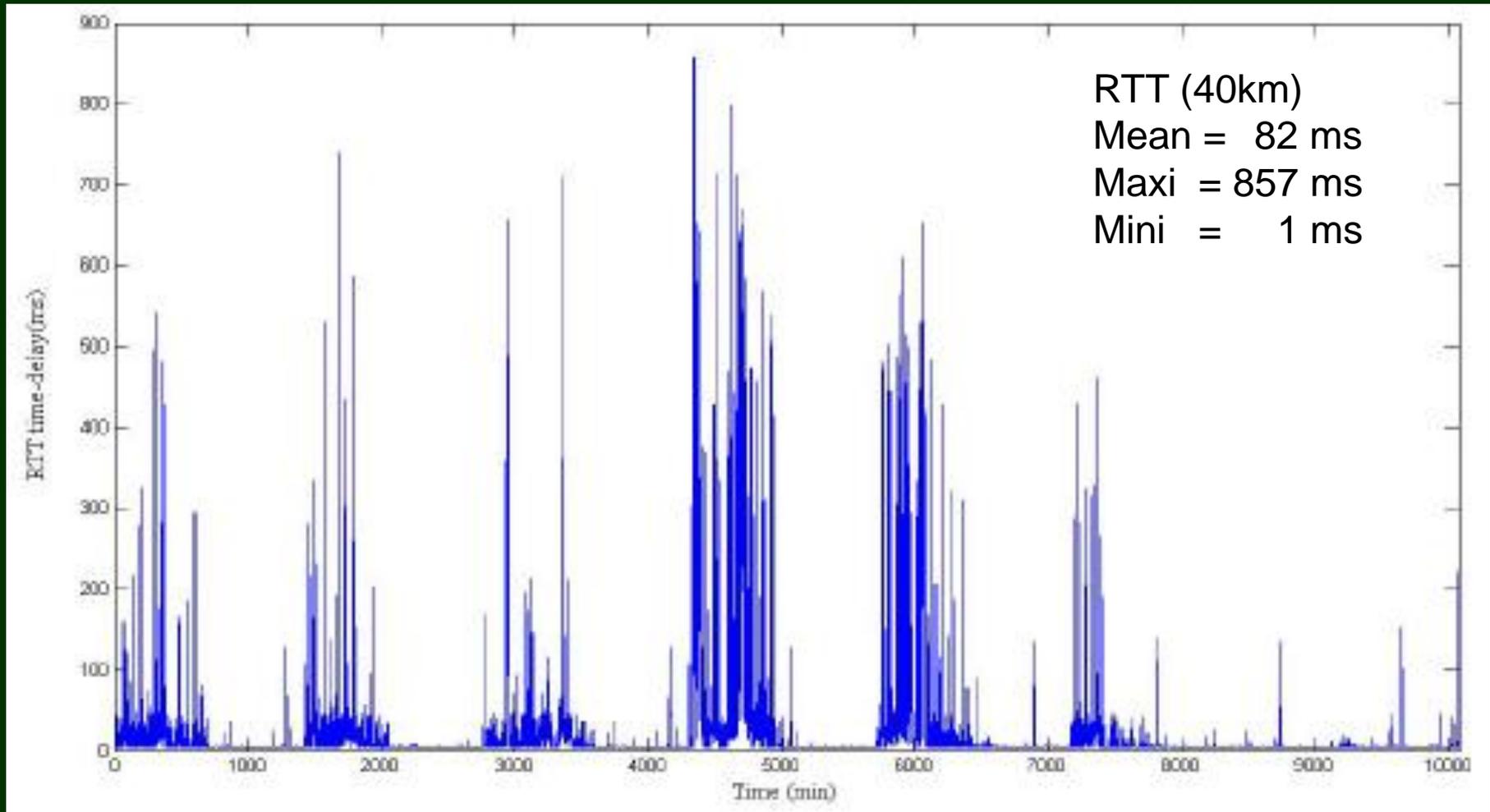


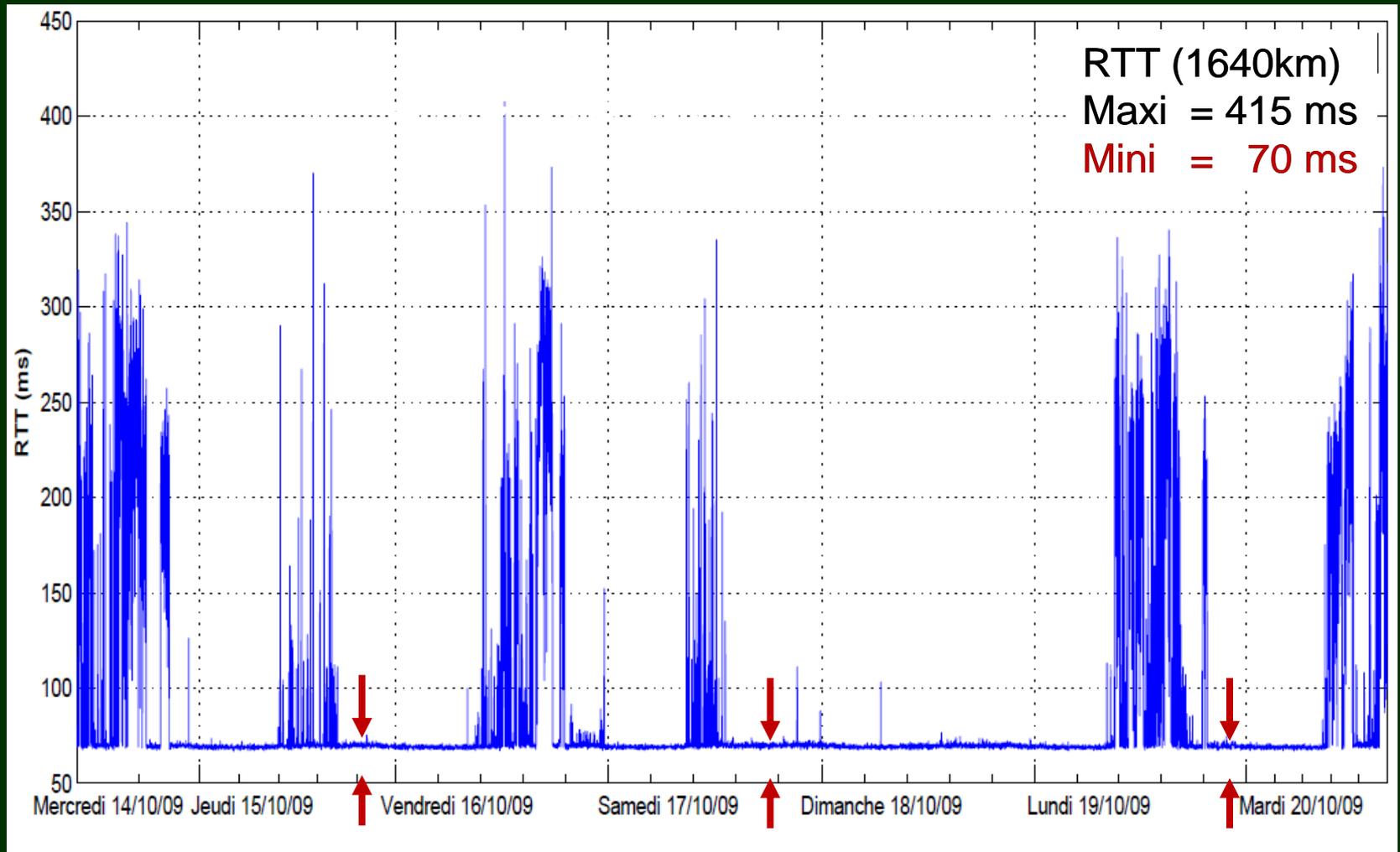
**Internet:**

Nighttime  
VS  
Daytime



# One week of RTT...





Tunis-Lille (1640 km) – Source: S. Belhaj, ENSIT 2009

Other RTT (approx. values):

unshared CAN 2m: 200µsec

bluetooth 2m: 40ms

internet 40km: 300ms

internet 1640km: 300ms

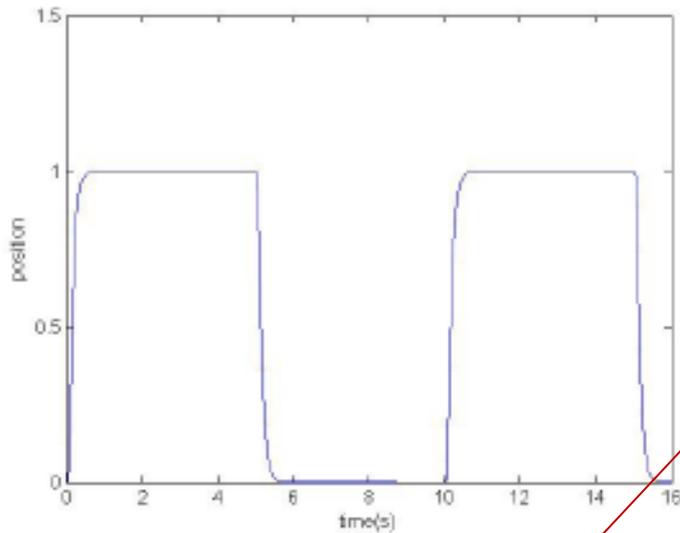
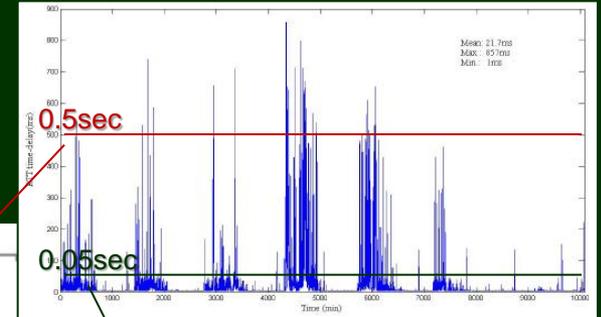
orbital stations: 0.4-7s

underwater 1.7km: >2sec

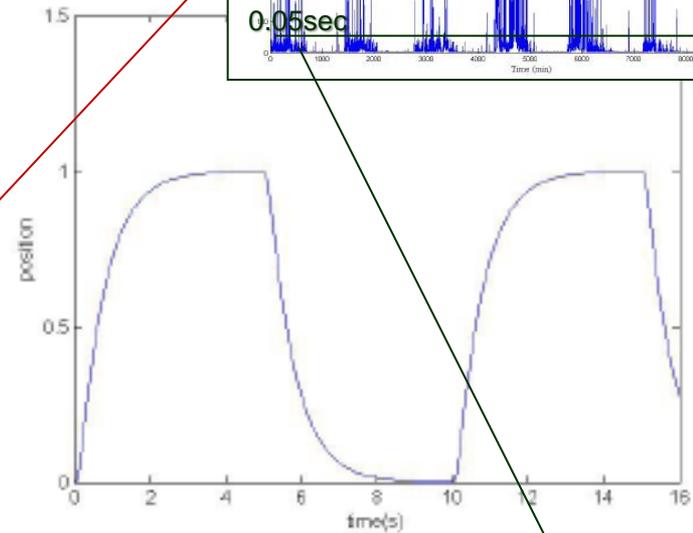


# One week of RTT...

*The achievable exponential rate depends on  $h_m$ , which motivates some adaptation w.r.t. QoS...*



$$h_m = 0.05s, \alpha = 8.74$$



$$h_m = 0.5s, \alpha = 0.96$$

Link max delay  $\leftrightarrow$  provable performance

## Model of the switching system

Two switching modes are considered : the big time-delay and the small time-delay.

$$1) \quad \dot{x}(t) = Ax(t) + \chi_{[h_1, h_2]}(\delta_{con}(t))BK_1x(t - \delta_{con}(t)) + (1 - \chi_{[h_1, h_2]}(\delta_{con}(t)))BK_2x(t - \delta_{con}(t)), \quad (8)$$

$$2) \quad \dot{e}(t) = Ae(t) - \chi_{[h_1, h_2]}(\delta_{obs}(t))L_1Ce(t - \delta_{obs}(t)) - (1 - \chi_{[h_1, h_2]}(\delta_{obs}(t)))L_2Ce(t - \delta_{obs}(t)). \quad (9)$$

$\chi : \mathbb{R} \rightarrow \{0, 1\}$  is defined by :

$$\chi_{[h_1, h_2]}(s) = \begin{cases} 1, & \text{if } s \in [h_1, h_2] \\ 0, & \text{otherwise.} \end{cases} \quad (10)$$

Note : we assume  $\chi(\delta_{con}(t)) = \chi(\delta_{obs}(t))$ .

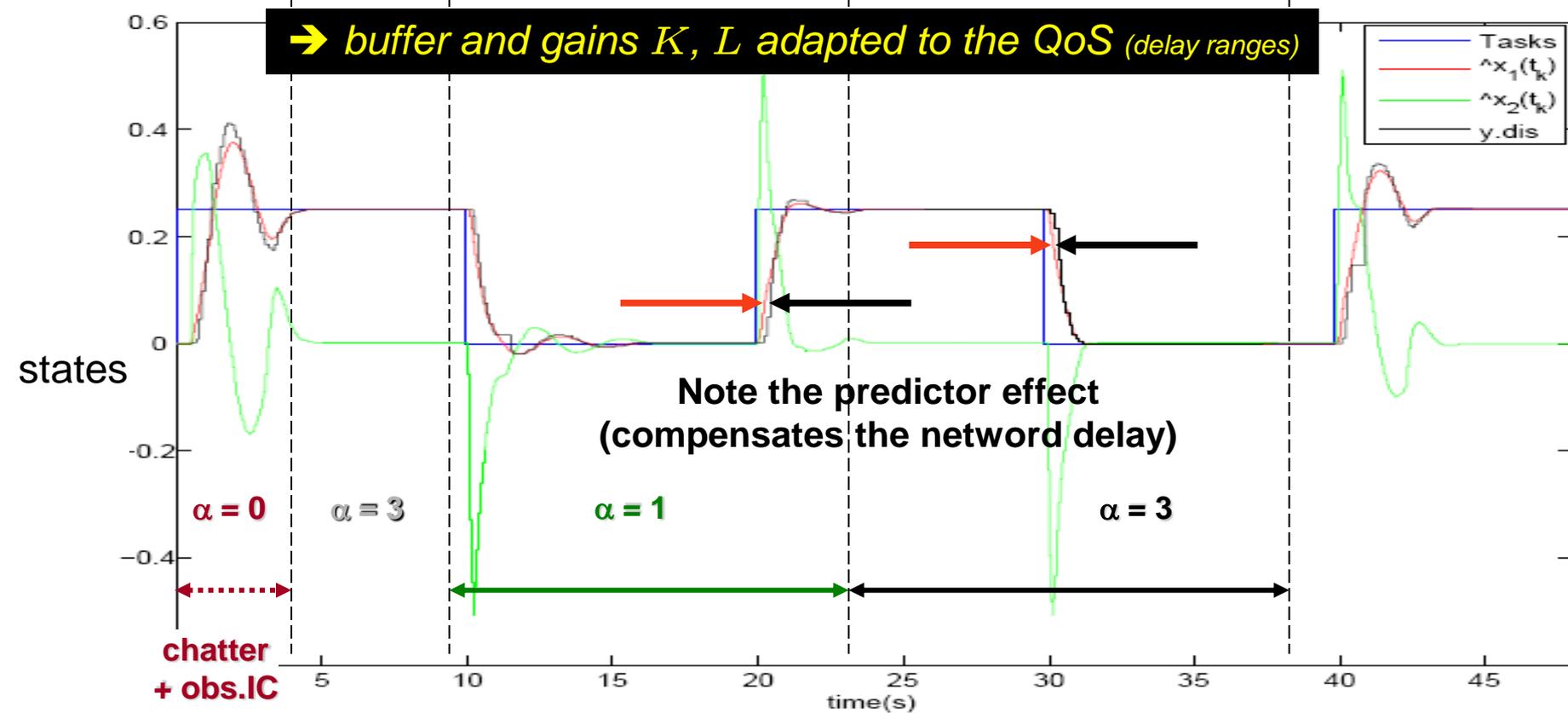
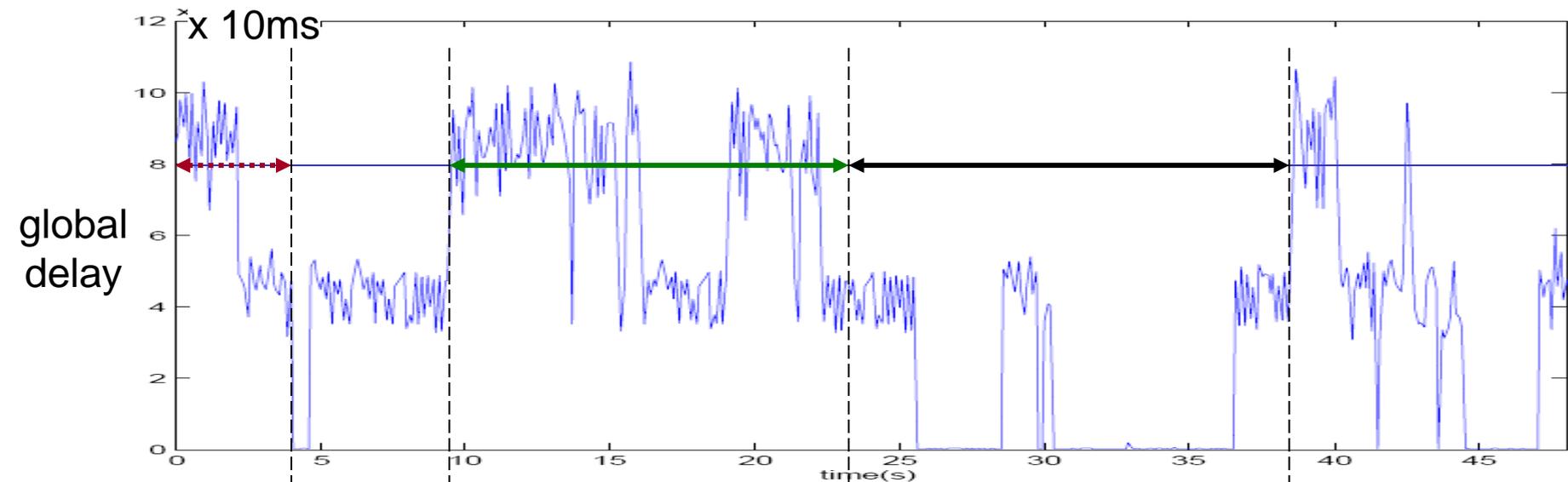
## General switched system

$$\dot{x}(t) = Ax(t) + \chi_{[h_1, h_2]}(\tau)A_1x(t - \tau(t)) + (1 - \chi_{[h_1, h_2]}(\tau))A_2x(t - \tau(t)), \quad (11)$$

## The LKF :

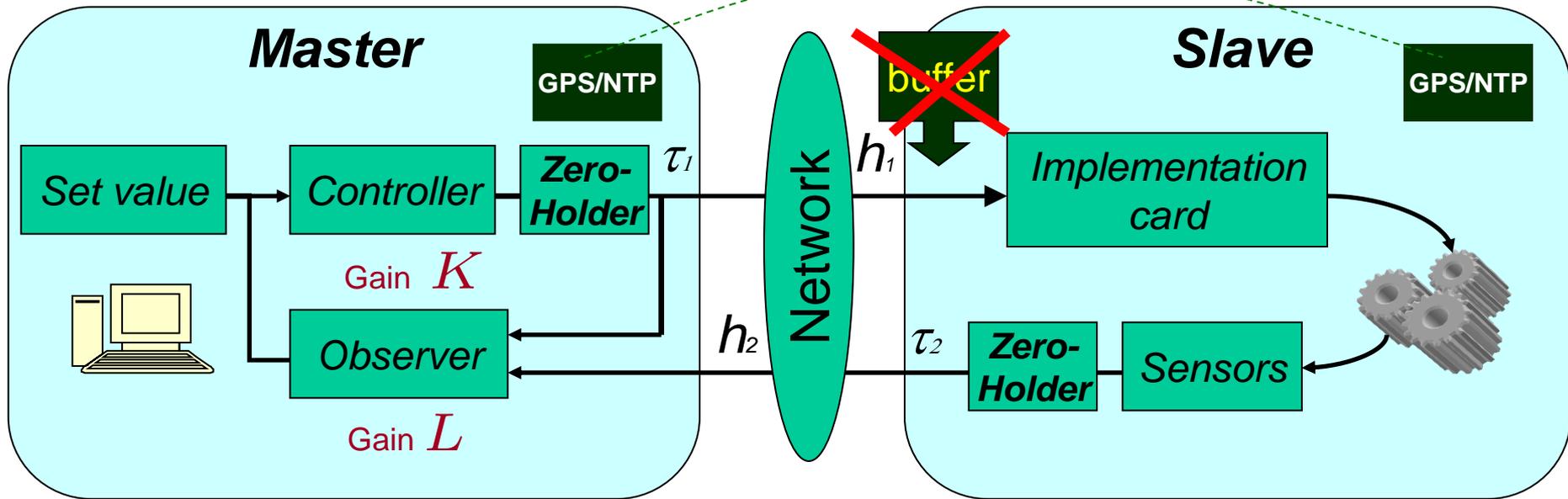
$$V(t, x_t, \dot{x}_t) = x^T(t)Px(t) + \sum_{i=0}^2 \int_{t-h_{i+1}}^t x^T(s)S_i x(s) ds + \sum_{i=0}^2 (h_{i+1} - h_i) \int_{-h_{i+1}}^{-h_i} \int_{t+\theta}^t x^T(s)R_i \dot{x}(s) ds d\theta, \quad (12)$$

where  $h_0 = 0$ ,  $P > 0$  and  $R_i, S_i \geq 0$ .



## 4.3. Buffer-free control (*event-driven*)

A. Seuret - JPR 2008 (theory) + W. Jiang, A. Kruszewski *et al.* (experim.+switches)  
cf. IEEE T. CST 2011

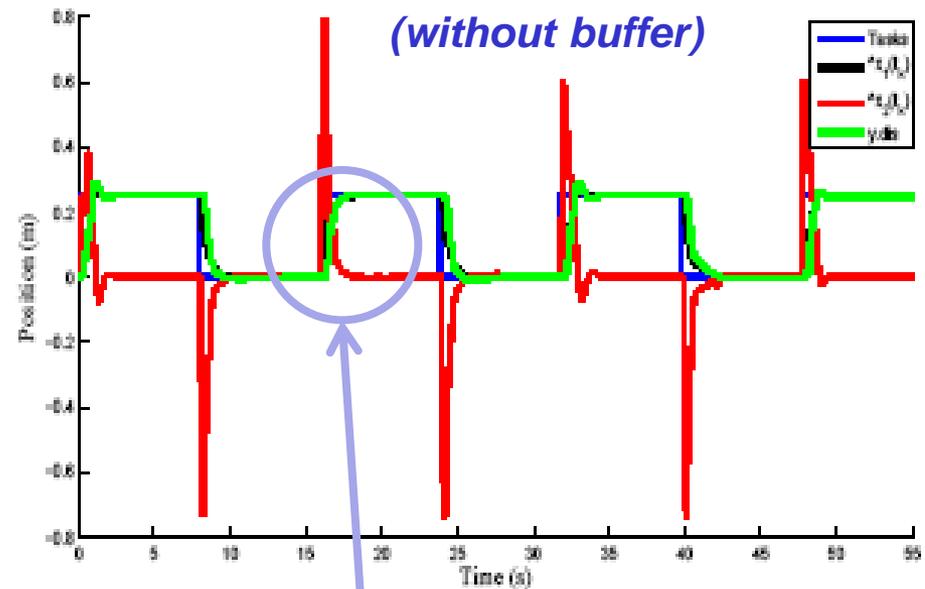
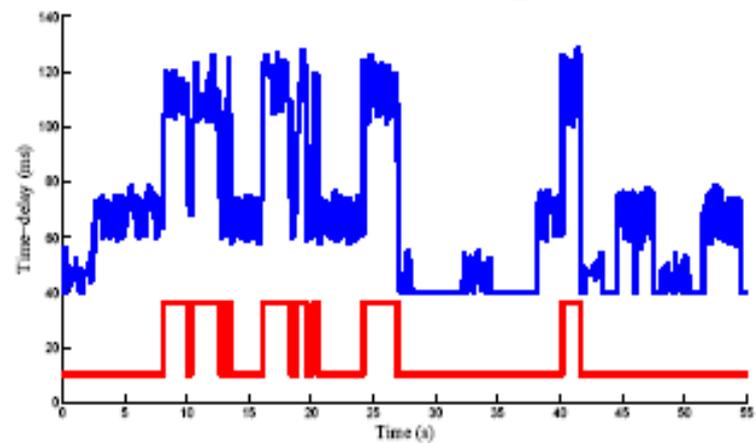
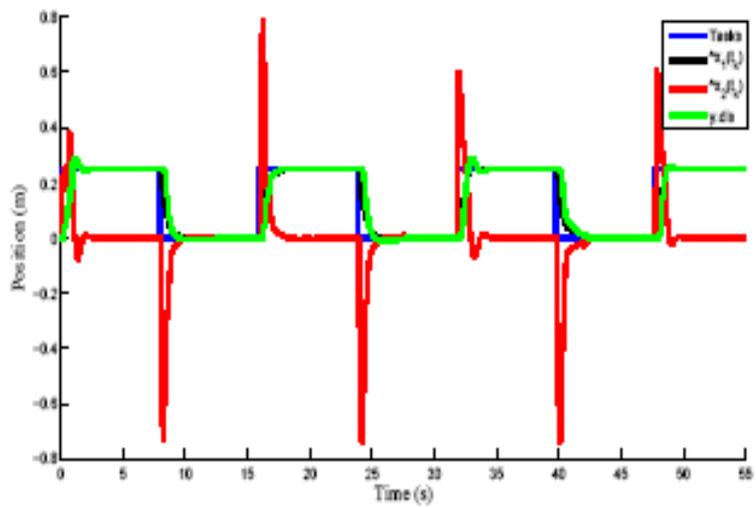


$$\hat{\delta} \neq \delta$$

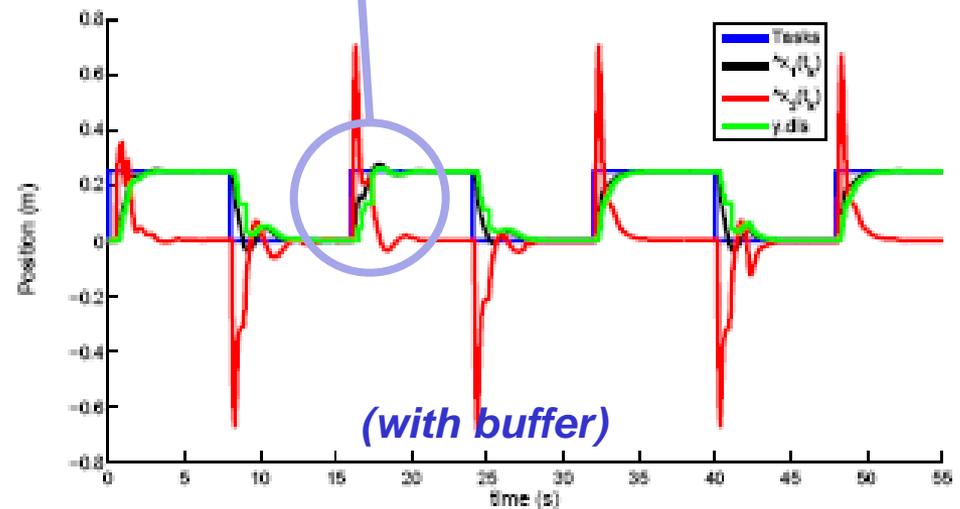
$$\begin{cases} \dot{\hat{x}}(t) = A\hat{x}(t) + Bu(t - \hat{\delta}_1(t)) \\ \quad -L(y(t - \delta_2(t)) - \hat{y}(t - \delta_2(t))), \\ \hat{y}(t) = C\hat{x}(t), \end{cases}$$

$$\begin{cases} \dot{x}(t) = Ax(t) + Bu(t - \delta_1(t)), \\ y(t) = Cx(t). \end{cases}$$

# Results from the event-driven mode

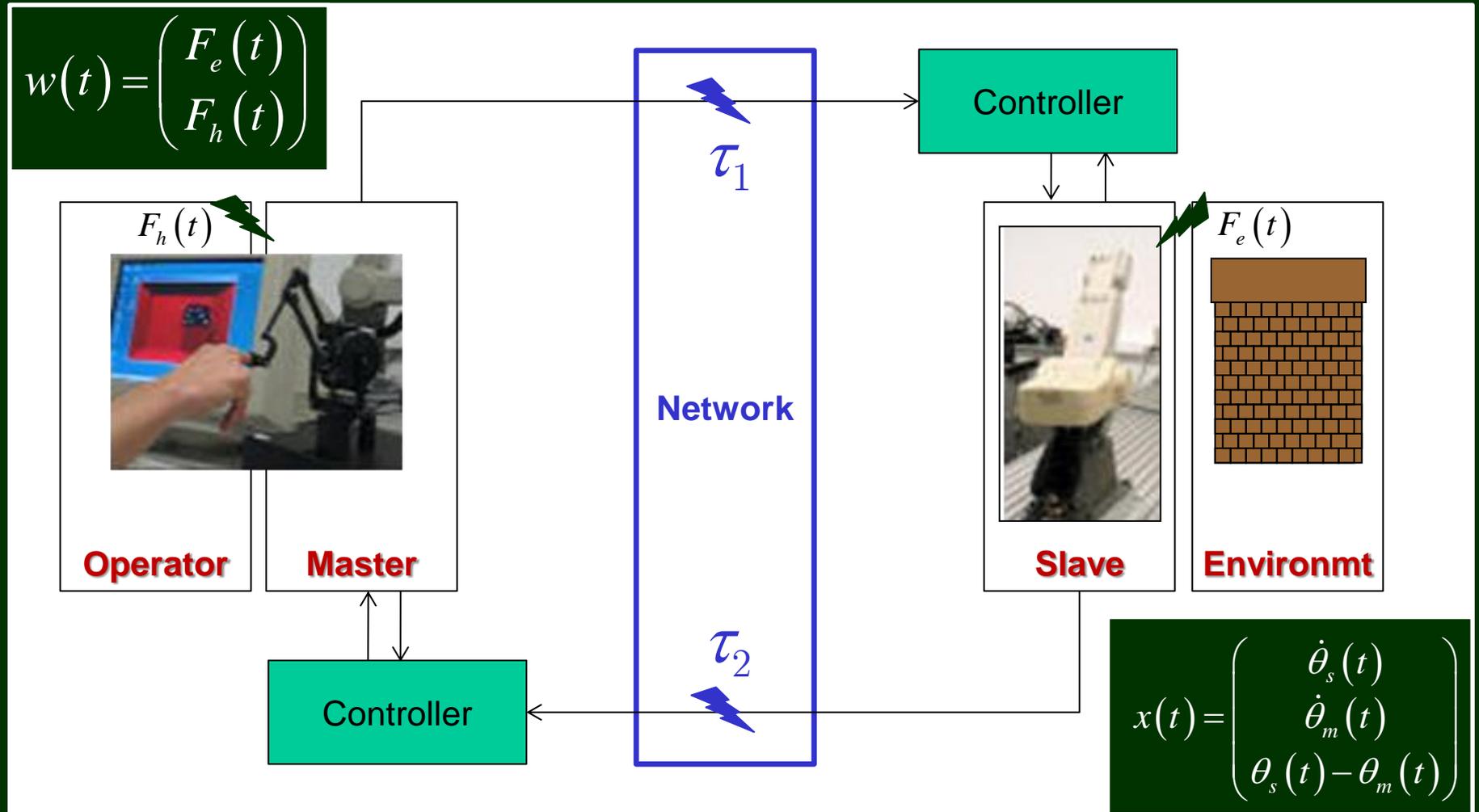


Event-driven vs. time-driven mode.



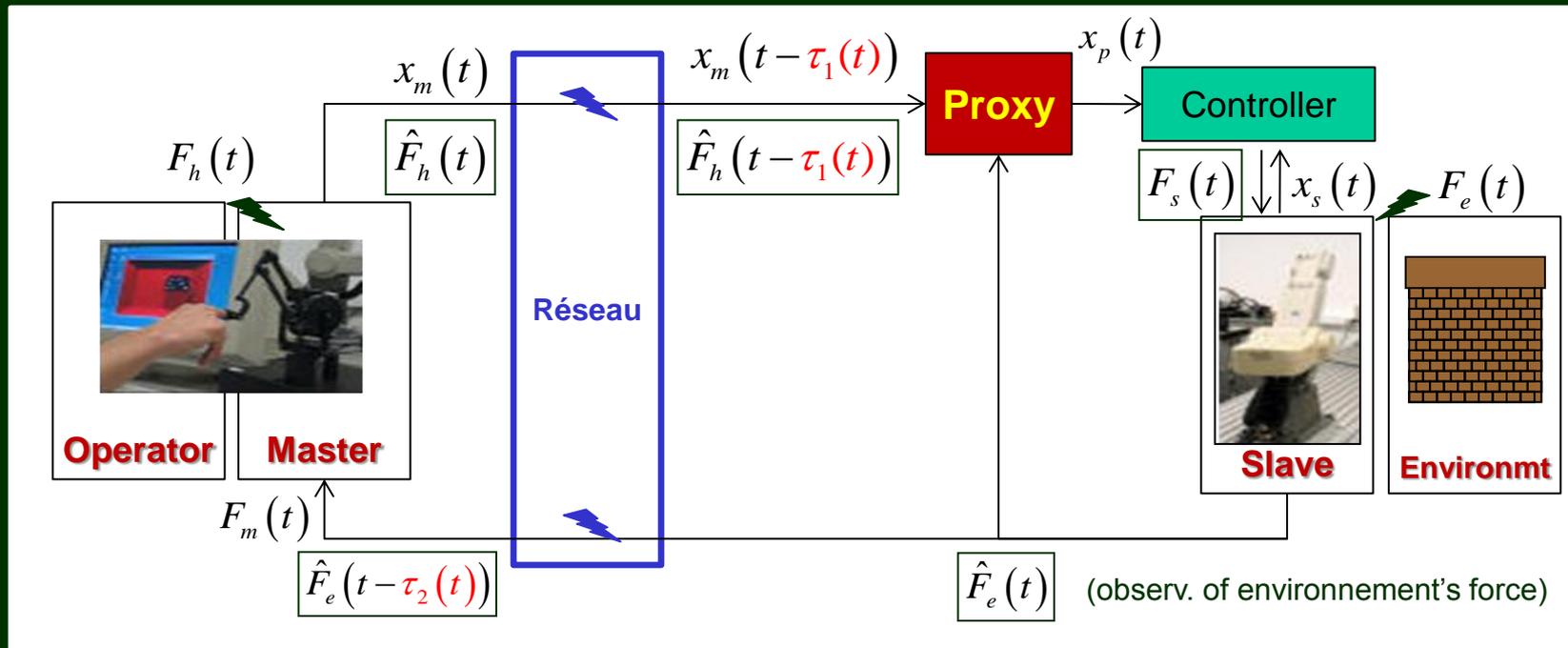
# Natural continuation: teleoperation (LKF + $H_\infty$ )

## 1) Basic scheme: position tracking - $\theta$ (no force target)



## 2) Improved scheme: force and position tracking (haptic rendering)

(ETFA 2011)



- Proxy synchronized on Master
- Slave synchronized on Proxy

Proxy « emulates » Master  
without delay



- Reduction of the delay effect
- Accurate haptic rendering

## 2) Improved scheme: force and position tracking (haptic rendering)

(ETFA 2011)



- Reduction of the delay effect
- Accurate haptic rendering

Combining LKF with  $H_\infty$ 

$$J(w) = \int_0^\infty (z(t)^T z(t) - \gamma^2 w(t)^T w(t)) dt < 0$$

To ensure  $J(w) < 0$ , we consider the condition,

$$\dot{V}(t, x(t), \dot{x}(t)) + z(t)^T z(t) - \gamma^2 w(t)^T w(t) < 0$$

We choose a Lyapunov-Krasovskii Functional candidate,

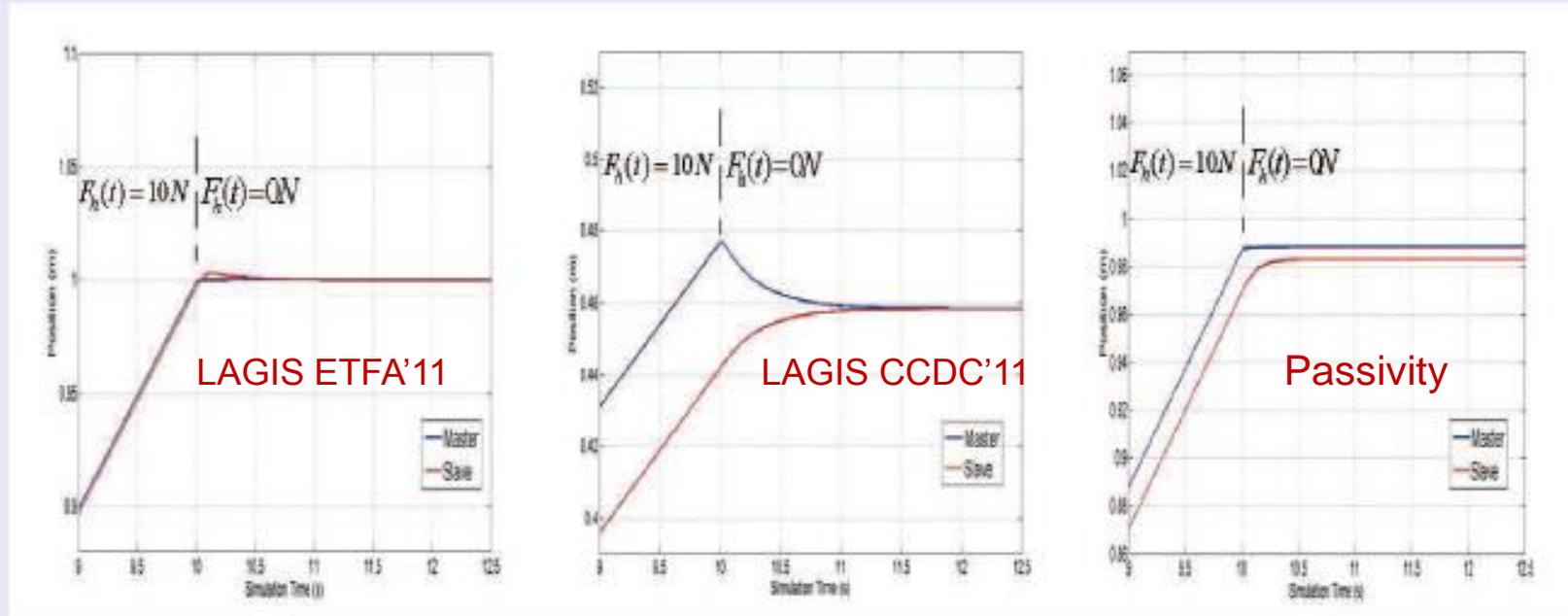
$$\begin{aligned} V(t, x(t), \dot{x}(t)) &= x(t)^T P x(t) \\ &+ \int_{t-h_2}^t x(s)^T S_a x(s) ds + \int_{t-h_1}^t x(s)^T S x(s) ds \\ &+ h_1 \int_{-h_1}^0 \int_{t+\theta}^t \dot{x}(s)^T R \dot{x}(s) ds d\theta \\ &+ \sum_{i=1}^n (h_2 - h_1) \int_{-h_2}^{-h_1} \int_{t+\theta}^t \dot{x}(s)^T R_{ai} \dot{x}(s) ds d\theta \end{aligned}$$

$$w(t) = \begin{pmatrix} F_e(t) \\ F_h(t) \end{pmatrix}$$

$$x(t) = \begin{pmatrix} \dot{\theta}_s(t) \\ \dot{\theta}_m(t) \\ \theta_s(t) - \theta_m(t) \end{pmatrix}$$

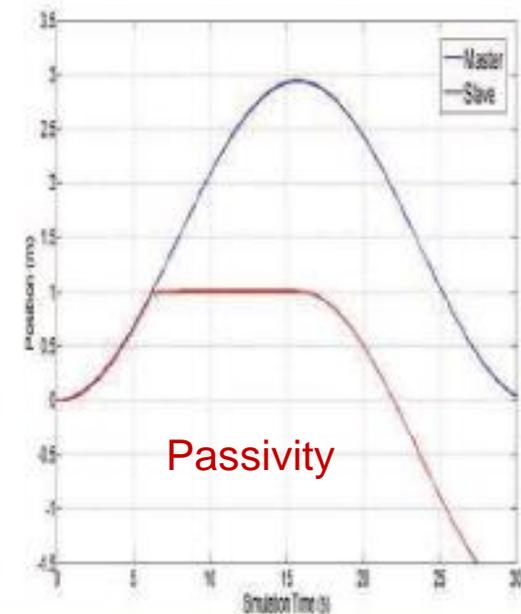
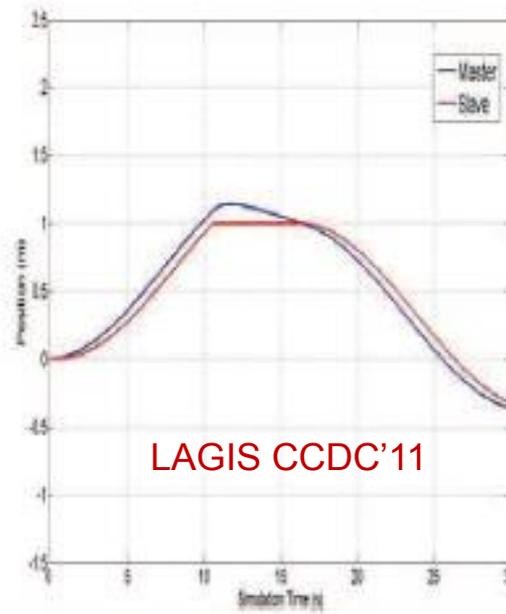
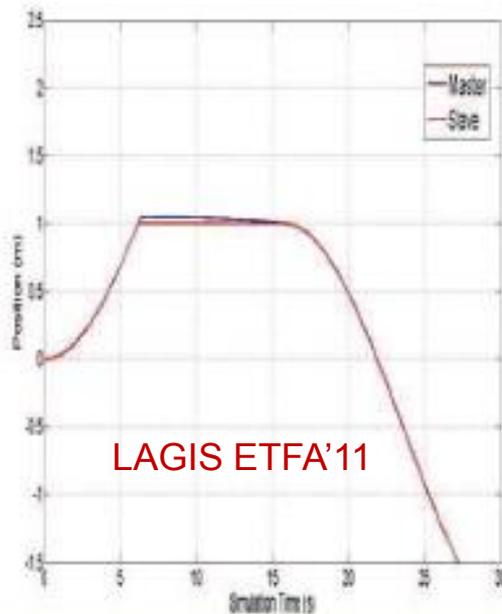
$\rightarrow = z(t)$

# Tracking in abrupt changing motion :



- Left Figure : new proxy control scheme.
- Middle Figure : new control scheme (B. Zhang, A. Kruszewski, J.-P. Richard, CCDC, 2011).
- Right Figure : passivity theorem (Y. Ye, Y.-J. Pan and Y. Gupta, CDC, 2009).

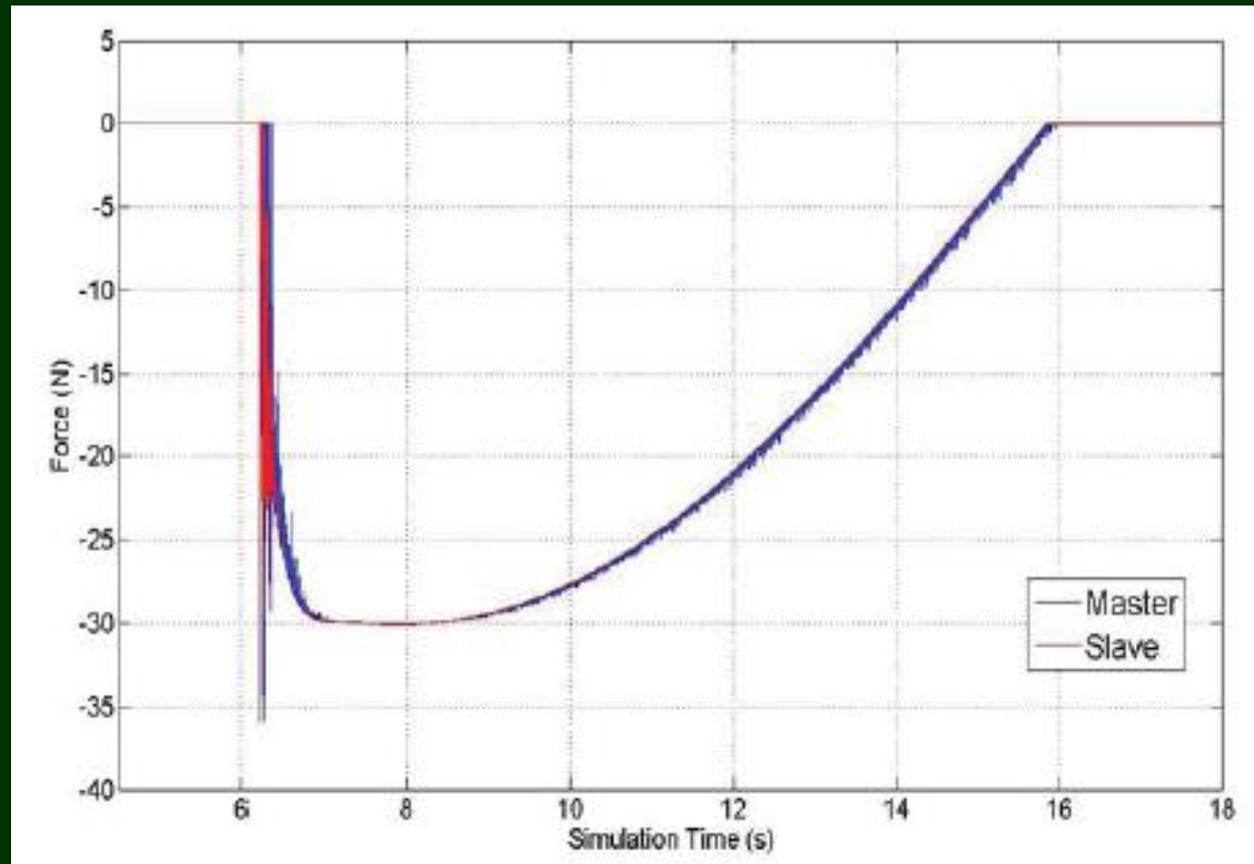
# Tracking in wall contact motion :



- The hard wall : the stiffness  $K_e = 30kN/m$ , the position  $x = 1.0m$ .
- Left Figure : new proxy control scheme.
- Middle Figure : new control scheme (B. Zhang, A. Kruszewski, J.-P. Richard, CCDC, 2011).
- Right Figure : passivity theorem (Y. Ye, Y.-J. Pan and Y. Gupta, CDC, 2009).

➔ the proxy structure allows for reducing the lag

and gives a good force rendering...



## Intermediate conclusion on bilateral teleoperation

- Classical solution = passivity, without performance
- Alternative LFK + Hinf, various possible structures:
  - position/Position (CCDC 2011)  $\Rightarrow$  position tracking OK
  - force/Position (ETFA 2011)  $\Rightarrow$  position +haptic rendering
  - LMI conditions  $\Rightarrow$  stability + performance  $\gamma$
  - under variable delays (estimated by means of time stamps+NTP)
  - and still *buffer-free*...

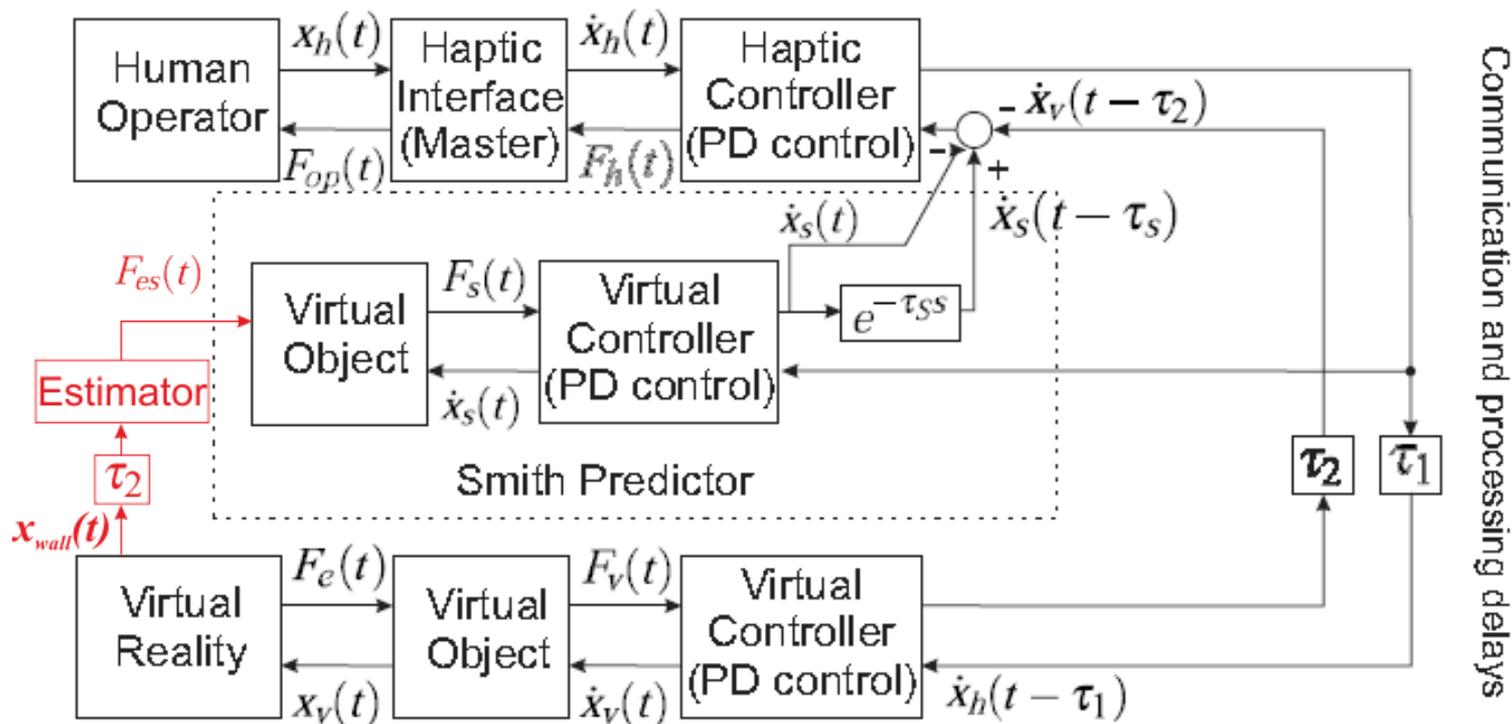
# An other work on bilateral teleoperation

## "Network-based haptic systems with time-delay"

B. LIACU 2012 (NICULESCU, ANDRIOT, COLLEDANI, BOUCHER, DUMUR)



- Aim: improve the end user *perception*.
- *Smith predictor with distance feedback*, uses the information from the virtual environment so to have a better predictor model in wall contact.
- Experiments with simulated **constant delays 50-80ms**.



# Overview

- Motivations and examples
- Modelling
- Sampling and delay
- A very basic example
- Control : *to buff, or not to buff?* A selection of results
- **Conclusions**

# Conclusion-Summary

- Quite general problems formulated thx to delay/switch models  
⇒ *design in the presence of variable delays*
- Control with a network model [Witrant 05] predictor with variable delay
- General case (without network model) :
  - ✓ with 2 buffers [Estrada 08] retarded error equation
  - ✓ with 1 buffer [Seuret 06] state feedback + observ./predict.
  - ✓ + adapt. to QoS [Jiang-Kruszewski-R-T 08] “
  - ✓ with 0 buffer [S-R 08, Jiang-K-R-T 09] “
- Bilateral teleoperation with performance (alternative to passivity)
  - ✓ with 0 buffer [Zhang-K-R 11] state feedback + obs +  $H_\infty$

# Other healthy readings:



*"A switched system approach to exponential stabilization through communication network"*

A. KRUSZEWSKI, W.J. JIANG, E. FRIDMAN, J.P. RICHARD, A.TOGUYENI

IEEE TCST, 20 (4), pp. 887–900, 2012

*"A novel control design for delayed teleoperation based on delay-scheduled Lyapunov-Krasovskii functionals"*

A. KRUSZEWSKI, B. ZHANG, J.P. RICHARD

Int. J. Control, accepted May 2013, to appear.

*"Control design for teleoperation over unreliable networks: A predictor-based approach"*

A. KRUSZEWSKI, B. ZHANG, J.P. RICHARD

Springer, in *Delay Systems: From Theory to Numerics and Appl.*, Edt. Vyhldal, Lafay, Sipahi., 2013

*"Remote Stabilization via Communication Networks with a Distributed Control Law"*

E. WITRANT, C. CANUDAS DE WIT, D. GEORGES, M. ALAMIR

IEEE TAC, vol. 52, pp. 1480-1485, 2007

*"Master-Slave synchronization for two inverted pendulums with communication time-delay"*

H J. ESTRADA-GARCIA, L.A. MARQUEZ-MARTINEZ, C.H. MOOG

Springer LNCIS vol.388, 2009, Chap. Part V, pp. 403-414.

*"Control of a remote system over network including delays and packet dropout"*

A. SEURET, J.P. RICHARD

IFAC'08, 17th IFAC World Congress, Seoul, South Korea, July 2008

*"A refined input delay approach to sampled-data control"*

E. FRIDMAN, Automatica, 48 (2), 2010

*"SOS for sampled-data systems"*

A. SEURET, M. PEETS, IFAC'11, Milano, Italy, 2011

*"A novel stability analysis of linear systems under asynchronous samplings"*.

A. SEURET, Automatica 48 (1), pp. 177-182, 2011

... ongoing at  on in this area

- Scheduling issues: aperiodic sampling for *nonlinear* systems (PhD Hassan Omran Feb. 2014 → hybrid/dissipativity)



*"Stability of bilinear sampled-data systems with an emulation of static state feedback"*

H. OMRAN, L. HETEL, J.P. RICHARD, F. LAMNABHI-LAGARRIGUE

CDC'12, 51st Conf. on Decision & Control, Hawaii, USA, 2012

*"On the stability of input-affine nonlinear systems with sampled-data control"*

H. OMRAN, L. HETEL, J.P. RICHARD, F. LAMNABHI-LAGARRIGUE

ECC'13, 12th European Control Conf., Zurich, Switzerland, 2013

- Keep on developping experimental platforms

- NCS@LAGIS (various benchtests with Wifi – Zigbee – LAN – CAN – wired)
- EquipEx FUN Future Internet of Things (WSRN)

The logo for Inria, featuring the word 'Inria' in a red, cursive script font. Below it, the tagline 'INVENTORS FOR THE DIGITAL WORLD' is written in a smaller, red, sans-serif font.

